

Advanced modeling and energy-saving-oriented assessment of control strategies for air-cooled chillers in space cooling applications

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Abstract

Chillers are reference technologies to meet the demand for space cooling in the tertiary and commercial sectors. Meantime, being power-to-cold technologies, they could increase the flexibility of these buildings in those contexts of a high share of electricity from renewable energy sources through new control strategies. To reliably assess the achievable energy savings in these novel applications, models capable of simulating not only the steady-state operation but also the dynamic response are required. However, the operation of these systems is usually evaluated through highly simplified models, also omitting controls. To fill this gap, this paper proposes an integrated thermodynamic and control modeling for an air-cooled chiller, accounting for usual and innovative control strategies. To show the capabilities of the model, an air-cooled chiller serving an office in the Mediterranean area is assumed. Both a variable-speed chiller and a constant-speed chiller with sequential control for compressors are simulated. Results show that for a variable-speed chiller, the set point for the supplied cold water is met, and the thermal inertia of the hydronic loop affects the reaching of the steady-state operation. In the case of a constant-speed chiller with sequential control, the number of “ON-OFF” cycles for each compressor is monitored and the minimum inertia of the hydronic loop for the safe operation of compressors is found. The analysis reveals that a variable temperature setpoint for the supplied water allows for a percentage increase in the energy performance between 10.8%-60.3%. The proposed model enables the analysis of innovative controls aimed at improving energy savings and increasing building flexibility.

Keywords

Energy savings, air conditioning, space cooling, air-cooled chiller, thermodynamic modeling, control strategy, dynamic response.

1. Introduction

In 2021 space cooling accounted for nearly 16% of the building sector's final electricity consumption [1]. This share is expected to increase in the near future as climate change and population growth will push the demand for cooling [2]. The use of electricity from renewable energy sources (RES) together with the adoption of high-performance air-conditioning systems could limit the environmental effects of such an increase [3]. Focusing on air-conditioning systems, air-cooled and water-cooled chillers are widely adopted to meet the cooling demand in the tertiary and commercial sectors. To achieve higher energy savings, in the last two decades, traditional constant-speed systems have been gradually

38 replaced by variable-speed technologies [4]. To further improve the energy and environmental
39 performance, heat exchanger design has been improved [5], scroll compressors have gradually
40 replaced reciprocating compressors [6], and new refrigerants with low global warming potential have
41 been developed [7].

42 In addition to technological improvements, research has devoted great efforts to increasing the energy
43 performance of these systems when operating in buildings. In this respect, several studies have
44 proposed deterministic or stochastic approaches to determine optimal and robust operating strategies.
45 For instance, Niu et al. [8] proposed a genetic algorithm to optimize the setpoint for water-cooled
46 chillers in Shanghai (China). The results showed an 8.5% increase in energy savings. Chan et al. [9]
47 used an artificial neural network together with particle swarm optimization to operate a chiller plant
48 serving a hospital. The neural network predicted the outdoor temperature and building cooling
49 demand, while the particle swarm optimization aimed at finding the optimal value setpoints for chilled
50 water supply temperature. The author estimated an 8.6% increase in energy performance compared
51 with the traditional control strategy. Catrini et al. [10] proposed exergoeconomics to optimize both
52 the energy and economic performances of multiple air-cooled chillers. The minimum unit cost of the
53 chilled water was achieved in the case of unevenly sized chillers. Saloux and Zang [11] developed a
54 data-driven model-based control to vary the supply water temperature setpoint for a water-cooled
55 chiller. The results pointed out a 33% reduction in electric energy consumption. Fan and Zhou [12]
56 proposed a model-based predictive control to optimize the operation of water-cooled chiller plants
57 with a water-side economizer. The authors estimated a 14.3% decrease in energy consumption
58 compared to conventional control. Ismaen et al. [13] optimized the design and operation of multiple
59 chillers in a district cooling network through multiple integer linear optimization, while considering
60 chiller short-cycling and the unloading conditions. Zhang et al. [14] simulated the operation of an air-
61 cooled chiller for cooling in data centers, and the relation among the power consumption with
62 return water temperature, ambient temperature, and the water flow rate was investigated to minimize
63 energy consumption. Qiu et al. [15] proposed a hybrid model-free chilled water temperature to reset
64 the supply cold water temperature method for chillers is proposed. The method relied only on
65 reinforcement learning techniques without needing preliminary modeling of components. The authors
66 claimed that the approach could be a useful alternative for systems without sufficient data due to its
67 online self-learning capability. Liu et al. [16] proposed a method for optimizing the operation of
68 chillers in the presence of uncertainties in cooling demand by using a Markov chain. Results showed
69 that confidence in the method could be increased by 56.7%. Sun et al. [17] developed a method based
70 on the Monte Carlo technique to reduce the impacts of flow measurement uncertainties in the case of
71 multiple chillers sequencing control. Alghamdi et al. [18] found that a proportional-integral-

72 derivative controller for a chiller with five temperature setpoints allowed for only a 2.2% increase in
73 energy savings. Yu and Chan [19] proposed a method for determining optimum condensing
74 temperature and variable chilled water flow for the case of air-cooled centrifugal chillers. Liao et al.
75 [20] evaluated the robustness of typical chiller sequencing controls in the presence of uncertainties.
76 The analysis revealed that some control strategies could contribute to the worsening of uncertainty
77 levels.

