



17 **Abstract**

18 An integrated model for membrane bioreactors (MBR) was employed in view of the management  
19 optimization of an MBR biological nutrient removal (BNR) pilot plant in terms of operational costs  
20 and direct greenhouse gases emissions. The influence of the operational parameters (OPs) on  
21 performance indicators (PIs) was investigated by adopting the Extended-FAST sensitivity analysis  
22 method. Further, a multi-objective analysis was performed by applying the Technique for Order of  
23 Preference by Similarity to Ideal Solution (TOPSIS). The results show-up that the sludge retention  
24 time is the OP mostly affecting all the investigated PIs. By applying the set of optimal OPs, there was  
25 a reduction of 48% and 10% of the operational costs and direct emissions, respectively.

26

27 **Keywords:** Mathematical modelling optimization, multi-objective analysis, wastewater treatment  
28 plant, greenhouse gases, membrane fouling.

29

## 30 **1. Introduction**

31 The aim of this paper is to describe methods to minimize the environmental footprint for membrane  
32 bioreactors (MBR). Several parameters will influence the footprint, such as effluent quality,  
33 operational cost, energy consumption and greenhouse gas (GHG) emissions. Consequently, the  
34 minimization has to be addressed by using multicriteria optimization, where the various influencing  
35 factors can be weighted in different ways. The aim of the study is to obtain operating strategies that  
36 will reduce the environmental footprint.

37 Wastewater treatment plants (WWTP) are focusing new challenges and are moving towards new  
38 frontiers which include complying with increased wastewater **discharge** standards, reducing  
39 greenhouse gas (GHG) emissions, **minimizing** operational and capital cost for the treatment facilities,  
40 increasing effective energy management, using more compact systems and reducing the WWTP  
41 footprint (Sweetapple et al., 2014; Bozkurt et al., 2016). Indeed, WWTPs are shifting from being  
42 "end-of-the-pipe" solutions to resource recovery sites (Puyol et al., 2016). GHG emissions are mainly  
43 generated in the biological processes, some of them occurring from the process reactions (direct  
44 emissions – DE), and others from electricity consumption (indirect emissions - IE) (IPCC, 2013). The  
45 main emitted GHGs are carbon dioxide (CO<sub>2</sub>), methane (CH<sub>4</sub>) and nitrous oxide (N<sub>2</sub>O) (Mannina et  
46 al., 2016). Among the GHGs, N<sub>2</sub>O is of special interest due to its great global warming potential  
47 (GWP) and the high capacity to deplete the ozone layer (IPCC et al., 2007; Mannina et al., 2018). An  
48 accurate quantification of GHG emissions is an important step to reduce process footprint. Plant land  
49 occupation is an essential factor to consider, and it is suggested that membrane bioreactors (MBR)  
50 adoption as a viable solution to meet lower effluent demands and reduced space requirements (Judd,  
51 2010; Atasanova et al., 2017). Mathematical models are powerful tools to quantify GHG emissions,  
52 comparing different WWTP design and operational strategies (Mannina et al., 2016). Several  
53 mathematical models have been proposed in literature for accounting GHG emissions ranging from  
54 empirical simplified to mechanistic approaches (Pocquet et al., 2016; Spérandio et al., 2016).

55 However, only few mathematical models quantify GHG emission from MBRs (Mannina et al., 2018).  
56 MBRs differ from conventional activated sludge systems (CASs) and CAS results cannot easily be  
57 translated to MBR operations (Judd, 2010; Mannina et al., 2018). Consequently, MBR footprint  
58 optimization requires dedicated studies. As an illustration of the multiple criteria problem, a reduction  
59 of the airflow rate in the aerobic reactor, for minimizing the energy consumption, may increase the  
60 N<sub>2</sub>O emissions because of incomplete nitrification (Flores-Alsina et al., 2014). The identification of  
61 the interrelationship between operational conditions and direct (i.e., N<sub>2</sub>O, CH<sub>4</sub> and CO<sub>2</sub>) and indirect  
62 (i.e., energy consumption) GHG emissions represents a key issue in reducing the environmental  
63 footprint (Mannina et al., 2017). Multi-objective optimization is aiming to cope with competing  
64 criteria that will influence the footprint. Such a tool can help decision makers on obtaining a deeper  
65 perception of necessary trade-offs between conflicting operational strategies (Sweetapple et al., 2014;  
66 Wang and Rangaiah, 2017). Maere et al. (2011) compared several control and operational strategies  
67 to optimize MBR operation. Authors found effective results for the MBR operation optimization by  
68 employing closed loop aeration (based on a fixed dissolved oxygen concentration inside the aerobic  
69 reactor) rather than open loop. Indeed, by implementing the closed loop aeration, a reduction of the  
70 operational costs by 13-17% was obtained (Maere et al., 2011). Despite useful insights gained by  
71 Maere et al. (2011), the results were obtained using an ideal membrane (i.e., neglecting the interplay  
72 between physical and biological processes). Therefore, the results may not be directly applicable to  
73 full scale MBR systems. Sweetapple et al. (2014) presented a study on a multi-objective optimisation,  
74 for a CAS system, taking into account GHGs, effluent quality and operational costs. Different  
75 problem formulations were explored to identify the most effective approach and the optimal set of  
76 parameters for plant operation. Main conclusions were that GHG emissions could be substantially  
77 reduced without increasing operational costs (Sweetapple et al., 2014). Another multi-objective  
78 optimization for a CAS system was carried out by Long et al. (2019). The authors applied Monte  
79 Carlo simulations to optimize costs and reduce pollution from an industrial WWTP. Their study was  
80 applied for pre-treatment, centralized and reclaimed wastewater facilities and the results showed how

