

1 **PMT: new analytical framework for automated evaluation of**
2 **geo-environmental modelling approaches**

3 Omid Rahmati ^{1,2*}, Aiding Kornejady ³, Mahmood Samadi ⁴, Ravinesh C. Deo ⁵, Christian
4 Conoscenti ⁶, Luigi Lombardo ⁷, Kavina Dayal ⁸, Ruhollah Taghizadeh-Mehrjardi ^{9,10}, Hamid
5 Reza Pourghasemi ¹¹, Sandeep Kumar ¹², Dieu Tien Bui ^{13,14*}

6 ¹ Geographic Information Science Research Group, Ton Duc Thang University, Ho Chi Minh City,
7 Vietnam

8 ² Faculty of Environment and Labour Safety, Ton Duc Thang University, Ho Chi Minh City, Vietnam

9 ³ Young Researchers and Elite Club, Gorgan Branch, Islamic Azad University, Gorgan, Iran

10 ⁴ Faculty of Natural Resources, University of Tehran, Karaj, Iran

11 ⁵ School of Agricultural, Computational and Environmental Sciences, Centre for Sustainable Agricultural
12 Systems & Centre for Applied Climate Sciences, University of Southern Queensland, Springfield, QLD
13 4300, Australia

14 ⁶ Department of Earth and Marine Sciences (DISTEM), University of Palermo, Via Archirafi 22, 90123
15 Palermo, Italy

16 ⁷ Faculty of Geo-Information Science and Earth Observation (ITC), University of Twente, Enschede,
17 Netherlands

18 ⁸ CSIRO Agriculture and Food, 15 College Road, Sandy Bay, TAS 7005, Australia

19 ⁹ Department of Geosciences, Soil Science and Geomorphology, University of Tübingen, Tübingen,
20 Germany

21 ¹⁰ Faculty of Agriculture and Natural Resources, Ardakan University, Ardakan, Iran

22 ¹¹ Department of Natural Resources and Environmental Engineering, College of Agriculture, Shiraz
23 University, Shiraz, Iran

24 ¹² Department of Agronomy, Horticulture and Plant Science, South Dakota State University, Brookings,
25 USA

26 ¹³ Institute of Research and Development, Duy Tan University, Da Nang 550000, Vietnam

27 ¹⁴ Geographic Information System Group, Department of Business and IT, University of South-Eastern
28 Norway, N-3800 Bø i Telemark, Norway

29 * Corresponding authors' Email addresses: Orahmati68@gmail.com; Dieu.T.Bui@usn.no

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33 **geo-environmental modelling approaches**

34 **Abstract**

35 Geospatial computation, data transformation to a relevant statistical software, and step-wise
36 quantitative performance assessment can be cumbersome, especially when considering that the
37 entire modelling procedure is repeatedly interrupted by several input/output steps, and the self-
38 consistency and self-adaptive response to the modelled data and the features therein are lost
39 while handling the data from different kinds of working environments. To date, an automated
40 and a comprehensive validation system, which includes both the cutoff-dependent and –
41 independent evaluation criteria for spatial modelling approaches, has not yet been developed for
42 GIS based methodologies. This study, for the first time, aims to fill this gap by designing and
43 evaluating a user-friendly model validation approach, denoted as Performance Measure Tool
44 (PMT), and developed using freely available Python programming platform. The considered
45 cutoff-dependent criteria include receiver operating characteristic (ROC) curve, success-rate
46 curve (SRC) and prediction-rate curve (PRC), whereas cutoff-independent consist of twenty-one
47 performance metrics such as efficiency, misclassification rate, false omission rate, F-score, threat
48 score, odds ratio, etc. To test the robustness of the developed tool, we applied it to a wide variety
49 of geo-environmental modelling approaches, especially in different countries, data, and spatial
50 contexts around the world including, the USA (soil digital modelling), Australia (drought risk
51 evaluation), Vietnam (landslide studies), Iran (flood studies), and Italy (gully erosion studies).
52 The newly proposed PMT is demonstrated to be capable of analyzing a wide range of

53 environmental modelling results, and provides inclusive performance evaluation metrics in a
54 relatively short time and user-convenient framework whilst each of the metrics is used to address
55 a particular aspect of the predictive model. Drawing on the inferences, a scenario-based protocol
56 for model performance evaluation is suggested.

57 **Keywords:** PMT, Spatial modelling, Goodness-of-fit, Validation, Performance analysis;
58 predictive model evaluation framework

59

60 **Software and data availability**

61 Name of tool:	PMT (Performance Measure Tool)
62 Developers:	Samadi M., Kornejady A., and Rahmati O.
63 Hardware required:	General-purpose computer (2 Gb RAM)
64 Software required:	ArcGIS 10.2
65 Programming languages:	Python [©] 2.7
66 Program size:	120 KB
67 Availability and cost:	Freely available in GitHub
68 Web link:	https://github.com/mahmoodsamadi/PMT
69 Year first available:	2018

70

71 **1. Introduction**

72 Spatially-applicable predictive models must include a mandatory step where different aspects
73 of the model performance can be quantitatively benchmarked. Without considering the
74 performance of such geo-environmental models, the users would not be confident about the
75 veracity of the modelling results, and is unlikely to utilize them for practical decision making

76 (Pullar and Springer, 2000; Glade, 2005; Beguería, 2006). The accuracy of predictive models,
77 which is a pertinent factor demonstrating the usefulness of the relevant models, can significantly
78 result in the misclassification costs of the approach depending on the error magnitudes and types
79 (Fratini et al., 2010). For example, in the modelling of natural hazards, the Error Type I (*i.e.*, false
80 positive) is likely to indicate that a stable part of a spatial region is classified as being unstable,
81 and therefore, it can lead to unnecessary control and risk mitigation measures that are
82 implemented. The Error Type II (*i.e.*, false negative) can imply that a given terrain unit is
83 susceptible to the hazard, and it can be incorrectly classified as being stable, and consequently,
84 this terrain region can be allowed to be occupied by people or infrastructure without a responsible
85 and actionable risk mitigation activity. These errors, if not assessed properly, can consequently
86 incur social and economic costs, depending on the vulnerability and economic value of the
87 elements at risk (*e.g.*, infrastructures, lives, etc.). In light of this need, a robust investigation of
88 such predictive errors in spatially-applicable models is highly warranted, to make the modelling
89 approaches and model results more viable for real-life usage, risk mitigation and implementation.

90 Over the past couple of decades, a number of susceptibility assessment models have been built,
91 each striving to portray the current and future spatial patterns of a specific phenomenon. Many
92 studies have included a “model comparison” or a “performance assessment” step that was aimed
93 to evaluate the spatial modelling result, and to select the most optimal spatially-relevant model.
94 These sorts of models, largely promulgated as an operational tool, have largely been reported in
95 different fields and applications, such as landslide susceptibility studies (*e.g.*, Kornejady et al.,
96 2017; Kavzoglu et al., 2019; Yan et al., 2019), flood susceptibility studies (*e.g.*, Rahmati and
97 Pourghasemi, 2017; Siahkamari et al., 2018; Choubin et al., 2019), forest fire modelling purposes
98 (*e.g.*, Arpaci et al., 2014; Tien Bui et al., 2017), groundwater potential modelling studies (*e.g.*,

99 Naghibi et al., 2017; Miraki et al., 2019), species distribution modelling tasks (*e.g.*, Bucklin et al.,
100 2015; Shabani et al., 2016; Quillfeldt et al., 2017), land subsidence modelling (*e.g.*, Abdollahi et
101 al., 2018; Ghorbanzadeh et al., 2018), soil digital mapping (*e.g.*, Minasny and McBratney, 2007;
102 Wiesmeier et al., 2011; Malone et al., 2017), gully-erosion susceptibility (*e.g.*, Akgün and Türk,
103 2011; Conoscenti et al., 2014; Garosi et al., 2018). The evaluation of predictive models with
104 different statistical metrics and their implemented approaches, especially in such a diverse range
105 of studies, clearly warrant automated and coherent scientific strategies where performance
106 evaluations are implemented by means of a universally acceptable and statistically robust tool.

107 A review of published literature in this respect reveals significant advancements in predictive
108 model performance evaluations where the context of application and the respective model type
109 were seen to play a pivotal role in how these evaluation tools were implemented. Recently, the
110 study of Rahmati and Pourghasemi (2018) compared the performance of ten different advanced
111 machine learning models for the modelling of landslide susceptibility, while the study of Fukuda
112 et al. (2013) applied and compared seven different data-driven models for developing species
113 distribution maps. These authors considered the receiver operating characteristic (ROC) curves
114 and a number of cutoff-dependent methods for judging the capability of their model, and
115 consequently, in preparing and transporting the results to their statistical software, although this
116 was a relatively time-consuming task. Particularly, one must note that when susceptibility maps
117 are supposed to be directly incorporated into land-use planning, the best performing model are
118 likely to be highly favored for practical decision-making tasks (Youssef et al., 2016; Siahkamari et
119 al., 2018). This is primarily because the model performance assessments provide immensely
120 useful insights into the optimal structure of such models, and the possibility of their practical
121 implementation for perceived risk mitigation (Van Westen, 2006).

122 Most performance evaluation metrics that are designed to evaluate the overall learning skill of
123 the predictive model, and the validity of the generated results from them are based on comparing
124 the predicted patterns in spatial models with the actual observation datasets (Chung and Fabbri,
125 2008). In a somewhat different approach to the traditional model evaluation approaches (*e.g.*,
126 graphical check of the model's susceptibility maps in respect to the ground-truth datasets), the new
127 generation of model performance metrics is mainly applicable for quantifying the traditional terms
128 and the models' functionality. According to a general consensus, the performance indices in a
129 predictive model can be classified into two different categories: cutoff-dependent metrics (*e.g.*,
130 Cohen's Kappa, sensitivity, and specificity) and the -independent metrics (*e.g.* receiver operating
131 characteristic, ROC method) (Frattini et al., 2010). These approaches have been used in a number
132 of spatial modelling sub-fields.

133 Meanwhile, there is little doubt that the ArcGIS software, by virtue of its wide flexibility,
134 portability and the relevance in spatial modelling approaches (*e.g.* geostatistics, mapping tools,
135 variogram, kriging, and local/global scale metrics), has been unceasingly used by many
136 researchers to implement the most basic as well as the more complex spatial functions and
137 statistical criterion that are available. In spite of this widespread usage of ArcGIS software as a
138 spatial modeling platform , the absence of a dedicated GIS-based tool and its non-availability to
139 aspiring researchers and practitioners who are outside of the major subscribed users and
140 institutions, is still very challenging (Scott and Janikas, 2010). Furthermore, the GIS users need to
141 employ cumbersome step-by-step procedures in order to calculate each of their performance
142 indices, and occasionally, they need to reach out for additional commercial and/or freely available
143 software platforms (*e.g.*, Microsoft Excel, SPSS, and R packages). These types of external model
144 evaluation frameworks and largely the expensive software that need to be used to analyze these

145 data outside of GIS platforms, represent a challenging task when aiming at optimizing any
146 modeling workflow.

147 In respect to these arguments for more robust evaluation of spatially-relevant predictive
148 models, some of the freely available software, such as the R package in the form of “cvTools”
149 (Alfons, 2012) or “CrossValidate” (Coombes, 2018), and the relevant modelling platforms in the
150 R software have partially satisfied the need to compute these metrics. However, these add-in tools
151 also seem to be relatively deficient in terms of their inclusiveness in the respective modelling
152 approach, and also sometimes, they may require additional external coding skills, which in some
153 cases may not be available to the users. Furthermore, each of these add-in software are likely to
154 include only some of the cutoff-dependent and/or –independent evaluation criteria, and not include
155 the others (as necessary) within a universally desirable manner, and therefore, the external
156 software may be less flexible and attractive to the novice modeler and other non-scientific
157 stakeholders, practitioner and decision-makers.

158 To address inherent limitations posed by existing approaches adopted in the evaluation of
159 spatial models, this research study aims to propose and construct a new, robust and comprehensive
160 GIS-based package, denoted as the Performance Measure Tool (PMT), to scrutinize in a
161 statistically sound manner the performance of spatially-relevant predictive models. The merits of
162 the proposed PMT, augmented by its extensive validation in diverse regions, contextual
163 applications and global studies, are likely to enable modelers and risk mitigation practitioners to
164 calculate practically useful performance metrics (both cutoff-dependent and the –independent
165 category). The PMT is designed in such way that it has the ability to provide information in a
166 tabular and graphical format with a relatively simple platform and self-explanatory user interface.
167 This proposed tool is likely to be useful for any spatially-relevant model, various types of end-

168 users—from the beginner who are not familiar with advanced coding, to those who are
169 comfortable with a ‘click-based procedure’ and also practitioners in any scientific sub-field who
170 need to implement decisions about the model’s versatility. To further ensure credibility and
171 generalizability of the software, the proposed PMT has been benchmarked rigorously to evaluate
172 its relative performance in different geo-environmental modelling contexts and in different parts
173 of the world including studies in Australia, Asia, Europe, and America.