78 Other research studies focused on developing advanced supervisory controls for chillers (and other
79 cooling systems) to increase the so-called “building flexibility” (i.e., the capability of the building to
80 adapt its operations not only to meet the needs of the occupants but also to help power grid operators
81 in managing hours of high demand or surplus of electricity production from RES) [21]. In this respect,
82 it is widely recognized that electrically driven cooling (and heating) systems could support the
83 management of the power grid in the context of the high share of RES [22]. Indeed, by being activated
84 in the presence of an electricity surplus, the produced cold can be stored onsite [23] or sold to a
85 cooling network [24]. Moreover, by adopting demand-response strategies [25], loads of the served
86 building could be shifted from peak to off-peak periods thus reducing stress on the power grid caused
87 by high demand. For instance, Tina et al. [26] investigated the capability of commercial buildings in
88 providing flexibility to help power grid operators. A Mediterranean shopping center served by a vapor
89 compression system was assumed as a case study. The authors found that a large flexibility potential
90 exists throughout the year, although occupants' discomfort could arise during summer. Lu et al. [27]
91 investigated the achievable flexibility thanks to the integrated operation of cooling systems and
92 building thermal mass in the case of nearly zero-energy office buildings. Compared with the
93 traditional night set-back control, the peak demand can be reduced by about 55%. Mugnini et al. [28]
94 evaluated the operational flexibility of the common residential space cooling technologies, paying
95 particular attention to the distribution system. Results show that split systems show lower flexibility,
96 whereas promising results could be achieved in the case of hydronic cooling systems. Triolo et al.
97 [29] estimated cooling demand flexibility in a district energy system equipped with chillers achieved
98 by using temperature set point changes. The authors estimated a 13.5% decrease in the demand in the
99 case of a 1.1 °C setpoint increase.

100 In general, from the previous literature analysis, it was observed that some of the published papers
101 usually relied on very simplified modeling of chillers [14],[13]. Some of them adopt performance
102 data available from catalogs, corrected to account for the coefficient of performance variation in off-
103 design conditions [12],[20]. Others, on the contrary, put forth an experimental campaign to map the
104 system's performance, without providing insights into the action of the embedded controls [11].

105 Finally, other papers performed detailed thermodynamic modeling of the systems, without any focus
106 on the chillers' embedded controls [10].

107 Considering the interest of research in optimizing chillers' energy performance and in investigating
108 their potential role in improving buildings' flexibility, the provision of modeling grounded on a
109 detailed thermodynamic basis and architecture control is of paramount importance to achieve more
110 reliable results. Indeed, the developed models should provide insights into (i) the ability of the
111 systems to quickly respond to the variation in the cooling (or heating) demand of the users (e.g.,
112 buildings or cooling network); (ii) the capability to adapt to the variation in the electricity produced
113 by local RES while accounting for limits of the electric motor and the embedded controller, and (iii)
114 the possibility to compare new control strategies aimed at improving the overall energy performance
115 or to change operation according to ancillary services required by grid operators. Only a few papers
116 have addressed some of these aspects [30]-[31]. For instance, Liu et al. [30] highlighted that when
117 cooling systems are used for fast load balancing, the drastic changes in the compressor speed can
118 cause severe superheat regulation issues including oscillations and even wet compression. Maier et
119 al. [32] proposed a piecewise linear model based on simulation results and a quadratic modeling
120 approach air-source heat pump while considering the supply temperature as a control variable. Both
121 models were compared to a simplified linear model, which was found to underestimate operating
122 costs. Clauß and Georges [31] investigated the influence of the modeling of the vapor compression
123 systems control in the context of demand response. The authors compared different controls (e.g.,
124 proportional, continuous, etc.) and they demonstrated that the modeling complexity of the system
125 control has a significant impact on the key performance indicators, proving that this aspect should
126 not be overlooked. For instance, for short time operation, the modeling of the heat pump controller
127 and the transient effects of the heat pump, such as cycling losses during start-up, are important.