81 pollutant level and operational costs were related. Their results confirmed the importance to apply  
82 multiple objectives to balance costs and pollution. The fact that many criteria, such as energy  
83 reduction, membrane fouling, and GHG emission, are influenced in different directions, **which**  
84 motivate the use of multiple criteria optimization. This has been clearly demonstrated for CAS  
85 systems (see e.g., Flores-Alsina et al., 2014). Even if multi-objective optimization has been applied  
86 for CAS system, there are no studies presented for MBR system, to the authors' knowledge, **whereas**  
87 **minimizing MBR environmental footprint considering multiple objectives is highly desired.**

88 In this paper an integrated MBR mathematical model was adapted to a University of Cape Town  
89 (UCT)-MBR pilot-plant (Mannina et al., 2018). The influence of five operational parameters on ten  
90 performance indicators has been explored. Multi-objective optimization analysis has been used to  
91 find the trade-off between plant performance and cost.

92

## 93 **2. Material and methods**

### 94 **2.1 Mathematical model description and application**

95 The MBR integrated model described in (Mannina et al., 2018) is applied here. The model consists  
96 of biological (Mannina et al., 2018) and physical (Mannina et al., 2011) sub-models. The biological  
97 sub-model is described by 116 parameters and 25 state variables. The model includes nitrogen  
98 transformation considering two- step nitrification and four-step denitrification processes (Pocquet et  
99 al., 2016; Hiatt and Grady, 2008).

100 In the first nitrification step, the model considers the ammonia ( $\text{NH}_4$ ) oxidation into nitrite ( $\text{NO}_2$ ) by  
101 means of ammonia-oxidizing bacteria (AOB). The second step describes oxidation of  $\text{NO}_2$  into  $\text{NO}_3$   
102 by means of nitrite-oxidizing bacteria (NOB). In the first step incomplete ammonia oxidation is  
103 incorporated. This may lead to the formation of intermediate products, such as hydroxylamine

104 (NH<sub>2</sub>OH) and nitric oxide (NO). Furthermore, incomplete oxidation of NH<sub>2</sub>OH into NO<sub>2</sub> with the  
105 accumulation of NO, and further reduction into N<sub>2</sub>O is also included in the model.

106 The model takes into account that phosphorus accumulating organisms (PAOs) and heterotrophic  
107 non-PAO biomass (OHO) contribute under anoxic conditions to the four-step denitrification. This  
108 includes: (i) reduction of NO<sub>3</sub> to NO<sub>2</sub>; (ii) reduction of NO<sub>2</sub> to NO; (iii) reduction of NO to N<sub>2</sub>O; and  
109 (iv) reduction of N<sub>2</sub>O to N<sub>2</sub>. The incomplete reduction of N<sub>2</sub>O into N<sub>2</sub> leading to N<sub>2</sub>O accumulation  
110 and emission (Mannina et al., 2018) is part of the model.

111 The biological sub-model evaluates the total GHG emissions (both in terms of N<sub>2</sub>O and CO<sub>2</sub>) as the  
112 sum of direct and indirect emissions.

113 The physical sub-model is characterized by 6 parameters and 2 state variables. Overall, four key  
114 processes occurring during the membrane physical filtration are taken into account (Mannina et al.,  
115 2011): (i) cake layer formation during the filtration and backwashing phases; (ii) partial organic  
116 matter removal in the cake layer; (iii) **chemical oxygen demand** (COD) removal due to the physical  
117 retention effect of the membrane as a barrier (pre-filter effect); and (iv) membrane fouling.

118 Biological and physical sub-models are highly interrelated as a result of total suspended solid (TSS)  
119 and **soluble microbial products** (SMP) interactions. Further details regarding the MBR integrated  
120 model can be found in Mannina et al., (2011, 2018).

121 The model has been applied to a UCT- MBR pilot plant, consisting of anaerobic (62 L), anoxic (102  
122 L) and aerobic (221 L) reactors in series. The solid-liquid separation phase was accomplished by an  
123 ultrafiltration hollow fiber membrane module (PURON® Triple Bundle Demo Module with a  
124 nominal pore size of 0.03 µm and a membrane area of 1.4 m<sup>2</sup>) located inside the aerated MBR reactor  
125 (Mannina et al., 2018). An oxygen depletion reactor (ODR) was installed between the MBR and the  
126 anoxic reactors to reduce the amount of oxygen recycled with the flow rate ( $Q_{RAS} = 80 \text{ L h}^{-1}$ ). For a  
127 more detailed description of the pilot plant we refer to Mannina et al. (2018).

## 128 2.2 Sensitivity Analysis

129 Sensitivity analysis has been applied to evaluate the model accuracy and calibration. The Extended-  
130 FAST (E-FAST) method (Saltelli et al., 2004), a widespread method based on the variance  
131 decomposition theorem, has been applied. In accordance to the method, two sensitivity indices for  
132 each  $i$ -th model factor must be calculated: the first-order effect index ( $S_i$ ) and the total-effect index  
133 ( $S_{Ti}$ ).  $S_i$  assesses the contribution of the  $i$ -th parameter to the variance of the model output [ $\text{Var}(Y)$ ]  
134 without considering the interaction among the model parameters.  $S_{Ti}$  is calculated to evaluate the  
135 contributions from high order interactions (Jing et al., 2018). Thus, the difference between  $S_{Ti}$  and  $S_i$   
136 represents the interaction among the model parameters.

137 The E-FAST method requires  $n \times N_R$  simulations, where  $n$  is the number of parameters and  $N_R$  is the  
138 number of runs per model parameter and varies from 500 to 1000 (Saltelli et al., 2004).