174 **2. Basic Design Framework of the Performance Measure Tool**

175 Implementing the notion that performance evaluation of a spatially-relevant predictive model
176 must be an important cornerstone of any spatial modelling attempt, in this study different cutoff-
177 dependent and –independent evaluation criteria, elaborated later in greater detail, have been
178 proposed. A brief review of recent literature shows that most of these analyses are underpinned by
179 a matrix-wise calculation, termed as the confusion matrix (and also, sometimes known as the table
180 of confusion, error matrix, or the matching matrix) and the contingency table (also known as the
181 cross tabulation or crosstab). Some researchers have interchangeably used these two names in
182 their studies and considered the confusion matrix largely as a special derivative of the contingency
183 matrix. Other researchers, however, pointed out a delicate, and logical difference, in that the
184 former is more suitable for evaluating the performance of different classifiers (*i.e.*, more common
185 in data mining models), while the latter is used to evaluate the rules of association and
186 interrelations between any two variables (Powers, 2011). However, the name “matching matrix” is
187 well-adapted in unsupervised machine learning algorithms, whereas the confusion matrix is used
188 in supervised learning (*i.e.*, input data fed by the training instances).

189 In this research, the confusion matrix has been considered as a way to describe the primary
190 basis for constructing the proposed spatially-relevant model evaluation tool. Consequently, a 2×2
191 confusion matrix is created where the rows are the instances in an actual class (*i.e.*, the
192 observations) and the columns are the instances in the predicted class, as illustrated in Table 1. As
193 the name “confusion” implies, the matrix is able to examine the degree of mislabeling one state (as
194 another) by means of directly comparing the predictions and the observations. The statistics
195 derived from the matrix are therefore all presented as either the row-wise (*e.g.*, positive and
196 negative predictive values) or the column-wise (*e.g.*, sensitivity and specificity) in the
197 implemented PMT tool.

198 **Table 1** HERE

199 It should be emphasized that the process and various stages of model performance assessments
200 can be rather a time-consuming and a complex task for the performance measures in a traditional
201 approach must be calculated separately using the geo-statistical techniques. This is particularly the
202 case for novice end-users (*e.g.*, risk mitigation practitioners who may be unfamiliar with various
203 mathematical and statistical knowledge). More importantly, to the best of the authors’ knowledge,
204 there is hardly any reliable, comprehensive and end-user-friendly tool currently available that can
205 be used to consider the most relevant performance metrics, particularly in the widely adopted
206 ArcGIS environment. Considering this deficit, this paper aims to develop an efficient and
207 automated approach that operates in a quick, reliable and organized manner, and also presents a
208 relatively effective framework providing a user-friendly interface. The PMT has deliberately been
209 written in the freeware, the Python programming environment using a portability feature that
210 enables it to be installed easily within a geo-processing framework found in the ArcToolbox of the
211 ArcGIS 10.2 software.

212 Figure S1 (refer to supplementary information) illustrates the graphical user interface and the
213 execution process of the proposed PMT.

214 **Fig. S1** HERE

215 To illustrate the operational mechanism of the proposed PMT, one part of the Python code used
216 for calculating the evaluation criteria is displayed in Figure S2. The required inputs used to
217 execute the tool and the relevant outputs files are given in Tables 2 and 3, respectively. It is
218 important to note that the PMT extension allows the end-users to evaluate the accuracy of the
219 predictive model in both steps, composed of training/calibration and the validation phase. End-
220 users can also adopt both parts of the training and validation process to check the accuracy of their
221 predictive models, although investigating the accuracy of the model in the training step can also be
222 left unchecked in this particular tool. This option is added because most of the interest is usually
223 focused on the validation component, as it guarantees the viability of the model to be used for the
224 prediction and decision-making process. Conversely, calibration is a component uniquely voted to
225 build the reference model, and to evaluate the covariate effects, although these can be subjected to
226 some degree of overfitting (Lombardo et al., 2018). These stages make the model easy-to-use
227 with no special skills required to run the proposed tool.

228 **Fig. S2** HERE

229 **Table 2** HERE

230 **Table 3** HERE

231 **3. Statistical background of the performance metrics**

232 **3.1. Confusion matrix**

233 In what follows next, the authors outline the kinds of information these metrics are able to
234 convey regarding the model performance. In order to construct a confusion matrix from a spatial
235 model, the users should define a cutoff (in percentile units) to split the spatial map into two
236 distinct classes in which the PMT can calculate the cutoff-dependent performance metrics. This is
237 the analogous operation to splitting a probability distribution into two distinct classes, although in
238 our case, this is performed directly within ArcGIS into map form. In this process, the first class
239 (*i.e.*, the lower percentage of susceptibility/ suitability map) is considered as the absence areas
240 (*e.g.*, the landslide-free areas) and the upper part as the presence locations (*e.g.*, the landslide
241 affected areas). For instance, let us assume a 50% cutoff for a landslide susceptibility map of
242 particular interest with 20 landslides located within the lower 50% (*i.e.*, low to moderate
243 susceptible areas). In this case, those 20 samples will be considered as error sources (denoted as
244 the ‘false negative error’, that has been discussed later) by the proposed tool and consequently, it
245 can reduce the performance of the predictive model since the landslides that have already occurred
246 are supposed to be located within the areas with the highest susceptibility values. The 50% cutoff
247 value is also quite common in existing literature, especially for the equally balanced
248 presence/absence datasets (*e.g.*, Lombardo and Mai, 2018). However, the prevalence can be
249 considered as the best alternative since it is able to represent the inherent predominance of a
250 phenomenon and it is not controlled by the experimenter. Additionally, quantifying the prevalence
251 of a natural phenomenon is somewhat problematic (discussed in Section 5.3). Most of the data
252 mining models can circumvent this issue by calculating the prevalence by means of estimating the
253 best possible distribution of an event using generalized algorithms which is common in the
254 presence-only models (*e.g.* Maximum entropy model).

255 **3.2. Cutoff-dependent Approach**

256 Cutoff-dependent metrics include True Positive Rate (TPR), True Negative Rate (TNR), False
257 Positive Rate (FPR), False Negative Rate (FNR), Misclassification rate, Accuracy, Positive
258 Predictive Value (PPV), False Discovery Rate (FDR), Negative Predictive Value (NPV), False
259 Omission Rate (FOR), F-score, Matthews Correlation Coefficient (MCC), Informedness
260 (Bookmaker informedness; BM), Markedness (MK), Threat Score, Equitable threat score, True
261 skill statistic, Heidke's skill score, Odds ratio, Odd ratio skill score, and Cohen's kappa. Table 4
262 details the equations for all of the cutoff-dependent metrics.

263 **Table 4** HERE

264 The TPR, also termed as the sensitivity, recall, or hit rate, represents the probability of correctly
265 predicting the positives as observed in reality (given as True positives (TP) / total number of
266 positives (P)). The TNR, termed as the specificity, aims to quantify the probability of correctly
267 predicting the negatives as observed in reality (given as true negatives (TN)/ total number of
268 negatives (N)). The FPR, also known as the “1–specificity” or fall-out, aims to indicate the
269 probability of incorrectly predicting a non-event location as an event (given as false positives
270 (FP)/ total number of negatives (N)). Furthermore, the FNR, also denoted as the miss rate,
271 indicates the probability of incorrectly predicting an event location as a non-event (given as false
272 negatives (FN)/ total number of positives (P)). This quantity is used to express how often the
273 model wrongly predicts absences. Misclassification rate undertakes both the false negative and
274 false positive values and therefore reflects an overall error rate ((FP+FN)/total). The accuracy (or
275 the model efficiency) is the opposite metric compared to the misclassification rate, since it is able
276 to highlights the overall success of the predictive model ((*i.e.*, TP+TN)/total). Overall, this metric
277 shows how often the predictive model is correct. The PPV, also denoted as the confidence or the
278 precision in data mining approaches, or as Powers (2011) analogously calls it as the accuracy of

279 predicted positives, is used to measure the proportion of predicted presences that correctly
280 represent the real presence. As a complement component of the PPV, a false discovery rate is
281 applied to conceptualize the Type I errors (*i.e.*, rejection of a true null hypothesis) (Benjamini
282 and Hochberg, 1995). In accordance with the PPV, the NPV is used to measure the precision of
283 the predictive model in predicting the absence (or non-event) locations. However, this metric
284 largely ignores how well the model is able to handle the presence locations and that the FOR
285 simply is the complement of the NPV. The F-score is also called the harmonic mean of the
286 precision and the recall (*i.e.*, sensitivity) where it reaches its best values at 1 (*i.e.*, best precision
287 and recall) and the worst at 0. In essence, MCC is a correlation coefficient metric computed
288 between the observed and the predicted binary classifications, and it is able to undertake a true
289 and a false positive and negative value. The terms *informedness* and *markedness*, implemented in
290 the PMT, were introduced initially by Powers (2011). Informedness, however, is likely to be the
291 only unbiased indicator in the confusion matrix and it measures the probability that an informed
292 decision that is being made rather than guessing, either the correct or the incorrect decision (due
293 to overtraining, atypical data, or even deliberately) (Powers, 2011). Markedness, also referred to
294 as *deltaP* in psychology, is the complementary pair of informedness indicating the probability
295 that an outcome is marked by the predictor (marker). Threat Score also penalizes the rare events
296 since some success of correct predictions of a less frequent event might be resulted out of
297 random chance. Although Threat Score uses different statistics in conjunction, the actual sources
298 of misclassification error are not discernible. Equitable Threat Score also known as the Gilbert's
299 skill score (Gilbert, 1884; Schaefer, 1990), the equitable threat score functions as per above
300 based on critical success score, but it is also used to eliminate the hit rates (*i.e.*, true positive
301 rates) originated by random chance. True skill statistic (TSS) (also called the Hanssen and

302 Kuipers discriminant or Pierces skill score), is applied to measure the ability of a predicted value
303 to discriminate between the events and the non-events, using all of the elements in the confusion
304 matrix. The Heidke's Skill Score operates according to the accuracy level but it is also used to
305 improve its meaning by eliminating the true positive rates that would be expected to occur by
306 chance (Heidke, 1926). Odd Ratio is used to measure the odds that an event (or an outcome) will
307 occur given a particular exposure, compared to the odds of the event occurring in the absence of
308 that exposure (Pepe et al., 2004). Odd Ratio Skill Score (also known as the Yule's Q) rescales
309 the values of the odds ratio into the -1 and the +1 range. In addition, Kappa is essentially a
310 measure of how well the model has performed as compared to how well it would have performed
311 purely by chance, and this would enable the modeler to better understand the true outcome of the
312 model in respect to the random occurrence of that value.

3.3. Cutoff-independent approach

313 This approach, included in the PMT, includes two different methods that can be categorized as:
314 (1) receiver operating characteristic (ROC) curve, and (2) success-rate curve (SRC) and
315 prediction-rate curve (PRC).

3.3.1. ROC curve

317 The ROC curve, used typically in risk assessment through predictive model results, simply
318 plots the sensitivity (*i.e.*, true positive rates) on the *Y*-axis against the 1-specificity (*i.e.*, false
319 positive rate) on the *X*-axis (Gorsevski et al., 2006). The area under the ROC curve (denoted as
320 AUROC, bounded by [0, 1]), is the actual measure of the model evaluation since it generates a
321 quantitative value of the performance (Pontius and Schneider, 2001; Mas et al., 2013; Swets,
322 2014). The closer the AUROC is to unity, the better is the performance. The ROC curve can be
323 interpreted differently depending on the dataset; it can address the learning capability (or the so-

324 called goodness-of-fit) of the model if the training set is used for plotting; it can also infer the
325 predictive skill of the model if the validation set is used (Fawcett, 2006; Lombardo and Mai 2018).