128 To cover this knowledge gap, this paper proposes an integrated thermodynamic and control modeling
129 of an air-cooled chiller. The thermodynamic modeling is first developed by relying on simulation
130 data obtained using software where detailed analysis of heat exchanger and compressor operation is
131 performed [33]. Regarding the induction motor, a full-scale state-space model is built, and the
132 implementation of a variable speed drive is also carried out. Two architecture controls aimed at
133 modulating the delivered cooling capacity are also presented. All the developed models are then
134 jointly solved by using MATLAB Simulink [34]. By using the proposed model, the following aspects
135 could be addressed:

- 136 - the comparison of different strategies for modulating the capacity delivered by chillers, while
137 considering constraints related to the motors and controller. In this case, the following
138 strategies for compressor management are analyzed: (i) a sequential control of multiple

- 139 compressors, which consists of switching “ON” and “OFF” each compressor in the case of
140 changes in user demand; and (ii) a variable-speed control which continuously varies the
141 rotating speed of the compressors, allowing then for a smooth variation in the delivered
142 cooling capacity.
- 143 - the analysis of the effect of the design of the hydronic circuit on the chiller’s dynamic response
144 (e.g., the average time needed by the unit to achieve the steady-state operation) and average
145 energy performance.
 - 146 - the provision of a model for simulating the operation of the chillers in the case of new
147 management strategies aimed at increasing energy savings or building flexibility. In this
148 respect, this paper proposes a supervisory control of the chillers which assumes a variable
149 temperature setpoint of the produced cold water with the outdoor temperature, aimed at
150 increasing energy efficiency and providing ancillary service to the grid.

151 To show the capabilities of the proposed model, an air-cooled chiller serving an office located in
152 Southern Italy is assumed as the case study. Some scenarios will be simulated to account for the
153 control strategies adopted and the effects of hydronic loop inertia. The paper is structured as follows:
154 in the second section, details on the thermodynamic, electromechanical, and control modeling are
155 provided. In the third section, the case study is described together with the simulated scenarios. In the
156 fourth section, results will be presented and discussed, and in the final section, conclusions are briefly
157 drawn.

158 **2. Materials and Method**

159 In this section, the modeling of an air-cooled chiller and the electric motors are presented. Then, a
160 description of the control architecture together with details on implementation is provided.

161 **2.1 Thermodynamic modeling of air-cooled chillers**

162 Figure 1 shows a simplified schematic of an air-cooled chiller to depict the main subcomponents,
163 physical variables, and acronyms widely used in the following. The major components are (i) an air-
164 to-refrigerant heat exchanger (e.g., a tube and fins coil or plate and fins) used as the condenser (CND);
165 (ii) a brazed-plate heat exchanger used as the evaporator (EVP) where water coming from the
166 hydraulic loop at a temperature T_{wr} is cooled down to T_{ws} (iii) an expansion valve (EV); (iv) a
167 compressor (CMP) coupled with an induction motor (IM). As will be explained later, to maintain a
168 desired value of the temperature of the water supplied to the hydronic circuit (T_{ws}), the main controller
169 (CTRL) will act on the electrical motor by regulating the rotating speed of the CMP or cycling it
170 “ON” and “OFF”.

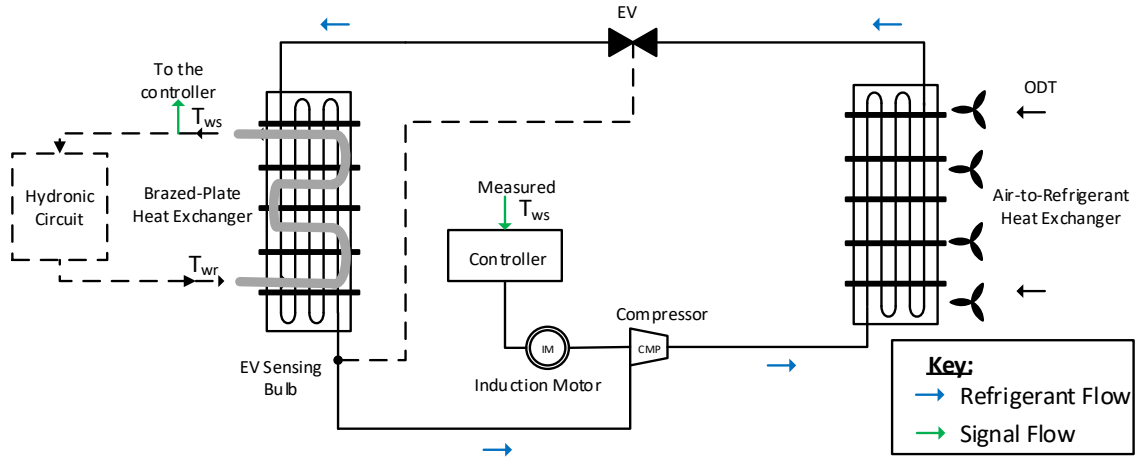


Figure 1. Simplified scheme of an air-cooled chiller.