## 139 2.3 Multi-objective optimization method

140 A major challenge in multi-objective optimization is to find the weights of the various components  
141 of the multi-criteria. To define what is “best” is a subjective decision, made by the modeller. For the  
142 model optimization, the TOPSIS method has been adopted (Wang and Rangaiah, 2017). This method  
143 will select as the optimal solution (among  $m$  solutions), the one having the smallest Euclidean distance  
144 from the ideal solution among  $m$  solutions ( $A^+$ , known as positive - ideal solution) and the largest  
145 Euclidean distance from the negative – ideal solution among  $m$  solutions ( $A^-$ ).

146 By selecting the  $A^+$  and  $A^-$  solutions the modeller will define the performance indicators adopted as  
147 objective function (OF) for the system under study. The ideal solution represents the combination of  
148 the best value of OFs. Conversely, the negative - ideal solution represents the combination of the  
149 worst value of OFs.

150 The TOPSIS method is based on the evaluation of a normalized OF ( $f_{ij}$ ) matrix ( $F_{ij}$ ), computed by  
151 dividing each ( $f_{ij}$ ) to the square root of the squared sum of all the  $f_{ij}$ . Then the  $F_{ij}$  is weighed  
152 depending on the influence of each OF ( $f_{ij}$ ).

$$153 \quad F_{ij} = \frac{f_{ij}}{\sqrt{\sum_{i=1}^m f_{ij}^2}} \quad [1]$$

154 where  $m$  represents the number of solutions for each OF and  $n$  the number of the OFs.

155

156 The TOPSIS procedure consists on 5 -steps (Hwang and Yoon, 1981). In the first step, the  
157 normalized objective matrix ( $F_{ij}$ ) ( $m$  rows X  $n$  columns) related to each solution ( $i$ ) of each OF ( $j$ )  
158 ( $f_{ij}$ ) is composed according to Equation 1. The  $m$  solutions represent the non-dominated solutions.

159 In the second step, the normalized objective matrix ( $v_{ij}$ ) is calculated by multiplying each column of  
160 objective matrix ( $F_{ij}$ ) with its weight ( $w_j$ ), in accordance to Equation 2.

161

$$162 \quad v_{ij} = F_{ij} \times w_j \quad [2]$$

163

164 In the third step, the best and the worst values of each OF ( $j$ ) is evaluated.

165 Considering the objectives that require to be maximized, the best value ( $v_j^+$ ) is the largest value within  
166 the related columns of matrix  $v_{ij}$ . Conversely, for the OFs that have to be minimized, the best value  
167 ( $v_j^+$ ) is the smallest value within the related columns of matrix  $v_{ij}$ .

168 The worst objective value that requires maximization ( $v_j^-$ ) is the smallest value within the related  
169 columns of matrix  $v_{ij}$ . For the OFs that have to be minimized, the worst value (i.e.,  $v_j^-$ ) is the largest  
170 value within the related columns of matrix  $v_{ij}$ .

171 In the fourth step, the Euclidean distance between each solution and the ideal and negative -ideal  
172 solution is calculated.

173 The distance to positive ideal solution ( $S_{i+}$ ) is calculated according to Equation 3.

174

$$175 \quad S_{i+} = \sqrt{\sum_{j=1}^n (v_{ij} - v_j^+)^2} \quad i = 1, 2, 3, \dots, m \quad [3]$$

176

177 Similarly ( $S_{i-}$ ) is evaluated by Equation 4:

178

$$179 \quad S_{i-} = \sqrt{\sum_{j=1}^n (v_{ij} - v_j^-)^2} \quad i = 1, 2, 3, \dots, m \quad [4]$$

180

181 In the final step, the closeness of each optimal solution is calculated according to Equation 5.

182

$$183 \quad C_i = \frac{S_{i-}}{S_{i-} + S_{i+}} \quad [5]$$

184

185 The solution having the largest  $C_i$  represents the optimal solution.

186 Further applications of the TOPSIS method can be found in (Wang and Rangaiah, 2017).

## 187 **2.4 Performance Indicators**

188 Ten Performance Indicators (PIs) were considered for the sensitivity and the multi-objective  
189 optimization analysis: Operational Costs (OC); Effluent Fine (EF); Effluent Quality Index (EQI) for

190 both liquid ( $EQ_{LIQ}$ ) and gas ( $EQ_{GAS}$ ) flows; oxygen-to-total-Kjeldahl-nitrogen ratio (RON); ratio  
191 nitrate-ammonia ( $R_{NAT}$ );  $CO_2$  and  $N_2O$  emissions; and direct (DE) and indirect (IE) GHG emissions.

192 The OC (€/treated volume) is calculated by adapting the cost function proposed by Vanrolleghem  
193 and Gillot (2002) to the case of MBR. Specifically, the cost is calculated as the sum of three terms  
194 (Guerrero et al., 2011): costs related to the chemical consumption for membrane cleaning (CC, as €/  
195 treated volume), energy demand ( $eD$ , €/) and effluent fine (EF) related to pollutants discharge (in  
196 accordance with Italian regulations), as expressed in Equation (6):

197

$$198 \quad OC = eD \cdot \gamma_e + CC + EF \quad [6]$$

199

200 where  $\gamma_e$  represents the cost per kWh. Italian rates are 0.21 € / kWh.

201 The energy demand  $eD$  (kWh) is calculated as:

202

$$203 \quad eD = P_w + P_{eff} + P_s \quad [7]$$

204

205 where  $P_w$ ,  $P_{eff}$  and  $P_s$  represent the energy consumption for the air blowers, permeate extraction and  
206 the recycle pumps, respectively.  $P_w$  and  $P_{eff}$  have been calculated according to literature (Mannina &  
207 Cosenza, 2013; 2015):

$$208 \quad P_w = \frac{wRT}{29.7(0.283)e} \left[ \left( \frac{p_2}{p_1} \right)^{0.283} - 1 \right] \quad [8]$$

209 where  $P_w$  [kW] is the power requirement for each blower,  $w$  is the mass flow of air [ $kg \ s^{-1}$ ],  $R$  is the  
210 gas constant for air [ $8.314 \ kJ \ kmol^{-1} \ K^{-1}$ ],  $T$  is the absolute temperature [K],  $p_1$  and  $p_2$  are the absolute

211 inlet and outlet pressures [atm], respectively. The constant 29.7 is a conversion to metric units, 0.283  
 212 is a constant for air,  $e$  is the blower efficiency (common range 0.7–0.9).