326 In this regard, the proportion between training and validation samples is highly relevant. A
327 70:30% split is quite common among the researchers (Pradhan and Lee, 2010). Although different
328 partitions have also been used, such as 80:20% (*e.g.* Lipovetsky, 2009), 70:30% (*e.g.* Choubin et
329 al., 2019) or even 50:50% (*e.g.* Deo et al., 2016; Deo et al., 2017), there is no empirical consensus
330 on the best partition since this is more of an expert-user based decision. Irrespective of this, having
331 a large amount of inventory data (*i.e.*, number of events), one can assign a greater percentage of
332 such data to train the predictive model and a lesser percentage for validation. Opting for a suitable
333 approach to partition the training and validation sets is yet another crucial matter that has been the
334 subject of many studies, *e.g.* Kornejady et al. (2017). In this regard, the random sampling, self-
335 organizing maps for input selection, Mahalanobis distance, excerpting separate training/validation
336 areas, and temporal partitioning are all some of the common sample partitioning approaches. For
337 more details, readers can refer to the references therein.

338 **3.3.2. Success-Rate Curve (SRC) and Prediction-Rate Curve (PRC)**

339 The SRC is a measure of the learning capability of the model, while the PRC is able to examine
340 the predictive power. Although the SRC and the PRC may share some common features with the
341 ROC, the ROC in particular uses almost all the elements of the confusion matrix. This includes
342 positive (TPR and TNR) and negative (FPR and FNR) aspects of the model, while the SRC and
343 the PRC are calculated independently from the confusion matrix. In fact, the SRC represents the
344 cumulative areal percentage of the susceptibility classes (*i.e.*, from the highest values to the lowest)
345 on the X -axis against the areal cumulative percentage of the training set located within those

346 susceptibility classes on the Y-axis (Chung, 2006; Blahut et al., 2010). In terms of its physical
347 interpretation, a steeper SRC curve is used to indicate that more events fall within the highly
348 susceptible classes; *i.e.*, a good learning skill. The PRC curve, however, follows the same plotting
349 process as the SRC, but the training data are replaced by the validation set.

350 **4. Testing the Efficacy of PMT: Selected Case Studies**

351 In this section, the proposed PMT is applied to 5 distinct, real geo-environmental modelling
352 tasks and case studies in order to robustly investigate its credibility and generalizability, and also
353 to demonstrate the potential benefits in considering different evaluation criteria promulgated by
354 the PMT. It is imperative to note that the selected case studies exhibited various noticeable
355 characteristics in terms of the issue under investigation, the modelling strategies, the overall
356 frameworks and the predictive model type, spatial or temporal scales considered and the
357 geographical and climatic conditions that influence the results and implementation of the model.

358 To provide a robust evaluation of the proposed PMT, the most relevant and a relatively diverse
359 range of data sets were obtained from most recently conducted research studies and also some
360 newly implemented models based on: (1) gully erosion prediction mapping in two small
361 catchments of central-western Sicily, Italy (Conoscenti et al., 2018) (2) flood hazard modelling in
362 the Galikesh region, Iran (Rahmati and Pourghasemi, 2017) (3) drought risk modelling in south-
363 east Queensland, Australia (Dayal, 2018; Dayal et al. 2018) (4) landslide susceptibility modelling
364 in the Kon Tum province, Vietnam (5) soil digital modelling in South Dakota, USA (Fig. 1). Each
365 of these studies employed a range of geo-spatial models where the PMT is used to provide a
366 consolidated assessment of its efficacy in providing greater insights into the practicality of the
367 modelling various frameworks.

368 An overall description of the study areas and the applied models are provided as follows whereas
369 further details of the modelling approaches are provided in the references therein.

370 A detailed flowchart of the various studies is shown in Fig. 2.

371 **Fig. 1** HERE

372 **Fig. 2** HERE

373 **4.1. Gully Erosion Modelling (Italy)**

374 Intense farming activities in two small catchments of central-western Sicily, Italy, have
375 expedited many erosion processes. In particular, the gully erosion has led to the landscape
376 dissection and massive soil loss (Conoscenti et al., 2018). The gullies in the study area have
377 developed as a result of the interrelation of several geo-environmental factors and human activities
378 such as access roads, parcel borders, wheel tracks, and plow furrows. In addition to the
379 multivariate adaptive regression splines (MARS) model already utilized by Conoscenti et al.
380 (2018) for gully erosion prediction mapping, in this paper we used the generalized linear model
381 (GLM) to conduct a fair comparison of their approach (Fig. 3).

382 **Fig. 3** HERE

383 **4.2. Flood Hazard Modelling (Iran)**

384 Over the last few decades, the Galikesh region, located in the Golestan province, in the north-
385 east of Iran, has witnessed severe flood events due to the particular climatic and topo-hydrological
386 conditions that resulted in many economic losses and casualties attributable to environmental
387 mismanagement (*e.g.*, deforestation, overgrazing, and over-exploitation). Since flood-inundation
388 has been one of the major issues of the urban areas in Golestan province for decades, Rahmati and

389 Pourghasemi (2017) used evidential belief function (EBF) to investigate the flood-prone hotspots
390 (Fig. 4). In this paper, we have implemented the proposed PMT as a statistical and decision-
391 support tool to provide an inclusive performance evaluation of their model.

392 **Fig. 4** HERE

393 **4.3. Drought Risk Modelling (Australia)**

394 An area located in the south-east of Queensland, Australia, encompasses intensive agricultural
395 activities, such as grazing, horticulture, and animal production, other than the densely populated
396 localities, which require a reliable water supply. As the study area is affected by severe and
397 frequent drought events, Dayal (2018) and Dayal et al. (2018) attempted to develop a spatial
398 drought risk map by employing the Bayes' theorem (*i.e.*, classifying spatial indicators), fuzzy
399 logic (*i.e.*, standardizing spatial indicators), and fuzzy GAMMA overlay (*i.e.*, aggregating drought
400 vulnerability, exposure, and hazard indices) technique (Fig. 5). Employing the findings of that
401 study, in this paper we utilized their final drought risk map as a potential input to the proposed
402 PMT, enabling us to examine the different aspects of its performance over the geospatial scale. In
403 order to investigate the influence of the cutoff values on the performance analysis, three different
404 cutoffs, *i.e.*, 50%, 70%, and 90% were taken into account and the results were compared, as
405 illustrated in Fig. 6.

406 **Fig. 5** HERE

407 **Fig. 6** HERE

408 **4.4. Landslide Susceptibility Modelling (Vietnam)**

409 Landslides are the dominant geo-hazardous elements in the Kon Tum province of Vietnam.
410 Hence, this study has used two novel data mining models including maximum entropy (MaxEnt)
411 and a recently developed model named as BayGmmKda (Bayesian-based ensemble of Gaussian
412 mixture model and radial-basis-function Fisher discriminant analysis) (Tien Bui and Hoang, 2017)
413 (Fig. 7). This study also uses the proposed PMT to highlight the potential asymmetries among the
414 performance metrics.

415 **Fig. 7** HERE

416 **4.5. Soil Digital Modelling (USA)**

417 Soil digital modelling has received significant attention amongst scientists in recent years,
418 where computer-assisted pedometric-predictive mapping of soil properties has led to the creation
419 of an inclusive geographically-referenced soil database. To this end, an attempt is carried out to
420 map the soil bulk density (BD) predictive distribution in South Dakota, USA, by obtaining soil
421 bulk density samples of the study area and using two data mining models, namely the artificial
422 neural network (ANN) and decision tree (DAT) (Fig. 8). We have delineated the need for
423 rendering quantitative suitability maps into probability values to be able to use the proposed PMT
424 for further assessing the models' performance. In general, there is a few differences between
425 models' requirements. For example, DAT model does not require a separate dataset to optimize
426 parameters and just uses the training dataset for model building (i.e., learning and predicting),
427 whereas ANN model uses both the training and validation datasets for model building, validation,
428 and reevaluation and tuning parameters. Therefore, in ANN model, soil inventory dataset was
429 divided into three subsets: training (50% of input data) and 25% each for validation and testing.
430 For comparison sake, the same 25% testing dataset was kept in a vault and used for assessing the
431 generalization power of both the ANN and DAT models.

432

433

Fig. 8 HERE

434 **5. Results and Discussion**

435 The following results and the subsequent discussions are based on Table 5, containing all the
436 previously-described performance metrics that have been calculated by means of the newly
437 proposed GIS-based PMT extension system. After a preliminary diagnosis of the models in each
438 of the aforementioned case studies, a detailed comparison of the performance metrics is provided.¹

439

Table 5 HERE

440 **5.1. Gully Erosion Modelling, Italy**

441 According to the AUROC values, both the GLM and the MARS model show excellent
442 performance where the differences in the AUROC values were almost negligible. According to
443 Conoscenti et al. (2018), the excellent performance of these two models is indebted to a well-
444 investigation of the gullies in the study area and opting the main controlling factors that best
445 defined the occurrence mechanism. This process has been carried out by building a base model
446 comprised of the slope gradient and the contribution area and is then fed by nine other geo-
447 environmental factors one at a time. Moreover, the exemplary features of the chosen model have
448 also led to a significantly good performance, defined by measures such as the handling of all types
449 of factors (*i.e.*, both categorical and continuous) and well detecting the interactions among the
450 factors and also between the factors and the response event. Notably, Gómez-Gutiérrez et al.

¹ Note: the discussion provided here follows a particular way as the inferences derived from each case study is modified or reemphasized perpetually on the basis of the collective information obtained from different case studies and modelling scenarios. It is tried to be err on the side of caution to avoid raising any misleading points and engaging in dogmatic defense of one approach to the detriment of another.

451 (2015) also applied the MARS model to predict the gully occurrence in a relatively close (ca. 85
452 km) catchment with similar characteristics; however, the AUROC values stood at the range of
453 about 0.75-0.85, which was lower than that of Conoscenti et al. (2018). This highlights the
454 importance of making a well-structured input data and the calibration/ validation techniques. To
455 this point, both models seem to have rather similar performances.

456 However, a greater discrimination between models become apparent, as present in the results,
457 after breaking down these overall precision metrics into smaller components (*i.e.*, considering
458 simpler indices) that explain the efficacy of the approach more elaborately. Considering the
459 misclassification rate of both models, it is evident that the GLM approach has most likely
460 misclassified the presence and the absence more than the MARS model. Also, accuracy, as
461 understood to be the opposite concept of misclassification rate, attested the same pattern, where
462 the MARS model exhibited a higher accuracy in the classification of the presence and the absence
463 localities generated by the spatially-relevant model.

464 Further exploring the confusion matrix, it becomes evident that the higher value of the
465 misclassification rate in the GLM approach is directly rooted in the false negative rate. That is, the
466 GLM approach appears to have misclassified a number of ‘presence locations’ as the ‘absence
467 locations’ (in fact, this happened almost 13 folds greater than the MARS model). This indicates
468 that the GLM approach has somewhat failed to locate the gullies in notable study areas, and
469 therefore, may require further careful consideration prior to its application for real-life decisions.
470 In fact, the present analysis shows that this error appears to have also spread out to the other
471 metrics such as the sensitivity, F-score, NPV, and the FOR. The reason for the high AUROC value
472 for the GLM approach is plausibly due to that the latter is a cutoff independent metric, while the
473 confusion matrix elements have been calculated based on a 50% cutoff value. However, this does

474 not justify the GLM's underperformance at misclassifying the absence locations, since both
475 predictive models are compared under the same situation.

476 As explained in the *Theory* section, in such situations, the MCC may be the best representative
477 of the model's performance regarding the agreement between the observations and predictions.
478 One reason for this is because, as opposed to AUROC, AUSRC, and AUPRC, the MCC values the
479 cost of error and attempts to avoid to circumvent or truncate any error sources. Expectedly, the
480 MCC has well differentiated the performance of both MARS and GLM approaches, where the
481 MARS model with a value close to 1 almost represents a perfect model, while the GLM approach
482 with a value below 0.5 has shown a lesser degree of agreement between the observations and
483 predictions. This notion raises the possibility of some randomness (*i.e.*, being closer to zero). The
484 underperformance of the GLM approach highlights the disadvantages of using a predictive model
485 that is built on linear functions. Such a model is largely incapable of considering the nonlinear
486 interactions between the causal factors and the response event, may be sensitive to the number of
487 predictors, and more importantly, it could be sensitive to the outliers which are robustly handled
488 by non-linear basis functions in the MARS model. Given that the asymmetries of the cutoff-
489 dependent and -independent metrics are now more evident, a greater degree of scrutinization is
490 perhaps required, as provided by a more extensive discussion in the following real-life case
491 studies.