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173 The cooling capacity delivered (CC) and the mechanical power required by the CMPs (P_m) are
 174 necessary for assessing the energy performance of the chiller. Typically, the CMP rotating speed
 175 (ω_{CMP}), the dry-bulb temperature of the outdoor air (ODT), and the temperature of the water returning
 176 from the hydronic circuit and entering the evaporator (T_{wr}) are the variables that mostly influence the
 177 system performance, at given design and refrigerant charge [35]. It is then useful to develop ad-hoc
 178 equations like the ones shown in Eqs 1.a-b, where CC and P_m can be directly calculated in any
 179 operating conditions from the selected independent variables (typically available from measurement).

$$CC = f(\omega_{CMP}, ODT, T_{wr}) \quad (1.a)$$

$$P_m = g(\omega_{CMP}, ODT, T_{wr}) \quad (1.b)$$

180 However, to develop Eqs 1.a-b, a preliminary mapping of chiller behavior in a wide range of operating
 181 conditions is due. To this purpose, as it will be shown in Subsection 3.1, ad-hoc experimental
 182 campaigns or accurate plant simulations have to be performed. In this paper, Eqs 1.a-b are then
 183 formulated as shown in Eqs 2.a-b (more details about the accuracy of this assumption are provided
 184 in Subsection 3.1).

$$CC = L_1 \omega_{CMP} + L_2 ODT + L_3 T_{wr} \quad (2.a)$$

$$P_m = K_1 \omega_{CMP} + K_2 ODT + K_3 T_{wr} \quad (2.b)$$

185 In Eqs 2.a-b, K_i and L_i are fitting coefficients that can be found by applying numerical methods to the
 186 developed dataset.

187 The temperature of the water entering the EVP, i.e., T_{wr} , is obtained from the dynamic model of the
 188 hydronic circuit served by the chiller. This simplified model [36], sufficiently reliable for the scope
 189 of this paper, is presented in Eq. 3,

$$\frac{dT_{wr}}{dt} = \frac{1}{C_s} (CL - CC) \quad (3)$$

190 where the time variation of T_{wr} is proportional to the difference between the building cooling load
 191 (i.e., CL) and CC . C_s is a coefficient (measured in $\text{kJ}/^\circ\text{C}$) that quantifies the thermal inertia of the
 192 hydronic loop coupled to the chiller. This parameter is highly dependent on the water content in the
 193 hydronic circuit, and its value is usually determined during the design phase of the circuit to assure
 194 the safe operation of the CMPs of the cooling systems. Eqs 4.a-b are used to estimate this quantity.
 195 In particular, Eq. 4.b is also known as the ‘‘Portoso’s Equation’’ [37] which is typically used in Italy
 196 during the design phase of hydronic loops served by chillers [3].

$$C_s = \rho_w c_w V_{des} \quad (4.a)$$

$$V_{des} = \frac{60CC_{nom}}{\rho_w c_w \left(\frac{\Delta T_{wr}}{\Delta \tau}\right)_{ref}} \quad (4.b)$$

197 In Eqs 4.a-b ρ_w is the density of water, c_w is the specific heat capacity of water, and V_{des} is the volume
 198 of water in the hydronic loop, which should be sufficient to guarantee the safe operation of the chiller.
 199 CC_{nom} is the nominal cooling capacity delivered by the chiller at the design condition and $\left(\frac{\Delta T}{\Delta \tau}\right)_{ref}$ is
 200 the maximum variation of the water return temperature from the hydronic loop in one minute.
 201 Typically, it is assumed to be equal to $5^\circ\text{C}/\text{min}$ [37]. This value was derived from observation in the
 202 field. The temperature of the water supplied to the building (T_{ws}) is simply computed by the energy
 203 balance shown in Eq. 5,

$$T_{ws} = T_{wr} - \frac{CC}{\dot{m}_w c_w} \quad (5)$$

204 where \dot{m}_w is the mass flow rate of water circulating in the hydronic loop. The mass flow rate of water
 205 is constant throughout the operational period. Worth noting that T_{ws} is typically assumed as the
 206 controlled variable by the controller.

207 The mechanical load torque T_L required by the CMP is then calculated using Eq. 6, where the factor
 208 $\frac{60}{2\pi}$ is used to covert the CMP rotating speed (ω_{CMP}) from rpm/min to rad/s.

$$T_L = \frac{60 P_m}{2\pi \omega_{CMP}} \quad (6)$$

209 **2.2 State-space model of the induction motor**

210 An IM is used to supply mechanical power to CMP. To model the dynamic response of the IM, a 5th-
 211 order linear state-space model in the stationary reference frame is adopted as detailed in Eq. 7 [38,39]:

$$\frac{d}{dt} \begin{bmatrix} i_s \\ \varphi_r' \end{bmatrix} = A \begin{bmatrix} i_s \\ \varphi_r' \end{bmatrix} + B u_s = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} i_s \\ \varphi_r' \end{bmatrix} + \begin{bmatrix} B_1 \\ B_2 \end{bmatrix} u_s \quad (7)$$

212 In Eq. 7, $\begin{bmatrix} i_s \\ \varphi_r' \end{bmatrix}$ is the vector of state variables, i.e., i_s and φ_r' . In addition, i_s are the stator currents
 213 (i_{sq} and i_{sd}) and φ_r' are the rotor fluxes in direct and quadrature axis (φ_{rd}' and φ_{rq}'). Both vectors are
 214 referred the stationary reference frame of the machine. “A” is a 4x4 compound matrix filled with the
 215 coefficients of the state variables which are summarized in Table 1. u_s is the vector of stator voltages
 216 in direct and quadrature axis, indicated as u_{sq} and u_{sd} respectively. The B vector has the coefficient
 217 of the input variable of the stator voltage u_s , and the elements of this vector are presented in Table 1
 218 as well.