213 The power requirement (in kW) for the permeate extraction pump is

$$214 \quad P_{eff} = \frac{1}{t_1 - t_0} \int_{t_0}^{t_1} \frac{TMP \cdot Q_{eff}(t)}{3600 \cdot \eta} dt \quad [9]$$

215 where, TMP [kPa] is the trans-membrane pressure,  $Q_{eff}$  [ $m^3 h^{-1}$ ] is the effluent flow rate,  $t_0$  and  $t_1$  are  
 216 the initial and the final times, respectively, of pump operation, and  $\eta$  is the permeate pump efficiency.

217 The energy consumption for the recycle pumps ( $P_s$ ) has been calculated as (Metcalf & Eddy, 2003):

218

$$219 \quad P_s = \frac{1}{t_1 - t_0} \int 0.04 \cdot (Q_{R1} \cdot 0.06 + Q_{R2} \cdot 0.06 + Q_{WAS} \cdot 0.06) \cdot dt \quad [10]$$

220 Where  $Q_{R1}$  is the recycled flow rate from the anoxic to anaerobic tank,  $Q_{R2}$  the flow rate from the  
 221 aerobic to MBR tank, and  $Q_{WAS}$  the waste sludge flow rate, respectively.

222 The effluent fine EF has been evaluated according to Mannina & Cosenza (2013; 2015). The  
 223 membrane cleaning cost CC has been calculated considering a typical membrane cleaning protocol  
 224 that includes a chemical solution composed of 500 ppm of NaOCl and 2,000 ppm of citric acid, with  
 225 a cost of 0.48€ per chemical cleaning. For the pilot-plant considered in this work, the CC were  
 226 activated only when the transmembrane pressure (TMP) reached a value higher than 60kPa. The  
 227 threshold value of 60kPa is suggested by the membrane manufacturer.

228 The EQI (kg/treated volume) represents the mass of pollutants discharged throughout the evaluation  
 229 period (Mannina & Cosenza, 2015).  $EQI_{LIQ}$  has been calculated according to:

230

$$231 \quad EQI_{LIQ} = \frac{1}{T \cdot 1000} \int_{t_0}^{t_1} (\beta_{COD} \cdot COD_e + \beta_{SNH4} \cdot S_{NH4e} + \beta_{SN03} \cdot S_{NO3e} + \beta_{SN20} \cdot S_{N20e} + \beta_{SPO} \cdot S_{POe}) \cdot$$

$$232 \quad Q_{eff} dt \quad [11]$$

233 where  $\beta_i$  are the weighting factors of the effluent concentrations and are attributed for each single  
 234 soluble component of the effluent ( $i$  = chemical oxygen demand -  $COD_e$ , ammonia -  $S_{NH_4e}$ , nitrate -  
 235  $S_{NO_3e}$ , nitrous oxide -  $S_{N_2Oe}$  and phosphate -  $S_{PO_e}$ ). The following weighting factors were used  
 236 (Mannina & Cosenza, 2013):  $\beta_{COD}=1$ ,  $\beta_{NH}=20$ ,  $\beta_{NO_3}=20$ ,  $\beta_{N_2O}=50$  and  $\beta_{PO}=50$ .  $Q_{eff}$  is the effluent  
 237 flow rate,  $T$  is the simulation period, 1000 is the conversion factor from  $g\ m^{-3}$  to  $kg\ m^{-3}$ ,  $t_0$  and  $t_1$   
 238 represent the initial and the final simulation time, respectively.

239 The calculation of EQI was updated to consider gaseous emissions ( $EQI_{GAS}$ ). Applying the same  
 240 concept of the  $EQI_{LIQ}$ , the  $EQI_{GAS}$  has been calculated as:

$$242 \quad EQI_{GAS} = \frac{1}{T \cdot 1000} \int_{t_0}^{t_1} (\beta_{CO_2} \cdot Offgas_{CO_2} + \beta_{SN_2O} \cdot Offgas_{N_2O}) \cdot Q_{offgas} dt \quad [12]$$

243  
 244 where the terms are similar to Equation 11. However,  $Offgas_{CO_2}$  and  $Offgas_{N_2O}$  describe the gas  
 245 emitted as  $CO_2$  and  $N_2O$ . The  $\beta_i$  values are defined for each GHG ( $\beta_{N_2O}=50$  and  $\beta_{CO_2}=50$ ), and  $Q_{offgas}$   
 246 is the gas flow rate. RON indicates the amount of oxygen supplied by the aeration system (i.e., within  
 247 the aerobic reactor) versus the influent Total Kjeldahl Nitrogen (TKN). The PI allows to quantify the  
 248 rate of oxygen consumed to oxidize the influent TKN. The PI indicates the aeration regime of the  
 249 treatment plant consisting on the amount of air supplied to the aerobic reactor (Vangsgaard et al.,  
 250 2012). RON has been calculated according to (Boiocchi et al., 2017a):

$$252 \quad RON = \frac{\sum_{i=1}^n k_{LAER,i} \cdot V_{AER,i} \cdot (S_{O_2,SAT,AER,i} - S_{O_2,AER,i})}{Q_{in} \cdot S_{NH,in}} \quad [13]$$

253  
 254 where  $k_{LAER,i}$  is the oxygen mass transfer coefficient of the aerated tank  $i$ ;  $V_{AER,i}$  is the volume of the  
 255  $i$ -th aerated tank;  $S_{O_2,SAT}$  is the oxygen saturation concentration;  $S_{O_2,AER,i}$  is the DO concentration

256 inside the  $i$ -th aerated tank;  $Q_{IN}$  is the inlet flow rate fed to the biological zone; and  $TKN_{,in}$  is the inlet  
257 TKN fed to the biological zone.