492 **5.2. Flood hazard modelling, Iran**

493 Recently, Evidential Belief Function (EBF), as a bivariate statistical model underpinned by the
494 Dempster-Shafer theory (Shafer 1976), has been adopted for flood inundation and susceptibility
495 mapping in Iran (Rahmati and Pourghasemi, 2017). Starting with the AUROC values, the overall

496 performance is acceptable, with respectively, 0.86 as the learning capability (obtained from the
497 training set) and 0.78 as a predictive skill (obtained from the validation set). Higher learning skill
498 compared to the predictive capability is common, and generally expected since the model's
499 parameters have been calibrated on a much larger data sample compared to the validation set.
500 However, this might question the possibility of overfitting, where a statistical model begins to
501 describe the random error in the data rather than the relationships between variables; that is, the
502 model becomes accustomed to the pre-used set of data. In this regard, simple statistical
503 assumptions have been identified as one of the main sources of overfitting issues, especially in
504 bivariate statistical models. This can negatively influence the generalization power and the
505 transferability of the model's results to the validation set/ areas/ time periods.

506 Considering the results presented here, all of the favorable qualities of the model (*i.e.*, all the
507 performance metrics highlighting the success of the model) have deteriorated to some extent in the
508 model validation stage. Although according to the AUROC classifications provided by Hosmer
509 and Lemeshow (2000), the values greater than 0.7 and 0.8, respectively, indicate an acceptable and
510 excellent performances, which in turn somewhat addresses the possibility of overfitting. This is
511 also evident in the AUSRC and AUPRC values, indicating that the predictive model is
512 respectively well-performing in terms of both the learning capability and the predictive skill. As
513 for the AUSRC and AUPRC values, the differences are discernable when compared to the
514 training- and validation-derived AUROC values. These differences are conceivable, given that the
515 AUSRC and AUPRC are calculated merely based on the presence localities. Therefore, by using
516 the AUSRC and AUPRC, the potential error sources (*i.e.*, polluting the presence population to
517 some absences which are incorrectly classified as positives) are left unclear and some degree of
518 success (*i.e.*, correctly detecting the absence locations) are also not acknowledged and not

519 included in the final calculation. This makes using the AUSRC and AUPRC less favorable to use
520 due to their erroneous behavior (Frattini et al., 2010).

521 A closer scrutinization appears to shed more light on the randomly-driven performances and
522 consequently, the weakness of the model or the input data. Considering the MCC—so far
523 suggested as an all-inclusive metric in this study—the values greater than zero (*i.e.*, random
524 agreement) reveals a promising level of precision; however, the values may not be high enough
525 (*i.e.*, far from a perfect precision to be certain of a non-random performance. In particular, the
526 level of disagreement between the observed and the predicted values appears to increase in the
527 validation stage. Other comprehensive measures, such as the true skill statistic, informedness, and
528 markedness are also in concurrence with the MCC value.

529 The Heidke's Skill Score, well-known for providing a robust accuracy value by diminishing the
530 TPR values generated by random chance, shows how the preliminary accuracy values (*i.e.*,
531 efficiency) is likely to decay. Similarly, the Cohen's Kappa aims to address the random aspect of
532 the model performance and provides new values in agreement with the latter. However, as stated
533 in our recent discussion, one should be cautious when using the cutoff-dependent metrics.
534 Drawing relevance from a report given by Frattini et al. (2010), the score-based metrics, despite
535 providing valuable insights, highly relies on certain cutoff values. That is, different cutoff values
536 might result in different performance values. However, this assumption still does not contradict
537 using the score-based metrics for a comparison purpose, since, as stated above, all the predictive
538 models were supposed to be compared under the same cutoff value(s) (*e.g.*, the Italian case study).
539 To test this concern, we have applied three different cutoffs for assessing the performance of a
540 drought risk map developed in the south-east region of Queensland, Australia.

541 To elaborate further, we provide two assumptions regarding the reduction in the accuracy of the
542 EBF metric. The first assumption pertains to the model's structure. Bivariate statistical models
543 have long been criticized for ignoring the interactions among the predictors, which can have direct
544 (and largely negative) influence on both the learning and the predictive skills. Moreover, as stated
545 by Ruspini et al. (1992), and more recently Reineking (2014), a need for categorizing factors with
546 continuous nature and also presenting a generalized probabilistic reasoning limit the application of
547 the EBF metric only to some specific problems (*e.g.*, detecting the uncertainty sources) rather than
548 a general use. However, a review of the previous work of Rahmati and Pourghasemi (2017)
549 reveals that the two other well-known data mining models (*i.e.*, boosted regression trees and the
550 random forest) have been used in addition to the EBF and surprisingly, we noted that the EBF
551 outperformed both of the data mining models, although the differences were negligible (*i.e.*,
552 AUROCs= 0.73-0.78), which leaves us with the second hypothesis.

553 Regarding the latter, the input data can be responsible for such limited performances of all three
554 models. Reviewing the model input data shows that only 63 flooding points were used as an input
555 for the modelling process in the period of 2001-2009, let alone that they were categorized into two
556 sets of 47 (training) and 16 (validation) locations which seems to be rather small to build a proper
557 predictive model. Complementing the inventory map by collecting more data from a broader time
558 period would provide a larger information matrix for the models to rely on. This highlights a note
559 given by Ruspini et al. (1992); "*the alleged lack of decision-support and counterintuitive nature of*
560 *evidential belief models, in fact, indicates the lack of basic informational shortcomings*".

561 **5.3. Drought Risk Spatial Attribution and Modelling, Australia**

562 For a drought risk map produced in the south-east of Queensland, Australia, the following
563 inferences can be derived from the validation stage only in order to focus on the alteration of the
564 performance metric values. The question mentioned above regarding the liability of the cutoff-
565 dependent metrics is answered by means of producing three cutoffs thresholds, *i.e.*, 50%, 70%,
566 and 90%, and then comparing these results.

567 It was evident that the AUROC and AUSRC expectedly yielded intact performance values
568 through all of the three cutoffs (Table 5). Based on this, the predictive skill of the fuzzy model
569 appears to be well performing. However, the values of all the cutoff-dependent metrics drastically
570 change at each cutoff. It is evident that by a transition from 50% to 90% cutoff, the area of danger
571 zone appears to shrink (as illustrated in Fig. 8). Moreover, at each cutoff threshold, a different
572 population of the negatives and the positives appears to fall within the safe and danger zones.

573 The direct impact of these transitions on the results is transparent in Table 5. As appears,
574 moving from 50% to 70% cutoff, the *FN* error decreases to a certain level and adds to the *TN*,
575 serving as an advantage point for the model, while the false positives and true positives have
576 remained intact. Moreover, a vivid increase is also discernible in the values of the cutoff-
577 dependent metrics. However, another step towards the 90% cutoff backfires, where—similar to the
578 previous transition—although the *FN* value decreases and adds to *TN*, most of the *TP* population
579 migrates to *FP* category. This expectedly decreases the values of some cutoff-dependent metrics
580 such as F-score and PPV. Although 70% cutoff performed better than 50% and 90% cutoffs. Such
581 a choice would not be advisable for the other study areas and certainly not for the other predictive
582 models, because it is only in favor of this particular predictive model and the specific distribution
583 of the positive/negative points throughout the study area.

584 As previously mentioned in the *Theory* section, the only suitable substitute for the cutoff value
585 is the prevalence of the phenomenon, which again is difficult to ascertain, unless one constructs an
586 inclusive archive of the ‘presence-absence locations’ by visiting numerous sites. This type of data
587 compilation is more common in species distribution assessment, whereas, in natural hazard-related
588 studies, extracting absence locations are executed as an additional stage after inventory mapping,
589 based on random selection or other analytical strategies. Drawing on these inferences, it is
590 reasonable to ascertain that using cutoff-dependent performance metrics may not be practical for
591 individual model assessment, unless it is accompanied by mentioning the cutoff value from which
592 the metrics’ values are extracted (*i.e.*, 50% for Iran, Italy, and all the following case studies), or it
593 is carried out by setting the prevalence as the cutoff value.

594 As with the case of Iran, the AUROC yielded the most accurate performance value that a
595 spatial modeler can rely on. Thus, based on current arguments, we confirm the second assumption
596 in which the incapability of the models (*i.e.*, EBF, BRT, and RF) to progress is due to the
597 unsatisfactory input data (*i.e.*, either scarce inventory, inadequate spatial indicators or spatial
598 resolution) rather than the models’ structure. Analogously, the AUROC and AUPRC values are
599 more representative for the fuzzy model’s performance in Queensland, Australia. Also, they are
600 comparatively in accordance with the validation method of Dayal (2018) and Dayal et al. (2018),
601 based on which the correlation of the drought risk map and the soil moisture/ rainfall departure
602 maps confirmed plausible predictive skills.

603 Comparing the different predictive models (*i.e.*, choosing the premier model among the many
604 alternatives) or different scenarios of a specific model (*i.e.*, opting the best scenario from different
605 sample partitioning techniques, different spatial resolution, and so forth), is still feasible by using
606 the cutoff-dependent metrics as they do provide valuable information that can lead to a more

607 transparent distinction between the choices. In particular, the cutoff-dependent indices can assist
608 us with distinguishing the features of the GLM and the MARS models for the case study in Italy.
609 Hence, in the following case studies, the cutoff-metrics are used only for a comparison and
610 selection of the better-performing predictive model.

611 **5.4. Landslide Susceptibility Modelling, Vietnam**

612 In accordance with the analytical evidence from the results of previous case studies, this study
613 avers that the use of the cutoff-dependent metrics can be informative for a predictive model
614 comparison. The inferences of this case study are interesting in several ways, showing that how
615 one should interpret the latter with some degree of caution. According to the AUROC and
616 AUPRC values of MaxEnt and BayGmmKda models tested in Vietnam (Table 5), the MaxEnt
617 appears to slightly excel in predictive skill, although both models show an excellent performance
618 (AUROC > 0.8). On the other hand, asymmetries are evident in the values of the cutoff-dependent
619 metrics, as we have categorized them as the ROC-accordant and -discordant metrics (see Table 6).

620 **Table 6** HERE

621 According to Table 6 and the relevant equations provided in Table 4, both categories support
622 high *TP* and *TN* values, while there is a subtle difference that makes them oppose. In fact, a
623 model's success in *FP* stage is highly favored in the ROC-accordant metrics, while the discordant
624 group leans towards penalizing a model's downfall in the *FN* stage. This is evident in the
625 confusion matrix of the MaxEnt and BayGmmKda, in which the MaxEnt shows an outstanding
626 performance with a zero *FP* value, while the *FN* population is drastically increased in such a way
627 that it even surpasses the *FN+FP* population in BayGmmKda model. In this case, the
628 BayGmmKda has well balanced the FP and FN population that accords to Table 7. As previously

629 mentioned in the *Theory* section, although a zero FP (Type I error) in MaxEnt results cause no
630 infrastructural and study costs, a drastic increase in FN (Type II error) values can cause massive
631 casualties via misrepresenting an area as a safe location.

632 **Table 7** HERE

633 Considering the structure of these predictive models, as opposed to the presence-absence nature
634 of the BayGmmKda, MaxEnt is considered as a presence-only model where some randomly
635 chosen pseudo-absence locations (*i.e.*, background samples) help the model differentiate the
636 presence locations and eventually predict an occurrence pattern. Therefore, presence-absence-
637 based validation metrics (*i.e.*, all the metrics provided in this study) may not be a good fit for the
638 performance assessment of MaxEnt. This being the case, AUPRC might be the best fit for MaxEnt
639 and in fact, it has clearly distinguished the performance of both models. However, according to
640 Phillips et al. (2006), at least, those background locations should be considered as ‘pure absences’
641 to be able to graph a ROC curve, and also to calculate the metrics derived from confusion matrix.
642 This is an inevitable process for the MaxEnt. Another critical inference of this case study
643 underlines that although cutoff-dependent metrics are valuable metrics for comparing different
644 models, they are not necessarily supposed to be in line with cutoff-independent metrics. This is the
645 reason why MaxEnt and BayGmmKda both excel, but in different areas. Therefore, relying on
646 what we have conceived so far, each cutoff-dependent or -independent metric has a unique
647 indication of a model’s performance.

648 There is a consensus that selecting the best predictive model can be a matter of the user
649 preference and study area’s goals, which has been previously well-delineated in Goetz et al.
650 (2015). This can be carried out by relying on a pros and cons list for all the metrics and assessing

651 whether they work in agreement with the objective(s) of the project. Taking aside the
652 disadvantages of cutoff-dependent metrics, some critics have also been moved towards AUROC
653 (Lobo et al., 2008). The main complains pertain to ignoring the PPV (addressed earlier in *Theory*
654 section) and equally weighting omission (not recording some instances) and commission (miss-
655 recording some instances) errors. However, this directly stems from predefining a series of
656 thresholds and the presence-absence fabric of AUROC which is not only specific to AUROC but
657 rather all the performance metrics. Furthermore, these limitations do not question the metric itself,
658 but rather the application of them. For instance, ROC curves were first employed in the study of
659 “*discriminator systems for the detection of radio signals in the presence of noise in the 1940s*”,
660 following the attack on Pearl Harbor, USA (Garrett et al., 2008). Even the use of AUROC in
661 clinical biochemistry is carried out under a presence-absence condition (Obuchowski et al., 2004).
662 Therefore, in order to employ AUROC and other cutoff/prevalence- independent metrics in a
663 probabilistic environmental modelling context, their limitation should be accepted in favor of their
664 valuable outcomes regarding the performance evaluation.