219 **Table 1.** Elements of A and B matrices for the IM state-space model.

$A_{11} = -\left(\frac{R_s}{\sigma L_s} + \frac{1-\sigma}{\sigma T_r}\right)I$	(7.a)	$B_1 = \frac{1}{(\sigma L_s)}I, B_2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$	(7.e)
$A_{22} = -\frac{1}{T_r}I - \omega_r D$	(7.b)	$C = [I \quad 0]$	(7.f)
$A_{12} = \frac{L_m}{\sigma L_s L_r} \left(\frac{1}{T_r}I - \omega_r D\right)$	(7.c)	$I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	(7.g)
$A_{21} = -\frac{1}{\sigma L_s}I$	(7.d)	$D = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$	(7.h)

220
 221 In Table 1, R_s is the stator resistance, L_s is the stator inductance, T_r the rotor time constant, L_r is the
 222 rotor inductance, L_m is the mutual inductance, σ is equal to $(1 - \frac{L_m^2}{L_s L_r})$. C , I and, D are matrices used
 223 to present the equations in the direct and quadrature axis.

224 From the states obtained by solving Eq. 7, the electromagnetic torque of the IM, i.e., T_{el} is then
 225 evaluated by using Eq. 8, where p is the number of pair poles. Mechanical dynamic is then presented
 226 in Eq. 9, where the resulting output is the mechanical speed or also referred to as the CMP speed
 227 ω_{CMP} . Note that, the mechanical torque required by the chiller, which was previously indicated as T_L ,
 228 is given by Eq. 6, where J is the inertia of the rotor and μ is the viscosity friction of the rotor.

$$T_{el} = 1.5p(i_{sq} \varphi_{rd}' - i_{sd} \varphi_{rq}') \quad (8)$$

$$J \frac{d\omega_{CMP}}{dt} + \mu \omega_{CMP} = T_{el} - T_L \quad (9)$$

229

230 **2.3 Description and modeling of the chiller’s control architecture**

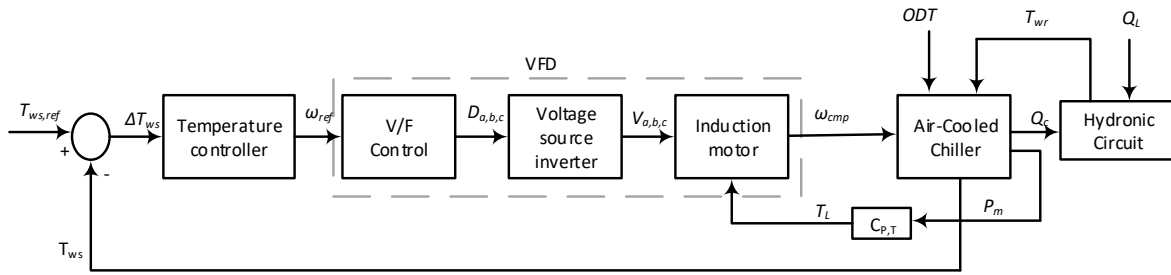
231 Air-cooled chillers could be equipped with constant-speed or with variable-speed CMPs. From a
232 survey of several commercial catalogs, chillers with a nominal cooling capacity of less than 60 kW_c
233 are typically equipped with CMPs with a variable speed drive (VFD), and the CMP rotating speed is
234 varied to meet a desired supply water temperature setpoint ($T_{ws,ref}$). Conversely, for larger units,
235 multiple constant-speed CMPs are used, and an “ON-OFF” control strategy is followed to vary the
236 delivered capacity according to some signal from local thermostats. In the next subsections, a
237 description of the control architectures is provided together with details on the modeling.