258  $R_{NAT}$  is the ratio between the nitrate produced and ammonia depleted in an aerobic zone and is an  
259 indicator of the degree of complete nitrification (Boiocchi et al., 2017b):

260

$$261 \quad R_{NAT} = \frac{NO_{3,OUT,AER}^- - NO_{3,IN,AER}^-}{NH_{4,IN,AER}^+ - NO_{4,OUT,AER}^+} \quad [14]$$

262

263 where  $S_{NO_3,IN,AER}$  and  $S_{NO_3,OUT,AER}$  represent the influent and effluent  $NO_3$  concentration of the aerobic  
264 tank, respectively.  $S_{NH_4,IN,AER}$  and  $S_{NH_4,OUT,AER}$  denote the influent and effluent  $NH_4$  concentrations of  
265 the aerobic tank, respectively.  $R_{NAT}$  indicates the amount of ammonia being oxidized by the AOB  
266 and converted into nitrate in the aerobic zone. When all the AOB-produced  $NO_2$  are oxidized by NOB  
267 (i.e., forming  $NO_3$ ) (complete nitrification),  $R_{NAT}$  will be equal to one. However,  $R_{NAT}$  larger than  
268 one is expected as there are additional processes (e.g., biomass decay and additional organic nitrogen  
269 release through ammonification) contributing to enhance the organic nitrogen concentrations within  
270 the aerobic tank.  $R_{NAT}$  indicates if the  $N_2O$  production is due to the low AOB activity (Boiocchi et  
271 al., 2017b).

272 The emissions of  $CO_2$  ( $kgCO_2 \cdot m^{-3}$ ) and  $N_2O$  ( $kgN_2O \cdot m^{-3}$ ) are evaluated by considering their stripping  
273 from the liquid phase to the gas phase according to (Mannina et al., 2018). The total direct emissions  
274 (DE,  $kgCO_{2,eq} m^{-3}$ ) are calculated as the sum of the  $N_2O$  and  $CO_2$  emissions. Since  $N_2O$  has a GWP  
275 265 times higher than that of  $CO_2$ ,  $N_2O$  emission is multiplied by 265.

276 Indirect emissions (IE,  $kgCO_{2,eq} m^{-3}$ ) are calculated multiplying eD by  $\gamma_{CO_2}$  (equal to  $0.245 kgCO_{2,eq}$   
277 /kWh) representing the specific  $CO_2$  emission due to the energy consumption (EIA, 2009).

278

## 279 **2.5 Operational parameter values**

280 The E-FAST method (Saltelli et al., 2004) has been applied to assess the influence of the following  
281 operational parameters on the PI, with respect to the benchmark scenario: sludge retention time -  
282 SRT, air flow rate in the aerobic reactor -  $Q_{\text{air,AER}}$ , air flow rate in the MBR -  $Q_{\text{air,MBR}}$ , the recycle ratio  
283 from the anoxic to the anaerobic reactor -  $R_{\text{QR1}}$ , and the recycle ratio from the aerobic to the anoxic  
284 reactor -  $R_{\text{QR2}}$ .

285 Table 1 summarizes the value of each operational parameter, its investigated variation range and the  
286 references.  $Q_{\text{air,MBR}}$  was changed according to the manufacturer's suggestion. The minimum value of  
287  $Q_{\text{air,AER}}$  should allow a dissolved oxygen concentration to exceed  $0.5 \text{ mg L}^{-1}$  (Metcalf, & Eddy  
288 (2003)). The maximum value of  $Q_{\text{air,AER}}$  has been twice the benchmark scenario one.

289 **<Here Table 1>**

290 The E-FAST method was applied with  $N_R (=5)$  simulations per parameter value, and consequently  
291 5,000 model simulations were executed. The purpose was to evaluate the outputs of the modelling  
292 application and sensitivity analysis over ten performance indicators, related to the operational costs,  
293 energy demand, oxygen consumption, nitrification efficiency, effluent and gas quality and GHG  
294 emissions.

295 The TOPSIS method has been applied considering the ten aforementioned performance indicators as  
296 the objective function (OF) to be optimized. All the performance indicators, except  $R_{\text{NAT}}$  (that was  
297 maximized), have been minimized during the TOPSIS method application. The same weight ( $w_j$ )  
298 (equal to 0.1) has been adopted for all the OFs.

299

## 300 **3. Results and Discussion**

### 301 **3.1 Sensitivity Analysis**

302 The values of the first-order effect index ( $S_i$ ) and the total-effect index ( $S_{Ti}$ ) and the difference  
303 between them are summarized in Table 2.

304 **<Here Table 2>**

305

306 The sum of each  $S_i$  for all ten performance indicators ranged between 0.91 and 0.99. Since the sum  
307 of  $S_i$  is close to 1, it is reasonable to conclude that the investigated parameters are non-correlated and  
308 performance indicators are not additive (Saltelli et al., 2004). Therefore, a few interactions among the  
309 investigated parameters are expected. This statement is also confirmed by the sum of  $S_{Ti}$ , which is  
310 always close to 1.0. This latter result suggests that there is a very low interaction between the  
311 parameters.