665 Under these premises, we aver that the project study goal can assist the decision maker with
666 opting the well-performing model. For instance, if the number of opposing metrics matters the
667 most, the BayGmmKda would be the well-performing one. In particular, many municipal
668 authorities may decide in favor of public safety, which in turn can end in an immediate rejection
669 of the MaxEnt due to having considerable Type II error that can also cause notable fatalities.
670 Comparatively, if the uncertain nature of the cutoff value is in question, one can choose the
671 decisive judgment of the AUROC.

672 **5.5. Soil Digital Modelling, USA**

673 As previously mentioned, this case study represents a unique application of the proposed PMT
674 for performance assessment of the Bulk Density (BD) lateral distribution in South Dakota, USA.
675 In contrast to the previous applications of data mining methods that deal with predicting the
676 probability of an occurrence, in this study we employed the ANN and DT approaches for
677 predicting an actual quantity of BD whose actual amounts can be measured in the field. Measuring
678 the BD samples from different location of the study area, root mean square error (RMSE) can be a
679 good metric to test the accuracy of the results (*i.e.*, an approximated standard deviation of data) if
680 the data are Gaussian (*i.e.*, rich data) and devoid of any outliers (Chai and Draxler, 2014).
681 However, RMSE or accuracy, in general, can be biased and may not reflect the total precision of a
682 predictive model, warranting the need for a consolidated list of model evaluation metrics that
683 provide more extensive insights into the predictive performance.

684 In respect to the above discussion, the proposed PMT approach can be a good alternative, but
685 the nature of the prediction map should be rendered into its probability terms or at least as an
686 indication of the probability. That is, the higher values of the prediction map can indicate the
687 greater probability of having higher BD values, and vice versa. By doing so, the cutoff-dependent
688 and -independent metrics have been calculated based on which, almost all the indices congruently
689 introduce ANN as a better-performing model compared to DAT; the rest of opposing metrics (e.g.
690 specificity and PPV) show negligible differences. This is in agreement with those reported by
691 Taghizadeh-Mehrjardi et al. (2017) where the ANN was seen to outperform the support vector
692 machine (SVM) model in the mapping of soil organic matter distribution.

693 **6. Synthesis and Conclusion**

694 This paper provides a novel scientific contribution towards the design and implementation of an
695 adaptive, largely automated and user-friendly GIS-based spatial model assessment system,
696 denoted as the Performance Measure Tool (PMT). PMT can be used to address existing challenges
697 in pragmatic evaluation of predictive models in diverse contexts, and generally, for any scientific
698 branch where information has a spatial connotation. The PMT encloses the relevant mathematical
699 formulations to make it an easy-to-use software; it has the added capability to evaluate the
700 accuracy of the spatial modelling approach based on the different cutoff-dependent and -
701 independent evaluation criteria. The PMT is considerably flexible, and hence, it can be widely
702 applicable in multiple scientific and engineering applications where spatially-relevant predictive
703 models are tested. The approach has the potential to be applied in diverse contexts, as verified in
704 this research study, to extend its usage from geo-environmental spatial models to fields such as
705 medical geography and epidemiology where data-driven approaches are adopted to generate
706 predictive models and such models require robust comparison with several benchmark models and
707 real-life (observed) datasets.

708 In context of proposing an additional GIS-based predictive model assessment tool, the
709 consolidated metrics that are generated and evaluated by the proposed PMT, certainly provides a
710 new practical pathway for real-life decision-makers who are seeking a better performing
711 predictive model (relative to any other comparative model). Based on contested reasons, and
712 evaluations of PMT with several studies collated in this research paper, real-life decision-makers
713 can deduce the grounds on which their predictive models performs better than the others prior to
714 implementing them for practical use. By accommodating multiple types of real-time geo-
715 environmental modelling instances in this study, the take-home messages are as follows. The use
716 of a merely row-wise or a column-wise calculated index from the confusion matrix is not a robust

717 approach for model selection as this can ignore the more practical concepts considered by their
718 counterpart tools.

719 In contrast, some of the model evaluation indices (*i.e.* cutoff-dependent and –independent ones)
720 generally use a collective information of the matrix in such a way that a set of multiple statistics
721 are used in conjunction with each other. Notwithstanding this, some cutoff-dependent metrics may
722 infer the same connotation which they can be used interchangeably (*e.g.*, threat score and
723 equitable threat score, or the odds ratio and the odds ratio skill score). Moreover, the choice of
724 using the cutoff-dependent metrics over each other without a prior knowledge can also constitute
725 an unjust approach since each metric is able to tackle a different aspect of the model performance.
726 However, all metrics can be highly sensitive to the cutoff values so, they should be suggested only
727 for the model comparison.

728 As demonstrated in the theory of PMT and relevant case studies, it becomes unambiguous that
729 the measurement of the prevalence of the studied phenomenon is highly advisable in order to
730 ascertain reliable cutoff-dependent values. Doing so, they are likely to be applicable even for the
731 performance assessment of an individual model, and also, they could be comparable with cutoff-
732 independent metrics.

733 On the other hand, the cutoff-independent metrics (*i.e.*, AUROC, AUSRC, and AUPRC) can
734 decisively screen the premier model regardless of the changes in their cutoff values. However, the
735 AUROC is also underpinned by some specific assumptions so that using it would require
736 accepting its mathematical fabric. Furthermore, AUSRC and AUPRC only support presence
737 locations, they show an erroneous behavior and in particular may result in an underestimation of
738 performance compared to AUROC. Moreover, all cutoff-dependent and -independent metrics can

739 occasionally mislead by providing different results and consequently different model ranks. In
740 such case, selecting the reference model is strictly tied to the aim of the research and specific
741 aspect(s) of interest. We also concluded that compartmentalizing models in different performance
742 categories is not feasible since the matter of performance itself is quite relative.

743 We also propose the following scenario-based decision-making inferences:

- 744 I. Italy and USA case studies: having more than one model→ if AUROC values converge
745 and the changes are negligible→ using other cutoff-dependent metrics to derive the
746 better-performing model.
- 747 II. Iran and Australia case studies: having one model→ no access to prevalence value
748 change→ cutoff-dependent metrics change drastically by altering cutoff values→ use
749 AUROC as the decisive metric.
- 750 III. Vietnam case study: more than one model→ metrics are opposing and taking different
751 parts (i.e. each selecting a different model) → decision should be made based on the
752 project goal by making pros and cons list for all the metrics.

753 As our final upshot, ROC and AUC are metrics that tend to lump together the prediction as a
754 whole; however, studying confusion matrices, accuracy and precision of a model ensure a better
755 insight on a model hit and misses. This is something that can be rarely found in the literature,
756 despite its great importance. The PMT quickly provides a full suite of performance metrics
757 allowing the users to better evaluate their spatial model and supporting a more critical judgment,
758 which in turn can promote better decision-making procedures.

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769

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971 **Figure Captions**

972 **Fig. 1** Study sites on the world map

973 **Fig. 2** Methodological flowchart adopted in this study

974 **Fig. 3** Gully erosion prediction maps of the central-western Sicily (Italy) generated by using the
975 GLM (a) and MARS (b) models

976 **Fig. 4** Flood-inundation susceptibility map of the Galikesh region (Iran) obtained from the EBF
977 model

978 **Fig. 5** Drought risk map of the south-east of Queensland (Australia) produced by using fuzzy
979 GAMMA overlay technique

980 **Fig. 6** Effects of 50% (a), 70% (b) and 90% (c) cutoff values on the extent of safe/danger zones
981 and classification of presence/absence samples in south-east of Queensland

982 **Fig. 7** Landslide susceptibility maps of the Kon Tum province (Vietnam) obtained from
983 BayGmmKda (a) and MaxEnt (b) models

984 **Fig. 8** Bulk density predictive distribution maps of South Dakota (USA) generated from ANN
985 (a) and DT (b) models

Table 1 Confusion matrix elements.

Observed	Predicted	
	Class stable (-)	Class unstable (+)
Class stable (-)*	(- -) True negative (TN)	(+ -) False positive (FP; Error Type I)
Class unstable (+)**	(- +) False negative (FN; Error Type II)	(+ +) True positive (TP)

* Absence areas ** Presence areas

Table 2 The PMT input files

ID	Setting	Description	ID	Setting	Description
1	Input raster layers	The raster maps generated by any spatial model representing the susceptibility or suitability of a phenomenon over an area (you can add different maps for the same area as many as desired).	5	Validation positives	Import the shapefile of all the validation samples of the phenomenon of interest (discarded dataset in the training stage).
2	Cutoff	An a-priori cutoff percentage to split the input raster into two segments (50% is set as default).	6	Validation negatives	Import the shapefile of the non-event validation locations.
3	Training positives	Import the shapefile of all the training samples of the phenomenon of interest.	7	Output workspace	The pass to contain the outputs (a folder address).
4	Training negatives	Import the shapefile of the absence training locations (should be prepared beforehand by different methods mentioned in the text)	8	Number of classes (for SRC and PRC curves)	The number into which the spatial raster is to be reclassified (100 classes are set as default). The reclassification method is based on an equal interval. A higher number of classes will result in smoother SRC and PRC curves with more precise AUSRC and AUPRC values.

Table 3 The PMT output files

ID	Setting	Description
1	Html file	It explains the main results of the performance analyses including confusion matrix, cutoff-dependent metrics, and cutoff-independent metrics. ROC, SRC, and PRC curves are other parts of this html file. In addition, all results were classified into two groups of cutoff-dependent and cutoff-independent approaches with some useful explanations regarding these approaches.
2	Microsoft excel file	This file summarize all of quantitative results (without explanations)

Table 4 Equations of cutoff-dependent performance metrics

Performance metric	Equation	Performance metric	Equation
True positive rate (TPR; sensitivity)	$\frac{TP}{P} = \frac{TP}{TP + FN}$	Matthews correlation coefficient (MCC)	$\frac{(TP \times TN) - (FP \times FN)}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}$
False positive rate (FPR; fall-out; 1-specificity)	$\frac{FP}{N} = \frac{FP}{FP + TN} = 1 - \frac{TN}{TN + FP}$	Informedness (Bookmaker informedness; BM)	$TPR + TNR - 1$
True negative rate (TNR; specificity)	$\frac{TN}{N} = \frac{TN}{TN + FP}$	Markedness (MK)	$PPV + NPV - 1$
False negative rate (miss rate)	$\frac{FN}{P} = \frac{FN}{FN + TP} = 1 - TPR$	Threat score	$\frac{TP}{TP + FN + FP}$
Efficiency (accuracy)	$\frac{TP + TN}{T}$	Equitable threat score	$\frac{TP - TP_{random}}{TP + FN + FP - TP_{random}}$ where, $TP_{random} = \frac{(TP + FN)(TP + FP)}{T}$
Misclassification rate	$\frac{FP + FN}{T}$	True skill statistic (Pierce's skill score)	$\frac{TP}{TP + FN} - \frac{FP}{FP + TN} = \text{Sensitivity} + \text{Specificity} - 1$
Positive predictive value (PPV; precision)	$\frac{TP}{TP + FP}$	Heidke's skill score	$\frac{TP + TN - E}{T - E}$ where $E = \frac{1}{T} [(TP + FN)(TP + FP) + (TN + FN)(TN + FP)]$
False discovery rate (FDR)	$1 - PPV = \frac{FP}{FP + TP}$	Odds ratio	$\frac{TP \times TN}{FN \times FP}$
Negative predictive value (NPV)	$\frac{TN}{TN + FN}$	Odd ratio skill score (Yule's Q)	$\frac{(TP \times TN) - (FP \times FN)}{(TP \times TN) + (FP \times FN)}$
False omission rate (FOR)	$1 - NPV = \frac{FN}{FN + TN}$	Cohen's kappa	$\frac{(TP + TN) - [(TP + FN)(TP + FP) + (FN + TN)(FP + TN)]/T}{T - [(TP + FN)(TP + FP) + (FN + TN)(FP + TN)]/T}$
F-score	$2 \frac{PPV \cdot TPR}{PPV + TPR} = \frac{2TP}{2TP + FP + FN}$	-	-

