

**Erratum: Atom-field dressed states in slow-light waveguide QED [Phys. Rev. A **93**, 033833 (2016)]**

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In Sec. V of our original paper we have introduced the nonlinearity parameter

$$\Delta_{\text{nl}}(N_e) = \frac{|N_e E_-^{(1)} - E_-^{(N_e)}|}{g|N_e - \sqrt{N_e}|}. \quad (1)$$

This parameter was then plotted in Fig. 9 for  $N_e = 2$  and the detunings  $\delta = 0$ ,  $\delta = 2J$ , and  $\delta = 3J$ . In all three cases the nonlinearity goes rapidly to zero for  $g \lesssim J$ . Although these results are correct, the plot shows only the nonlinearity parameters for the mostly photonlike states with  $\delta = 2J$  and  $\delta = 3J$ , instead of the more relevant cases of the fully hybridized state at the band edge with  $\delta = -2J$  or the atomlike state inside the band gap with  $\delta = -3J$ .

In Fig. 1 we show again the same plot of the nonlinearity parameter, but now including the cases  $\delta = -2J$  and  $\delta = -3J$  (we recall that in Fig. 9 we focus on the lowest dressed state). It can be seen that although for  $\delta = -2J$  the nonlinearity (compared to the Jaynes-Cummings nonlinearity) vanishes at small  $g$ , it is still much stronger than for the resonant case  $\delta = 0$ . This is consistent with the observation that for  $\delta = -2J$  the wavelength of the second photon,  $\lambda_2$ , can be much larger than the wavelength of the first bound photon,  $\lambda_1$  (see discussion in Sec. V C in the original paper). In contrast, for  $\delta = 0$  one finds  $\lambda_1 \approx \lambda_2$ . Note that the approximate scaling of the nonlinearity parameter for  $g \rightarrow 0$  can be understood from the simplified assumption  $E_-^{(2)} \approx E_-^{(1)} - 2J$ , which would correspond to a single-photon bound state plus an additional very loosely bound photon at the band edge. By recalling that  $E_-^{(1)} \simeq -2J - [g^4/(4J)]^{1/3}$  [see Eq. (27) in the original paper], we obtain  $\Delta_{\text{nl}}(2) \sim \sqrt[3]{g}$ .

For  $\delta = -3J$ , which for  $g \rightarrow 0$  corresponds to an atomlike state inside the band gap, the nonlinearity parameter diverges. Note that this divergence is a consequence of the chosen normalization for  $\Delta_{\text{nl}}(N_e)$  and can again be understood from the approximation  $E_-^{(2)} \simeq \delta - 2J$  for small  $g$ .

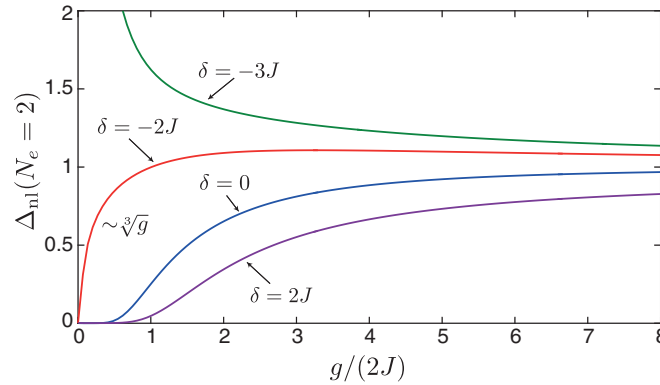


FIG. 1. Nonlinearity parameter  $\Delta_{\text{nl}}(N_e)$  as defined in Eq. (1) is plotted for  $N_e = 2$  and different atom-photon detunings  $\delta$ .