312 Figure 1 presents the Extended-FAST results for each performance indicator. The results related to  
313  $Q_{air,MBR}$  are not reported in the figure, as it was shown that this parameter has a negligible influence  
314 on the PIs (i.e.,  $S_i$ ,  $S_{Ti}$  and  $S_{Ti}-S_i$  are  $<10^{-2}$ ). Further details regarding  $Q_{air,MBR}$  are reported in the  
315 following sections.

316 **<Here Figure 1>**

317

318 Figure 1 demonstrates that SRT has the highest influence on the PIs, with  $S_i$  close to 1.0 for  $Offgas_{N_2O}$ ,  
319  $Offgas_{CO_2}$ , DE,  $EQI_{GAS}$ ,  $EQI_{LIQ}$  e EF (Figure 1a). SRT influences the results of  $R_{NAT}$  and RON, but  
320 with a minor intensity with respect to the other indicators (for  $R_{NAT}$ ,  $S_i = 0.60$  and  $S_{Ti} = 0.68$ ; for  
321 RON,  $S_i = 0.73$  and  $S_{Ti} = 0.75$ ).  $Offgas_{N_2O}$  increases with SRT (up to  $0.66 \cdot 10^{-2} \text{ kgCO}_{2,eq} \text{ m}^{-3}$ ) due to  
322 the increase of the autotrophic bacteria activities. At high SRTs biomass endogenous decay rate  
323 dominates since most carbon has been oxidized. This will limit the denitrification rate, thus  
324 contributing to  $N_2O$  emissions (Boiocchi et al., 2017b).  $Offgas_{CO_2}$  increases with an increase of SRT.

325 This increase is most evident for SRT values ranging between 10 and 25 days (OffgasCO<sub>2</sub> increases  
326 from 0.35 to 0.50 10<sup>-2</sup> kgCO<sub>2</sub> m<sup>-3</sup>) due to the increase of the biomass activity. Further increase of the  
327 SRT leads to the inert biomass accumulation inside the system (Judd, 2010). Therefore, for SRT  
328 values higher than 25 days, the OffgasCO<sub>2</sub> is quite stable and equal to 0.55 10<sup>-2</sup> kgCO<sub>2</sub> m<sup>-3</sup>. The DE  
329 and EQI<sub>GAS</sub> follow the same trend of the individual GHG emissions previously presented, being more  
330 influenced by the N<sub>2</sub>O emissions due to its higher GWP. The difference between both PIs in this case  
331 is that DE represents the amount of GHG emitted, while EQI<sub>GAS</sub> represents the potential of the WWTP  
332 to emit GHG. SRT also influences the results of EF and EQI<sub>LIQ</sub>, due to the higher capability of the  
333 system to support nitrification. The Q<sub>air,AER</sub> variation strongly influences IE and OC (Figure 1b).  
334 Specifically, the variation of Q<sub>air,AER</sub> influences the energy consumption, which is the main  
335 contributor for both IE and OC.

336 R<sub>QR1</sub> (Figure 1c) exerts a smaller influence over the PIs when compared to SRT and Q<sub>air,AER</sub>. A similar  
337 result was obtained for R<sub>QR2</sub> (Figure 2d), which slightly influences RON, EF and EQI<sub>LIQ</sub>. Figure 2  
338 shows the variation of RON and R<sub>NAT</sub> with SRT, R<sub>QR1</sub> and R<sub>QR2</sub>.

339 **<Here Figure 2>**

340

341 RON increases (from 4.04 to 5.90 gO<sub>2</sub> gNH<sub>4</sub><sup>-1</sup>) with the increase of SRT and R<sub>QR2</sub> (Figure 2a, Figure  
342 2b). The increase of the SRT leads to the increase of nitrification with the consequent rise of the  
343 amount of oxygen consumed and RON. The increase of R<sub>QR2</sub> reduces the oxygen concentration within  
344 the aerobic reactor, thus causing an increase of RON.

345 The R<sub>NAT</sub> will increase together with the SRT (Figure 2c). The reason is that it allows an increase of  
346 the nitrification rate, i.e. a higher amount of nitrate has been produced. The increase of R<sub>QR1</sub> leads to  
347 the decrease of R<sub>NAT</sub> (Figure 2d) since the inlet nitrate load to the aerobic reactor decreases. It is

348 caused by the increase of the combined oxygen concentration recycled from the anoxic to the  
349 anaerobic reactor. Therefore, most of the PAOs activity in the anaerobic reactor (turned anoxic) is as  
350 denitrifiers. Consequently, the nitrate concentration in the following reactors will be reduced.

351 To understand the role of SRT on GHG emissions, the spatial distribution of  $\text{Offgas}_{\text{N}_2\text{O}}$  within each  
352 reactor of the investigated MBR plant is shown in Figure 3. Data of Figure 2 consider three values of  
353 SRT (10, 25 and 50 days). Furthermore,  $Q_{\text{air,AER}} = 35 \text{ m}^3 \cdot \text{d}^{-1}$ ,  $Q_{\text{air,MBR}} = 15 \text{ m}^3 \cdot \text{d}^{-1}$ ,  $R_{\text{QR1}} = 0.8$ , and  
354  $R_{\text{QR2}} = 6.2$ .

355 **<Here Figure 3>**

356 From Figure 3 it is noted that the  $\text{N}_2\text{O}$  emissions from the anaerobic (Figure 3a) and anoxic (Figure  
357 3b) reactors are lower than that of the other reactors. These emissions are related to the heterotrophic  
358 activities (PAO and heterotrophic non-PAO) while incomplete denitrification takes place.