Table 5 Performance metrics calculated for each case study

Country	Subject	Model	Modelling step	Efficiency (accuracy)	True positive rate (TPR)	False positive rate (FPR)	Threat score	Equitable threat score	Hedke skill score	Odds ratio	Odd ratio skill score
Australia	Drought risk mapping	Fuzzy function: 50% cutoff	Validation	0.625	0.580	0.222	0.545	0.142	0.25	4.8462	0.657
		Fuzzy function: 70% cutoff		0.85	0.818	0.111	0.75	0.538	0.7	36	0.945
		Fuzzy function: 90% cutoff		0.625	1	0.428	0.25	0.142	0.25	0	1
Iran	Flood inundation mapping	EBF	Training	0.808	0.891	0.245	0.647	0.446	0.617	25.33	0.924
			Validation	0.718	0.769	0.315	0.526	0.28	0.437	7.22	0.756
USA	Distribution of soil organic matters	DAT	Validation	0.442	0.431	0	0.431	0.014	0.028	0	1
		ANN	Validation	0.730	0.625	0.1	0.588	0.315	0.48	15	0.875
Italy	Gully susceptibility mapping	MARS	Training	0.970	0.963	0.022	0.942	0.888	0.940	1151	0.998
			Validation	0.976	0.970	0.016	0.954	0.910	0.953	1885	0.998
		GLM	Training	0.656	0.592	0	0.592	0.185	0.312	0	1
			Validation	0.674	0.605	0	0.605	0.211	0.348	0	1
Vietnam	Landslide susceptibility mapping	MaxEnt	Validation	0.601	0.556	0	0.556	0.112	0.202	0	1
		BayGmmKda		0.739	0.731	0.2521	0.592	0.314	0.478	8.08	0.779

Table 5 (continued)

Country	Subject	Model	Modelling step	True skill statistic	Cohen's kappa	True negative rate (TNR)	False negative rate (miss rate)	Misclassification rate	Positive predictive value (PPV)	False discovery rate (FDR)	Negative predictive value (NPV)
Australia	Drought risk mapping	Fuzzy function: 50% cutoff	Validation	0.358	0.25	0.778	0.419	0.375	0.900	0.100	0.350
		Fuzzy function: 70% cutoff		0.707	0.7	0.889	0.182	0.150	0.900	0.100	0.800
		Fuzzy function: 90% cutoff		0.571	0.25	0.571	0.000	0.375	0.250	0.750	1.000
Iran	Flood inundation mapping	EBF	Training	0.646	0.617	0.754	0.108	0.192	0.702	0.298	0.915
			Validation	0.453	0.437	0.684	0.231	0.281	0.625	0.375	0.813
USA	Predictive distribution of soil bulk density	DAT	Validation	0.431	0.028	1.00	0.569	0.558	1.000	0.000	0.033
		ANN	Validation	0.525	0.48	0.90	0.375	0.269	0.909	0.091	0.600
Italy	Gully susceptibility mapping	MARS	Training	0.941	0.940	0.978	0.037	0.030	0.978	0.022	0.963
			Validation	0.953	0.953	0.983	0.030	0.024	0.983	0.017	0.970
		GLM	Training	0.592	0.312	1.000	0.407	0.344	1.000	0.000	0.313
			Validation	0.605	0.348	1.000	0.394	0.326	1.000	0.000	0.349
Vietnam	Landslide susceptibility mapping	MaxEnt	Validation	0.556	0.202	1.000	0.444	0.399	1.000	0.000	0.203
		BayGmmKda		0.479	0.478	0.748	0.269	0.261	0.757	0.243	0.722

Table 5 (continued)

Country	Subject	Model	Modelling step	False omission rate (FOR)	F-score	Matthews correlation coefficient (MCC)	Informedness (Bookmaker informedness; BM)	Markedness (MK)	AUROC	AUSRC	AUPRC
Australia	Drought risk mapping	Fuzzy function: 50% cutoff	Validation	0.650	0.706	0.299	0.358	0.250	0.873	-	74.400
		Fuzzy function: 70% cutoff		0.200	0.857	0.704	0.707	0.700	0.873	74.400	
		Fuzzy function: 90% cutoff		0.000	0.400	0.378	0.571	0.250	0.873	74.400	
Iran	Flood inundation mapping	EBF	Training	0.085	0.786	0.632	0.646	0.617	0.866	79.710	-
			Validation	0.188	0.690	0.445	0.453	0.438	0.787	-	75.209
USA	Predictive distribution of soil bulk density	DAT	Validation	0.967	0.603	0.120	0.431	0.033	0.839	-	77.620
		ANN	Validation	0.400	0.741	0.517	0.525	0.509	0.879	-	79.630
Italy	Gully susceptibility mapping	MARS	Training	0.037	0.971	0.941	0.941	0.941	0.992	99.141	-
			Validation	0.030	0.977	0.953	0.953	0.953	0.995	-	99.285
		GLM	Training	0.687	0.744	0.430	0.593	0.313	0.987	97.134	-
			Validation	0.651	0.754	0.460	0.606	0.349	0.992	-	97.542
Vietnam	Landslide susceptibility mapping	MaxEnt	Validation	0.797	0.715	0.336	0.556	0.203	0.889	-	0.855
		BayGmmKda		0.278	0.744	0.479	0.479	0.479	0.819	-	69.460

Table 6 Opposing performance metrics for Vietnam's case study

ROC-accordant	ROC-dissordant
Informedness	Markedness
PPV	MCC
TNR	NPV
TSS	Misclassification rate
1-Specificity	FNR
FDR	Cohen's Kappa
	F-score
	Hedke skill score
	Equitable threat score
	Threat score
	Sensitivity
	Accuracy
	FOR

Table 7 Comparing confusion matrix variants of MaxEnt and BayGmmKda models as implemented in Vietnam