238 *2.3.1 Control architecture for variable-speed air-cooled chillers*

239 In Figure 2, the control architecture for a variable-speed air-cooled chiller is shown. In this case, the
240 CMP rotating speed (provided by the IM) is modulated through the action of the VFD (indicated by
241 the grey-dotted box). A scaler control is used inside the VFD. The main reason for implementing
242 scalar control over other advanced control methods such as Field-Oriented Control or Direct-Torque
243 Control is the simplicity of implementing the control technique in software and hardware. As a result,
244 the overall cost is also minimized since the controller can be realized using a low-cost microprocessor.
245 Secondly, the reason to deploy advanced control methods is that scalar control operation is poor at
246 low speeds. For this application, the IM is operational only at high speeds, and the usage is justified.
247 The scaler control uses a simple “voltage over frequency V/F” technique to control an IM at variable
248 speeds. More details on scaler control are provided in [39]. As shown in Fig. 2, a proportional and
249 integral (PI) temperature controller provides a reference value of speed for the V/F control (i.e., ω_{ref})
250 based on the difference between the measured supply water temperature and the desired value (i.e.,
251 ΔT_{ws}). Then, based on ω_{ref} value, the V/F control provides the duty cycles, $D_{a,b,c}$ for each of the
252 inverter switching devices. Space vector modulation (SVM) is used to acquire the duty cycles for
253 each of the inverter switching devices. Finally, the Voltage Source Inverter (VSI) provides the three-
254 phase voltage $V_{a,b,c}$ input to the IM.

255 In the “air-cooled chiller” block, the thermodynamic model of the chiller (see subsection 2.1) is
256 implemented. The overall architecture can be solved in software, such as MATLAB Simulink.

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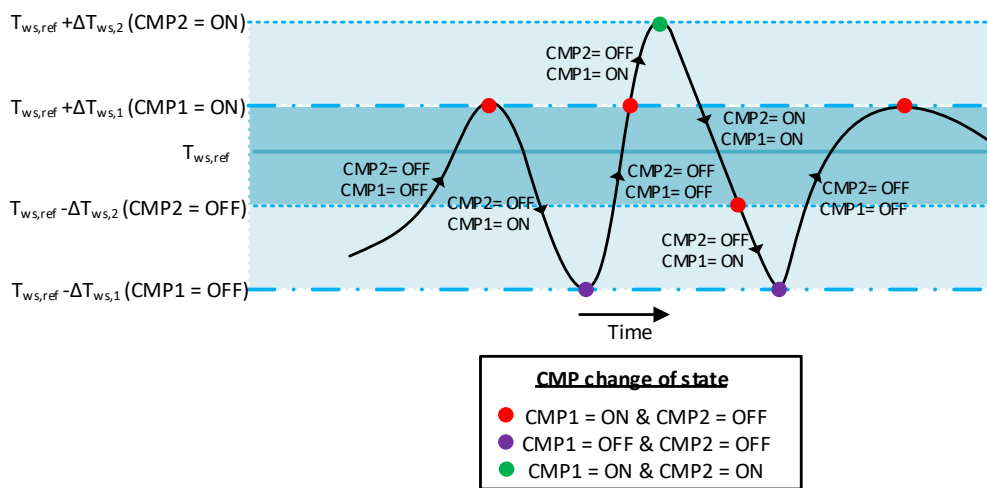


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Figure 2. Architecture control for a variable-speed air-cooled chiller.

260 *2.3.2 Control architecture for constant-speed chillers with multiple compressors*

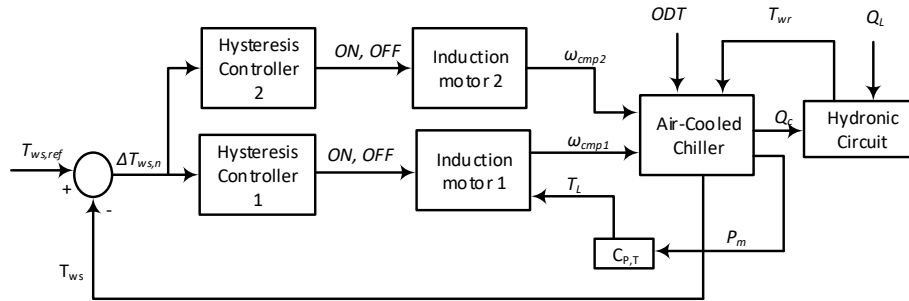
261 A control approach frequently used to modulate the delivered capacity of chillers is to cycle CMPs
 262 “ON-OFF” to maintain the water supply temperature (T_{ws}) around a desired value, as shown in Figure
 263 3. In this case, CMP rotating speed has a unique nominal value, and it is not modulated as in the case of
 264 VFD. If more than one CMP is available, that is a very common practice to guarantee more flexible
 265 modulation of cooling capacity, a logic must be used to coordinate the “ON-OFF” cycle of each of
 266 them. Typically, a sequential approach (or sequential control SC) is adopted. For the sake of clarity,
 267 Figure 3 shows a typical SC in the case of a chiller equipped with two CMPs. The black line represents
 268 the measured value of the water supply temperature. The horizontal blue lines indicated by $T_{ws} \pm$
 269 $\Delta T_{ws,n}$ values represent the temperature threshold values for activating or deactivating each CMP.
 270 Low values for $\pm \Delta T_{ws,n}$ could lead to many “ON-OFF” cycles of each CMPs. Conversely, large
 271 values could lead to high T_{ws} fluctuations. Hence, the values of $\pm \Delta T_{ws,n}$ are selected to assure a
 272 maximum number of “ON-OFF” cycles in an hour, thus increasing the CMPs’ lifetime.