359 The AOB and NOB are the major contributors to  $\text{N}_2\text{O}$  emissions (Boiocchi et al., 2017a), which can  
360 be observed by the increase of the  $\text{Offgas}_{\text{N}_2\text{O}}$  from the aerobic reactor (Figure 3c). The aerated reactors  
361 are the major contributors of  $\text{Offgas}_{\text{N}_2\text{O}}$  within the MBR plant (Ribera-Guardia et al., 2019), followed  
362 by the MBR reactor (Figure 3d). The emissions from the MBR reactor are mostly due to the stripping  
363 of  $\text{N}_2\text{O}$  in gas form from its related dissolved component (Massara et al., 2018).

364 The emissions for SRT equal to 10 days were negligible, mainly due to the lower AOB and NOB  
365 activities at low SRT values. The  $\text{N}_2\text{O}$  emissions are related to both the nitrification and denitrification  
366 processes, which are less pronounced (especially the nitrification) at low SRT values. For SRT values  
367 higher than 10 days allows a more complete nitrification, enhancing the probability of  $\text{N}_2\text{O}$  formation  
368 by the AOB. As mentioned before, the high SRT also favours the processes related to the  
369 heterotrophic microorganisms (e.g., phosphorus removal and denitrification), which also contributes  
370 to the  $\text{N}_2\text{O}$  formation pathways.

371 The influence of SRT on the growth of AOB and the NO<sub>2</sub> production within the aerobic reactor  
372 reported in Figure 4.

373 Figure 4a shows that AOB concentrations will decrease due to the low AOB growth rate at low SRT.  
374 For higher SRT values the Figure 4b, 4c), the AOB growth increases so that the AOB concentrations  
375 will increase. This will cause the NO<sub>2</sub> concentration to accumulate in the aerobic reactor. Similar  
376 results were obtained by Massara et al. (2017).

377 **<Here Figure 4>**

378

379 Figure 3 and Figure 4 suggest that a low concentration of AOB biomass leads to a low dissolved  
380 concentration of NH<sub>2</sub>OH or NO and, consequently, the N<sub>2</sub>O emission is negligible. This also means  
381 that the growth of NOB, heterotrophic non-PAOs and PAOs is compromised, negatively affecting  
382 nutrient removal. This emphasizes that the SRT is the model parameter having the largest influence  
383 on the most performance indicators.

384

### 385 **3.2 Multi-objective optimization and performance assessment**

386 In Table 3 the results of the five investigated operational parameters for the optimal and benchmark  
387 solution are displayed. The optimal solution shows an increase of the SRT value (from 35 to 49 days),  
388 a decrease of R<sub>QR1</sub> (from 1 to 0.54), an increase of R<sub>QR2</sub> (from 5 to 6.4), a substantial decrease of  
389 Q<sub>air,AER</sub> (from 22 to 11 m<sup>3</sup> d<sup>-1</sup>), a slight decrease of Q<sub>air,MBR</sub> (from 14.4 to 14.2 m<sup>3</sup> d<sup>-1</sup>).

390 **<Here Table 3>**

391

392 Table 4 summarizes the results for each OF related to the benchmark and the optimal solution. The  
393 TOPSIS application allowed to optimize seven of the ten OFs (in grey in Table 4). The substantial  
394 reduction of the  $Q_{\text{air,AER}}$  value contributed to reducing the optimal OC to almost half compared to the  
395 benchmark solution (from 1.05 to 0.59 € m<sup>-3</sup>), due to the reduced energy consumption. Since the IE  
396 are mainly related to energy consumption, a substantial reduction of IE occurred as well (from 1.12  
397 to 0.57 kgCO<sub>2,eq</sub> m<sup>-3</sup>). Energy savings of this magnitude, 48% of the OCs due to the aeration and IE,  
398 is naturally of major interest. Note that the dissolved oxygen concentration in the aerobic reactor is  
399 not limiting the nitrification process (always >1.5 mgO<sub>2</sub> L<sup>-1</sup>), despite the low  $Q_{\text{air,AER}}$  value.

400

<Here Table 4>

401 The optimal solution achieved a 10% reduction of DE (Table 4), mainly caused by the reduction of  
402 Offgas<sub>N2O</sub> compared to the benchmark (from 0.57 to 0.50 kgCO<sub>2,eq</sub> m<sup>-3</sup>). This result seems to  
403 contradict the trend shown in Figure 3 where the Offgas<sub>N2O</sub> concentration increases with the increase  
404 of SRT. However, the results in Figure 3 have been obtained for a higher  $Q_{\text{air,AER}}$  value (around 30  
405 m<sup>3</sup> d<sup>-1</sup>) than that of the optimal solution. Consequently, since the Offgas<sub>N2O</sub> concentration depends on  
406  $Q_{\text{air,AER}}$  value (lower  $Q_{\text{air,AER}}$  reduce the stripping effect) the results of the optimal solution have been  
407 influenced by the lower  $Q_{\text{air,AER}}$  value.

408 Table 4 illustrates that a slight increase of EF (from 0.09 to 0.1 € m<sup>-3</sup>) and EQ<sub>LIQ</sub> (from 14.7 to 15.6  
409 kg m<sup>-3</sup>) occurred for the optimal solution. The increase of EQ<sub>LIQ</sub> is caused by a slight increase (around  
410 10%) of effluent ammonia concentration; conversely, a substantial decrease in terms of S<sub>PO</sub>  
411 concentration in the effluent occurred for the optimal solution (from 1.5 mg L<sup>-1</sup> to 0.4 mg L<sup>-1</sup>). The  
412 reason is the increased hydraulic retention time (HRT) inside the anaerobic reactor, due to the

413 decreased  $R_{QR1}$  (from 1 to 0.54). A lower HRT of the anaerobic reactor allowed a major anaerobic  
414 phosphate release and a subsequently uptake from PAOs in the aerobic and anoxic conditions.