Observed	Models	
	MaxEnt	BayGmmKda
TN	330	1175
TP	1627	1231
FN	1297	452
FP	0	396

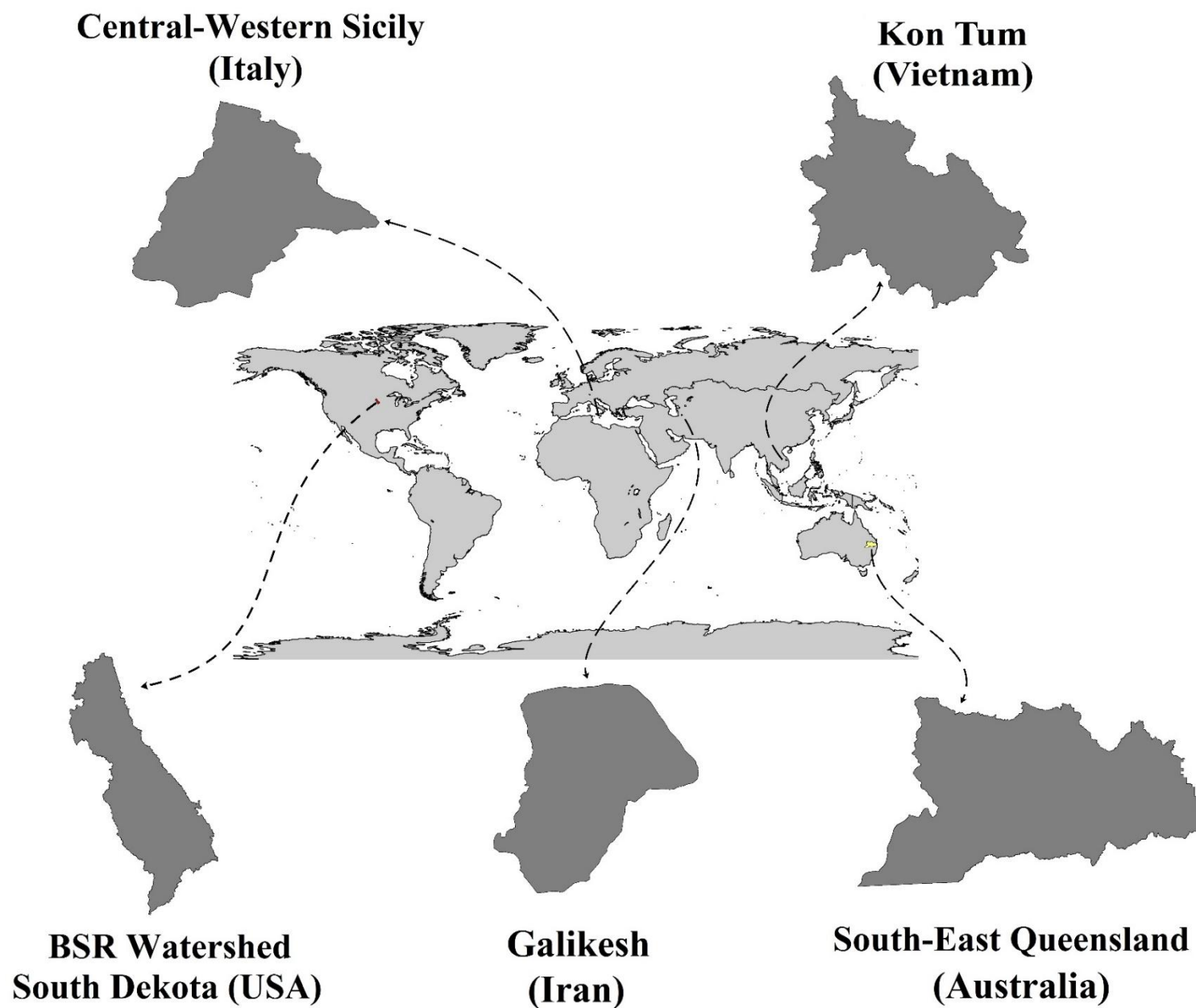


Fig. 1

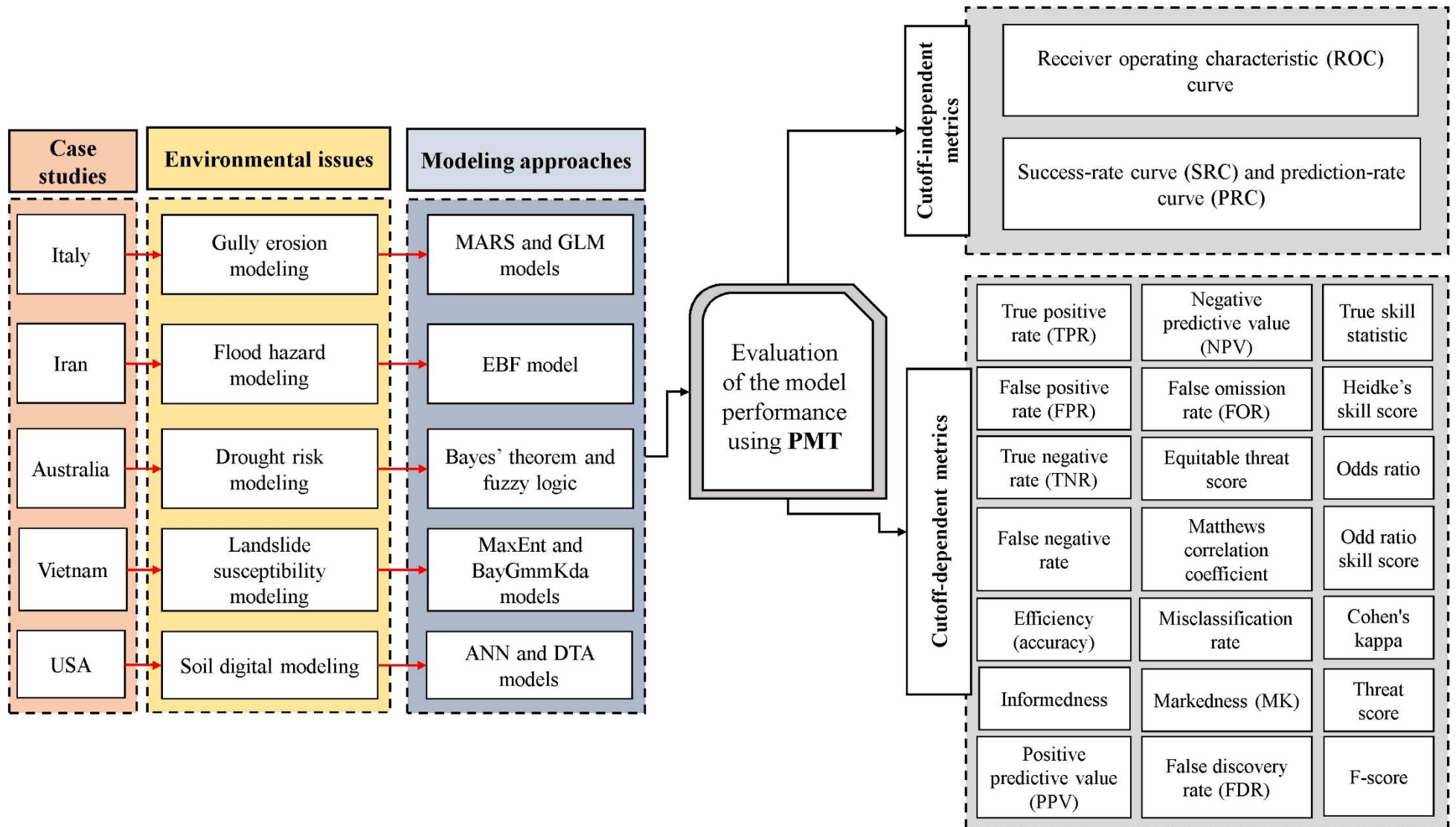


Fig. 2

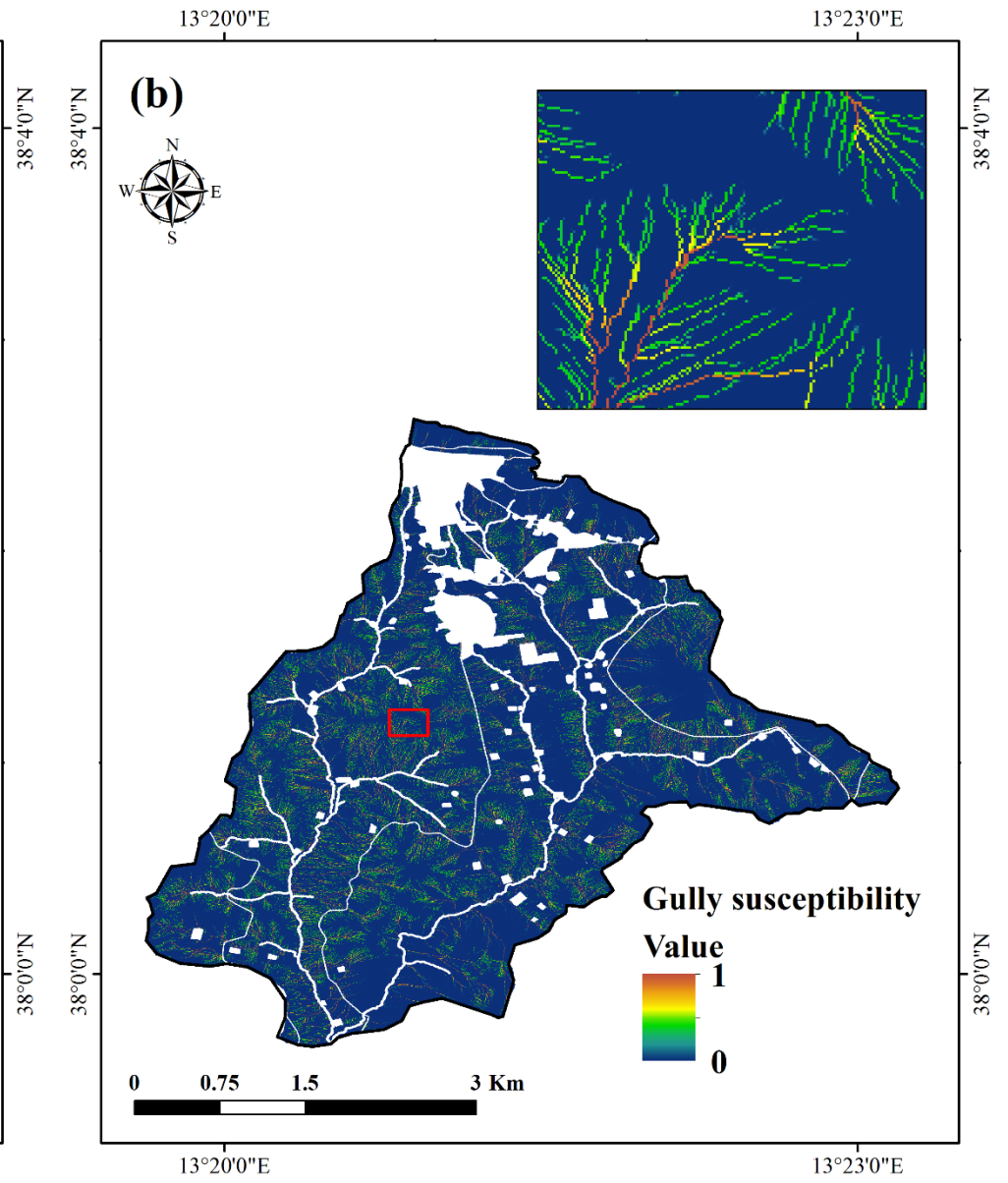
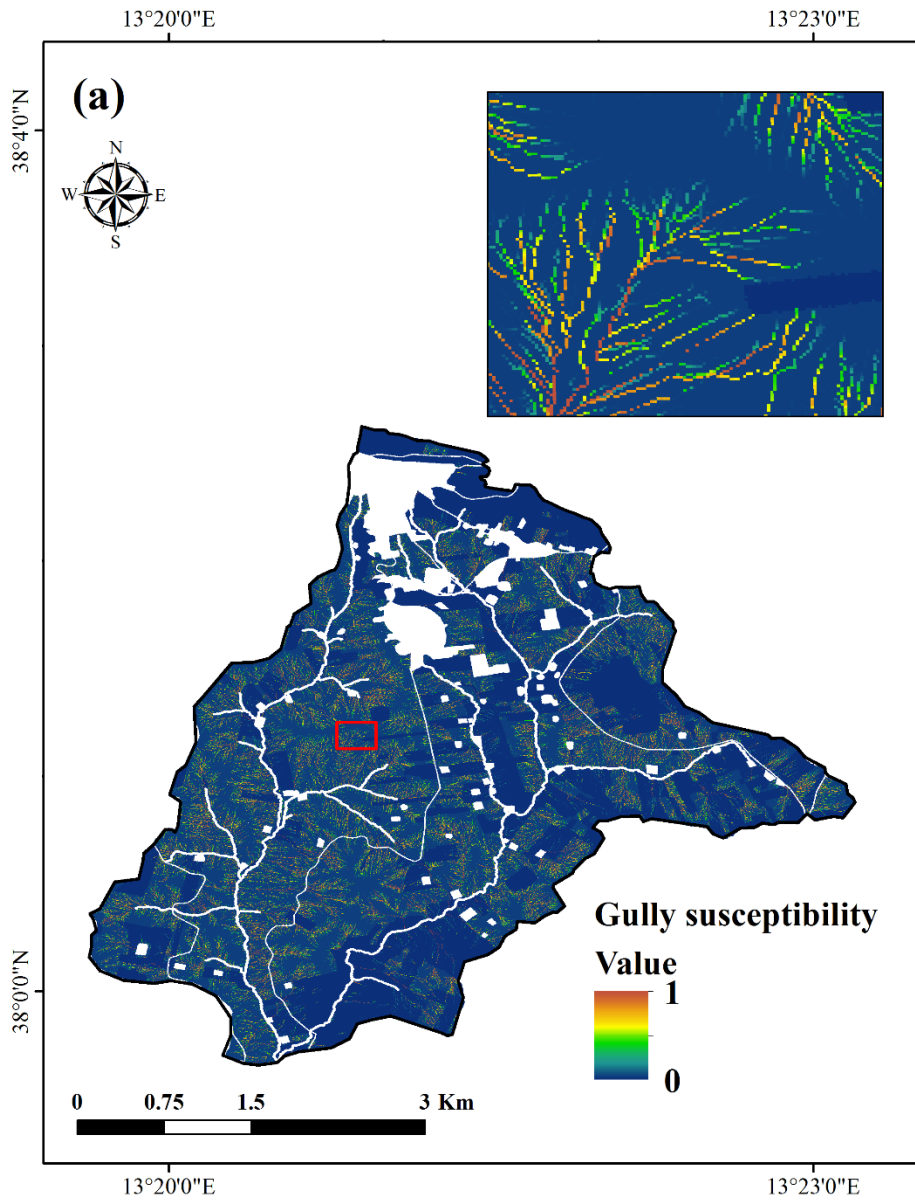