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Figure 3. Sequential control for an air-cooled chiller equipped with two constant-speed CMPs.

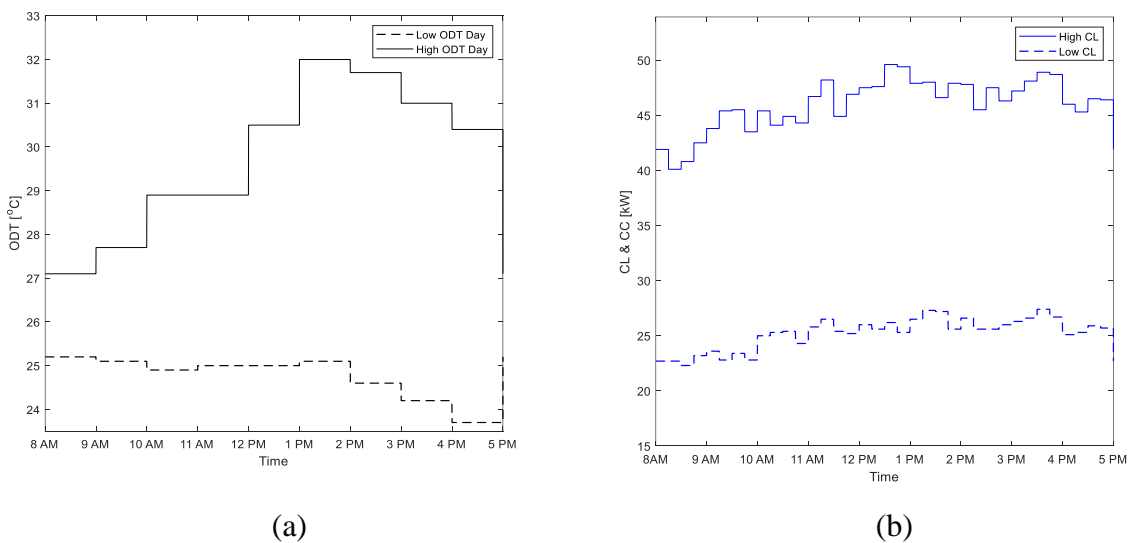
276 Figure 4 presents the architecture scheme for sequential control. A simple hysteresis controller can
 277 be used to implement the “ON-OFF” sequence of each CMP, which is assigned to work in a range of
 278 $\pm\Delta T_{ws,n}$. Worth noting that the hysteresis controller for each CMP can be simulated by using the built-
 279 in block named “hysteresis comparator” available in MATLAB Simulink.



280
 281 **Figure 4.** Architecture control for the sequential control strategy.

282 **3. Case study: description, modeling, and simulation**

283 An office building located in Palermo (Italy) is selected as a case study. Demand profiles are
 284 estimated using data available from energy audits performed in a previous study [40]. Two working
 285 days in the cooling period are here examined. One is characterized by a high cooling demand (i.e.,
 286 around the end of July), and the other one by a low demand (i.e., around the half of June). In Figure
 287 5.a-b, the values of ODT and cooling load are presented. Worth noting that, the dashed line is used
 288 for the profile in the low-cooling load day and the continuous line for the high-cooling load day.
 289 Focusing on the building load, it is assumed an operation for 9 hours during a day, (from 8 am to 5
 290 pm) with a variation of the load at 15 minutes. In addition, as shown in Figure 5.a, the ODT values
 291 vary on an hourly basis, and the values are retrieved from a meteorological dataset [41].



292 **Figure 5.** Daily profiles of low- and high-cooling load days: (a) ODT values, (b) cooling demand.

293 The nominal capacity of the chiller was selected based on the peak value of the cooling demand, equal
 294 to around 50 kW_c. In Table 2, the technical data of the refrigerant circuit and IM are shown. Note that
 295 these data are derived from commercial catalogs.

296 **Table 2.** Technical details on a 50 kW_c air-cooled chiller and electrical parameters of the induction motor.

Refrigerant Circuit		Induction Motor	
Refrigerant	R410a	P_n (kW)	10
CND Type	Fin and Tube	R_s (Ω)	0.8
Number of CND	1	R_r (Ω)	2.91
CND Fan Power [kW]	1.5	L_s (H)	0.21
Metering Device	Electronic Expansion Valve (EEV)	L_r (H)	0.21
EVP Water Flowrate [m ³ /h]	7.0	L_m (H)	0.2
EVP Pump Power [kW]	2	J (kg.m ²)	0.1
CMP Type (and Number)	Scroll (2)	σ (-)	0.03
CMP Power (each) [kW]	9.0	f (Hz)	50
Refrigerant Charge [kg]	14.3	p	2

297
 298 As shown in Table 2, the chiller is equipped with two scroll CMPs. For the scope of this paper, two
 299 control strategies for CMPs are considered:

- 300 - *variable-speed CMP* (in the following indicated also as a variable-speed chiller) according to
 301 which the speed of both CMPs is continuously varied between a minimum and a maximum
 302 value by the VFDs. From a survey of commercially available scroll CMPs, the rotating speed
 303 ω_{CMP} is assumed to vary between 1000 and 6200 rpm.
- 304 - “*ON-OFF*” *CMPs* with sequential control (in the following briefly indicated as a constant-
 305 speed chiller) according to which CMPs speed is kept constant (typically, 2900 rpm) once
 306 switched ON, and the cooling load is satisfied by cycling “ON-OFF” the CMPs according to
 307 the sequential approach shown in Fig. 3.