415 A value of  $R_{NAT}$  less than  $1.0 \text{ gNO}_3 \text{ gNH}_4^{-1}$  represents a good balance between AOB and NOB. This  
416 value was obtained for the optimal solution, confirming the low nitrification efficiency for the system  
417 under study (Boiocchi et al., 2017b), which has also influenced the  $\text{N}_2\text{O}$  formation during the  
418 nitrification/denitrification processes.

419 RON increased from 3.50 to  $5.79 \text{ gO}_2 \text{ gNH}_4^{-1}$  mainly due to reduction of the oxidized ammonia in  
420 the optimal solution (Table 4). The higher RON ( $5.79 \text{ gO}_2 \text{ gNH}_4^{-1}$ ) of the optimal solution is in  
421 agreement with the related lower  $\text{Offgas}_{\text{N}_2\text{O}}$  concentration. Indeed, according to Boiocchi et al.  
422 (2017a), for high value of RON ( $>5.0 \text{ gO}_2 \text{ gNH}_4^{-1}$ ), the NOB activity increases as well; the AOB and  
423 the heterotrophic biomass denitrification producing  $\text{N}_2\text{O}$  decreases due to the low  $\text{NO}_2$  availability,  
424 consequently  $\text{N}_2\text{O}$  decreases. The decrease of  $\text{Offgas}_{\text{N}_2\text{O}}$  also caused up to 8% reduction in  $\text{EQI}_{\text{GAS}}$   
425 compared to the benchmark solution (from 60.1 to  $55.60 \text{ kg m}^{-3}$  Figure 5 displays the average gaseous  
426  $\text{Offgas}_{\text{N}_2\text{O}}$  concentration per reactor and the average total DE.

Figure 5 shows that the major Offgas<sub>N2O</sub> concentration occurred in the MBR in both solutions. This is due to the higher aeration rate of the MBR compared to aerobic reactors. The result is in agreement with Mannina et al (2017) finding the highest N<sub>2</sub>O flux from the MBR reactor. The second major emitter is the aerobic reactor, emphasizing the role of the aeration in the Offgas<sub>N2O</sub> concentration. Only negligible Offgas<sub>N2O</sub> and DE emission were found from the anaerobic and anoxic reactors, since the greater part of N<sub>2</sub>O has been produced during the nitrification (Figure 5).

Figure 5a demonstrates the average Offgas<sub>N2O</sub> concentration and DE for all the plant reactors is smaller for the optimal solution than for the benchmark solution. The Offgas<sub>N2O</sub> concentration emitted from the MBR reduced from 0.45 to 0.38 10<sup>-2</sup> kgCO<sub>2eq</sub> m<sup>-3</sup>, and from the aerobic reactor from 0.075 to 0.06 10<sup>-2</sup> kgCO<sub>2eq</sub> m<sup>-3</sup>. Similar results were obtained for the DE, since it is mainly related to Offgas<sub>N2O</sub>. DE for to the MBR decreased from 0.48 to 0.4 10<sup>-2</sup> kgCO<sub>2eq</sub> m<sup>-3</sup>, and for the aerobic reactor from 0.095 to 0.86 10<sup>-2</sup> kgCO<sub>2eq</sub> m<sup>-3</sup> (Figure 5b).

427

<Here Figure 5>

428 Figure 6 illustrates results obtained from the TOPSIS application for some OF. The trend of the non-  
429 dominated solutions, representing all the solutions obtained for the 5,000 simulations, has been  
430 reported for R<sub>NAT</sub> vs Offgas<sub>N2O</sub>, Offgas<sub>N2O</sub> vs Offgas<sub>CO2</sub>, and DE vs R<sub>NAT</sub>. Optimal and benchmark  
431 solutions, (Table 3) are also indicated in Figure 6.

432 Data of Figure 6a show that few solutions enable the increase of R<sub>NAT</sub> (which should be maximized)  
433 at low total Offgas<sub>N2O</sub>. This result is mainly related to the R<sub>NAT</sub> value that is lower than 0.25 gNO<sub>3</sub>  
434 gNH<sub>4</sub><sup>-1</sup>; this value corresponds to an Offgas<sub>N2O</sub> concentration lower than 0.37 10<sup>-2</sup> kgCO<sub>2eq</sub> m<sup>-3</sup> that  
435 is typical of the AOB inhibition condition (Baiocchi et al., 2017a-b). The corresponding Offgas<sub>N2O</sub>  
436 concentration value is low due to the negligible nitrification and consequently to the denitrification.  
437 Since there is a direct relationship between N<sub>2</sub>O emission and DE, the increase of R<sub>NAT</sub> leads to the  
438 increase of DE (Figure 6c). However, since no R<sub>NAT</sub> value close to 1.0 gNO<sub>3</sub> gNH<sub>4</sub> has been obtained,

439 it can be confirmed that insufficient nitrification occurred inside the system for the all solutions.  
440 Further investigations with the use of a wider range for the assessed operational conditions may obtain  
441 better nitrification results and, consequently, lower  $\text{Offgas}_{\text{N}_2\text{O}}$  and DE at the highest  $R_{\text{NAT}}$ .

442 **<Here figure 6>**

#### 443 **4. Conclusions**

444 The sludge retention time is the key operational parameter affecting mainly the direct emissions; the  
445 results show that direct emissions increase with sludge retention time mainly due to the nitrous oxide  
446 concentration in the off-gas increases (up to  $0.66 \cdot 10^{-2} \text{ kgCO}_{2,\text{eq}} \text{ m}^{-3}$ ). Further, increasing sludge  
447 retention time (from 10 to 50 days) enhances the nitrification thanks to a higher concentration of  
448 autotrophic microorganisms. The multi-objective optimization approach is practical and feasible to  
449 be adopted both by modelers and by operators even for complex integrated membrane bioreactor  
450 models.

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