Fig. 3

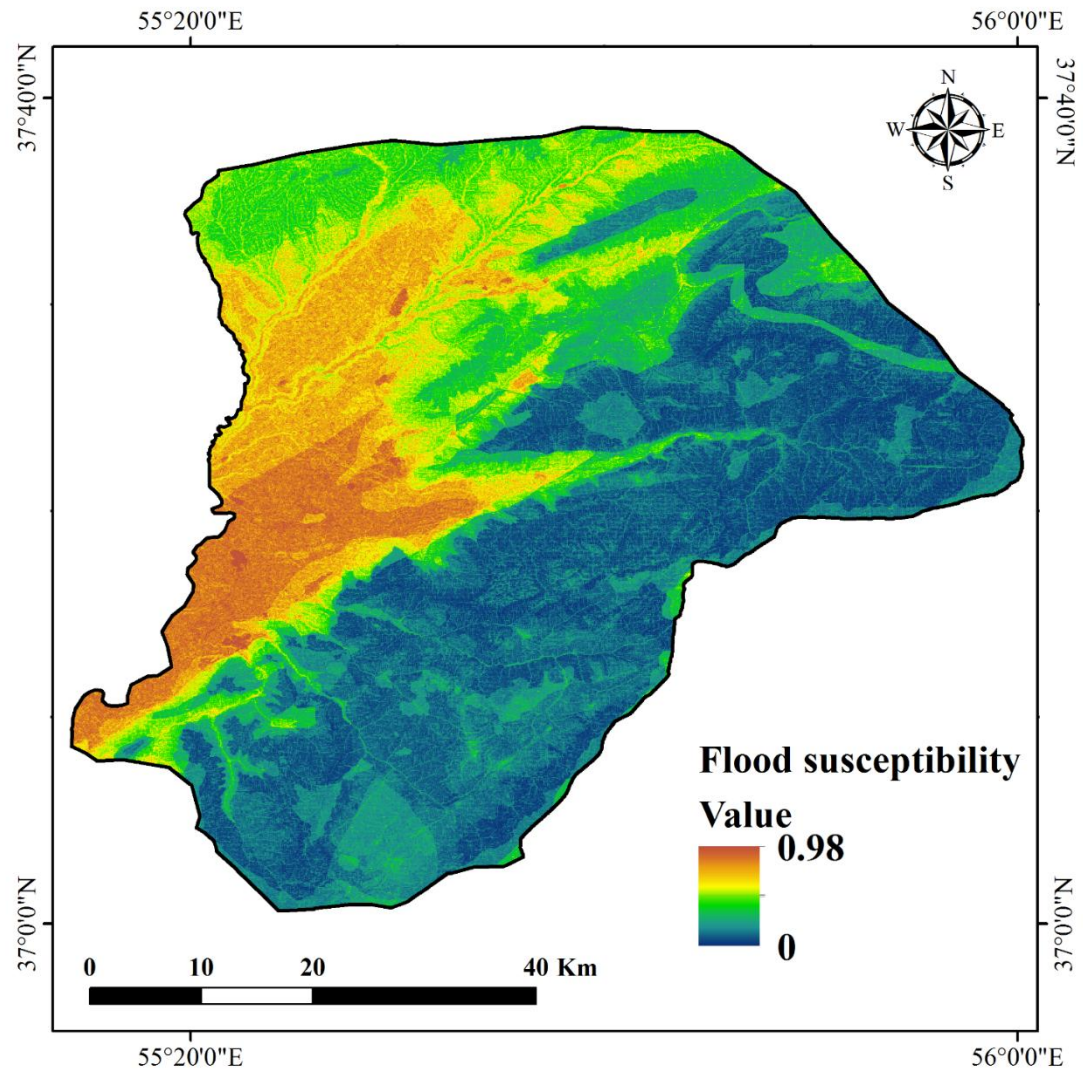


Fig. 4

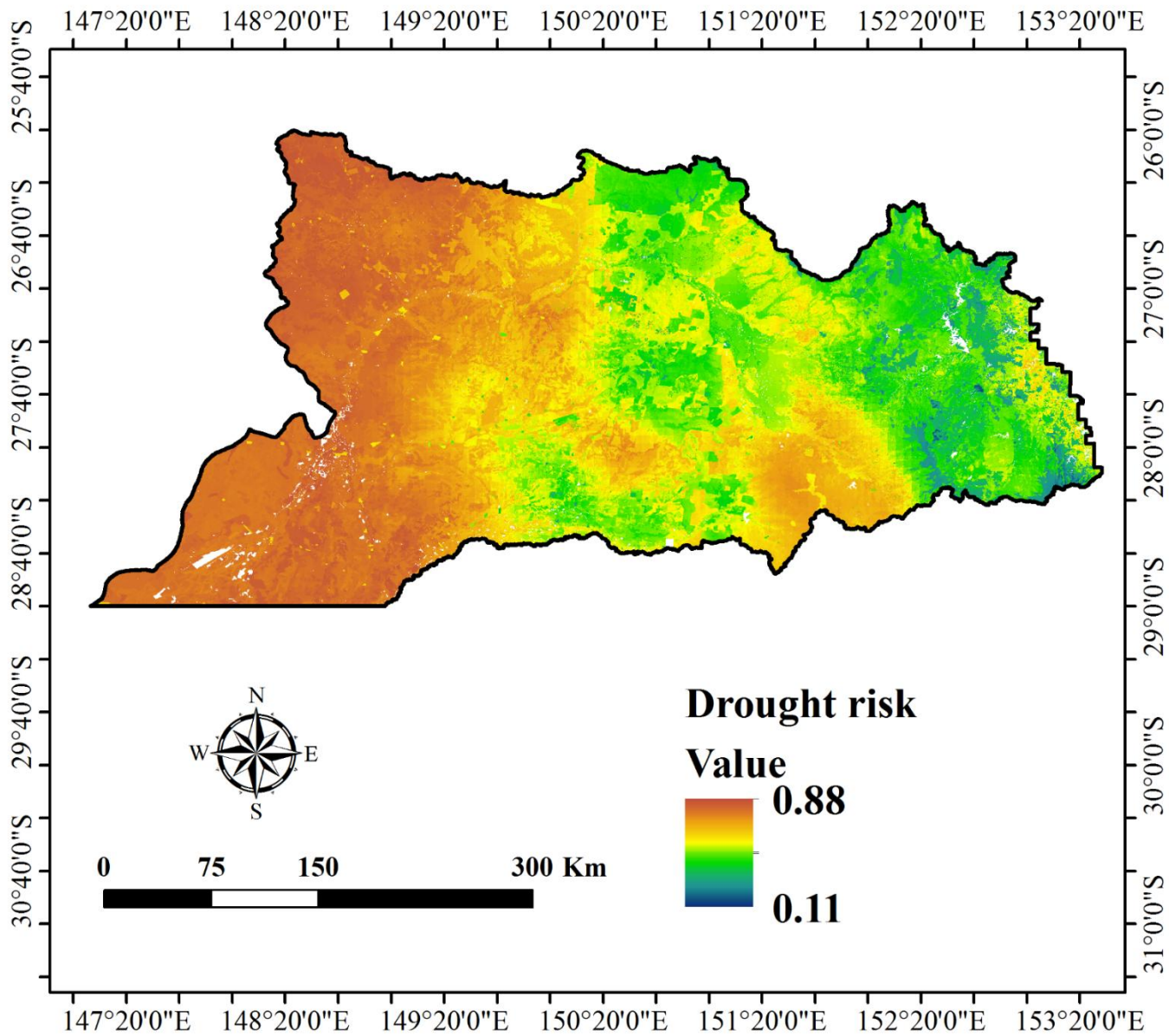


Fig. 5

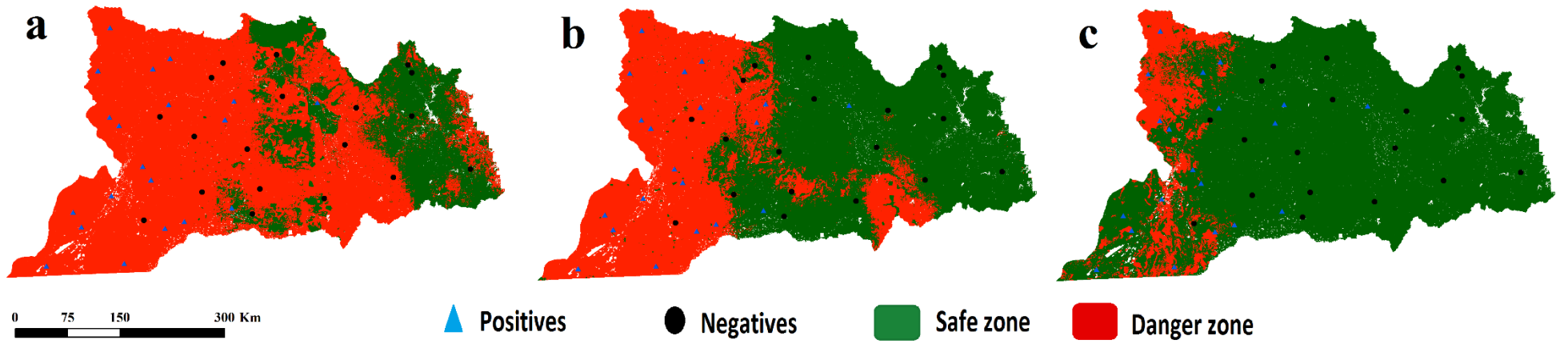


Fig. 6

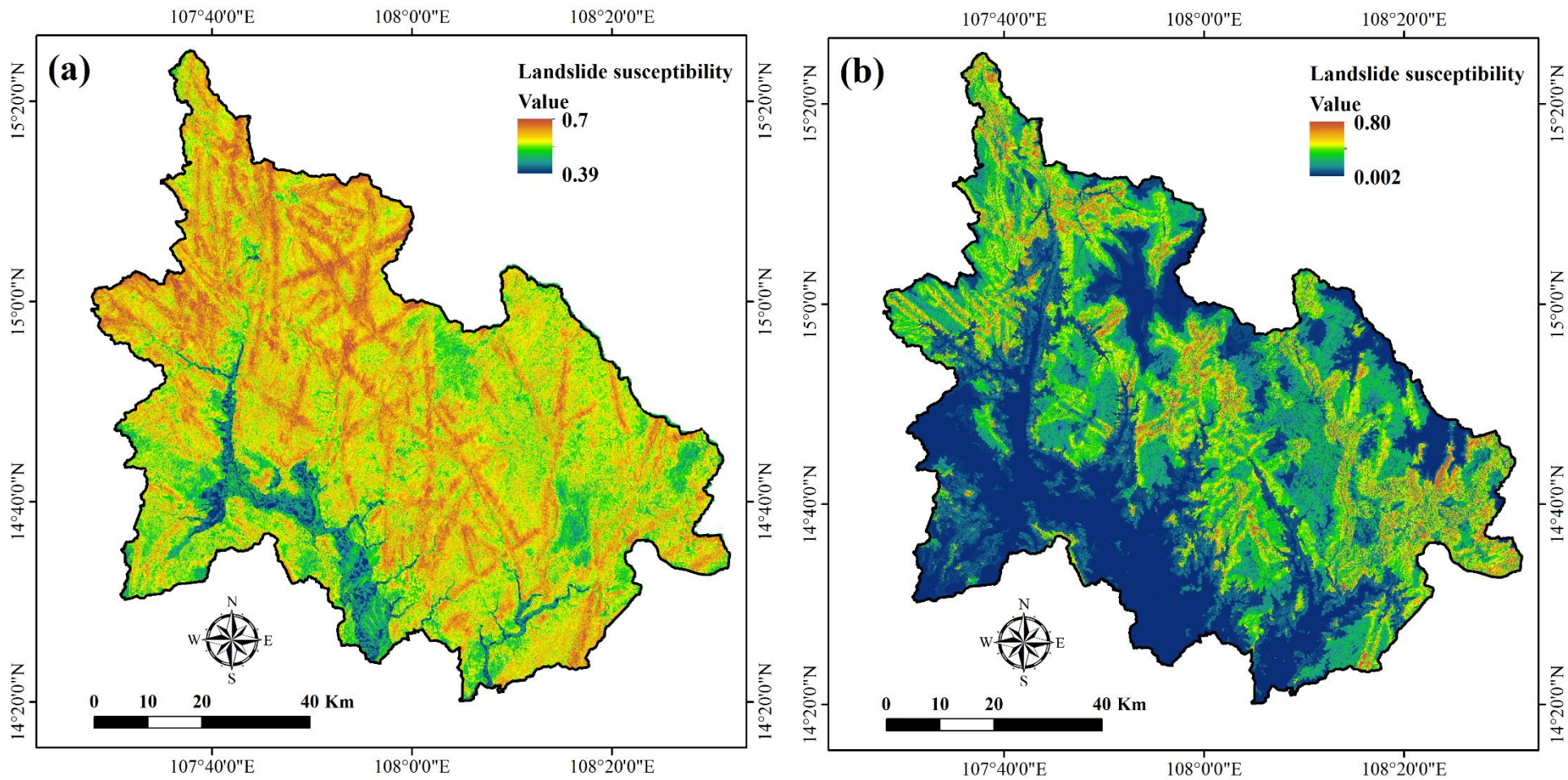


Fig. 7

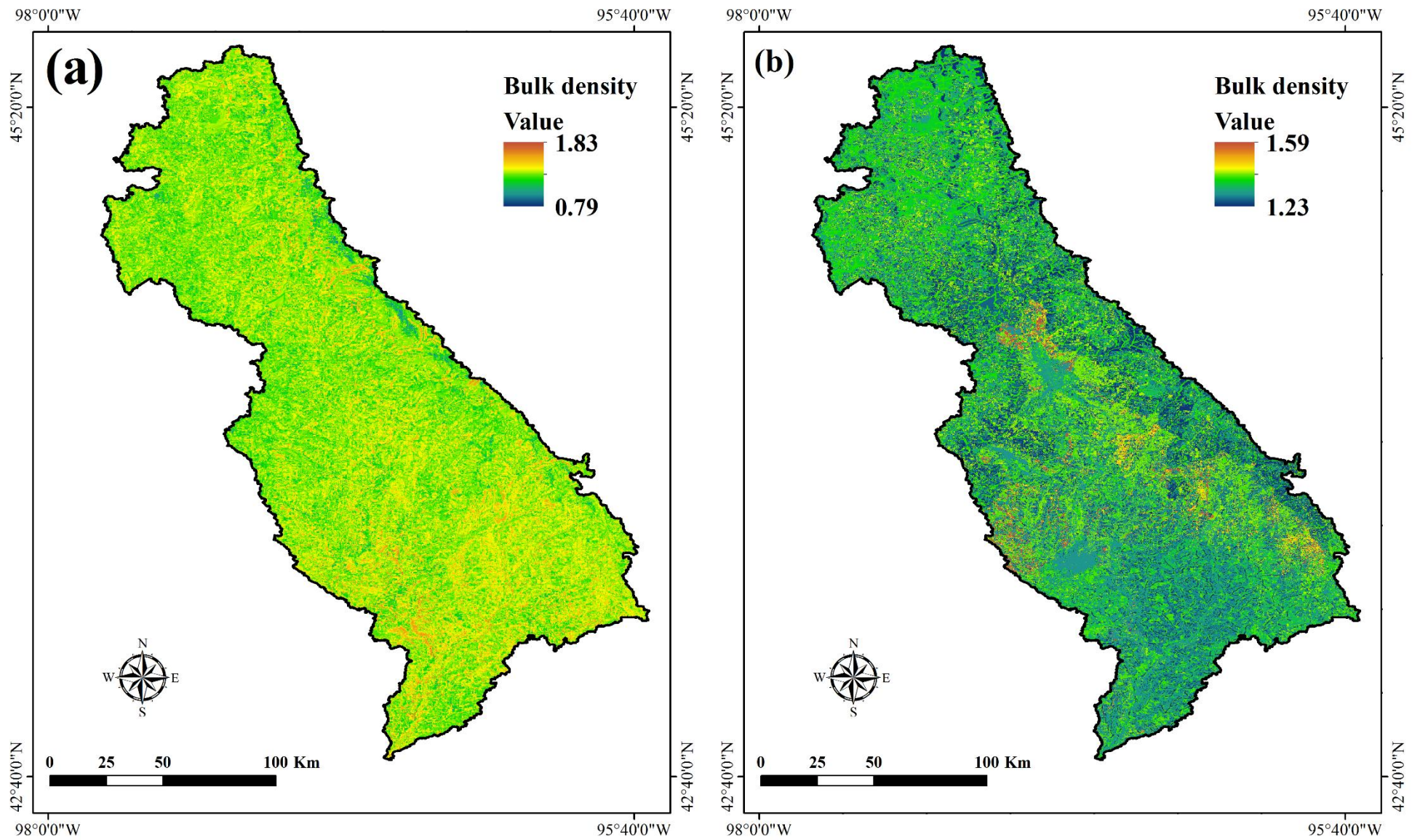


Fig. 8