308 3.1 Details on the performed simulations

309 The thermodynamic models of the air-cooled chillers are developed by using the IMST-Art software
 310 [33]. The tool implements 1-D thermohydraulic modeling of heat exchangers, refrigerant lines, and
 311 accessories, and its reliability has been proven by accurate validation against wide sets of
 312 experimental results [42]. To map the chiller’s performance, different simulations are developed for
 313 both variable-speed and constant-speed chillers, based on the matrix test shown in Table 3. As can be
 314 observed, *ODT* is varied over a wide range (from 22 up to 38 °C) to account for possible application
 315 of the same model in different climatic conditions. A step variation equal to “+2 °C” is assumed,
 316 leading to nine values to be simulated. Regarding the temperature of the water returning from the

317 hydronic circuit, T_{wr} , the range 8-14 °C is selected to account for different heating/cooling demands.
 318 For this variable, a variation step of “+2 °C” is assumed as well, leading to four T_{wr} values to be
 319 simulated.

320 In the case of the variable-speed chiller, the rotating speed of each CMP is varied (both operating
 321 simultaneously) between 1000 and 6200 rpm, with a step equal to “+400 rpm” and fourteen ω_{CMP}
 322 values had to be simulated). The number of simulation tests to be performed in IMST-Art is then
 323 obtained by combining nine ODT values, four T_{wr} values, and fourteen CMP speeds.

324 Regarding the constant-speed chiller, as shown in Table 3, the rotating speed of each CMP was set to
 325 2900 rpm, as suggested by a commercial catalog [43]. Simulations are first performed by combining
 326 the nine ODT values and the four T_{wr} values and considering that only one CMP is operating. Then,
 327 the tests are repeated considering both CMPs activated.

328 **Table 3.** Matrix test for the air-cooled chiller thermodynamic modeling.

Range		Change Step		Variable-Speed Chiller		Constant-Speed Chiller			
ODT	[°C]	22-38	+2 °C	ω_{CMP} [rpm]		ω_{CMP1} [rpm]		ω_{CMP2} [rpm]	
				Range	Change Step	“ON”	2900	“ON”	2900
$T_{w,r}$	[°C]	8-14	+2 °C	1000-6200	(+400 rpm)	“OFF”	0	“OFF”	0

329
 330 The linear coefficients of Eqs 2.a-b are obtained by using the Least-Square technique. In Table 4, the
 331 coefficients for the mechanical power and delivered capacity are shown for the variable-speed chiller.
 332 In Table 5, the results for the constant-speed chiller are detailed. Worth noting that to evaluate the
 333 error index of the realized model in comparison to the thermodynamic data, the Normalized Root
 334 Mean Square Error Index (NRMSE) is here used. Since the NRMSE values in Tables 4 and 5 are
 335 always less than 5%, a good approximation of simulation data is achieved by the proposed model.

336 **Table 4.** Values of the fitting coefficients for the variable-speed chiller.

Delivered Capacity				Absorbed Power		
VS-Cooling	L_1	0.009	RMSE [kW]:	K_1	0.004	RMSE [kW]:
	L_2	-0.32	2.26	K_2	0.05	1.41
	L_3	1.55	NRMSE [%]:	K_3	-0.26	NRMSE [%]:
			3.91			5.91

337
 338
 339
 340

Table 5. Values of the fitting coefficients for the constant-speed chiller.

Delivered Capacity				Absorbed Power			
One CMP-ON				One CMP- ON			
CS-Cooling	L_1	0.012	RMSE [kW]:	K_1	0.0008	RMSE [kW]:	
	L_2	-0.38	0.15	K_2	0.16	0.03	
	L_3	0.97	NRMSE [%]:	K_3	0.018	NRMSE [%]:	
			1.15			0.98	
	Delivered Capacity				Absorbed Power		
	Two CMPs-ON				Two CMPs- ON		
	L_1	0.02	RMSE [kW]:	K_1	0.002	RMSE [kW]:	
	L_2	-0.6	0.24	K_2	0.38	0.07	
	L_3	1.58	NRMSE [%]:	K_3	0.043	NRMSE [%]:	
			1.87			2.33	

342 3.2 Implementation of the integrated control scheme and main assumptions for the analysis

343 The overall schemes for sequential control and variable speed are implemented in MATLAB
 344 Simulink. Since the simulation considers the full-day operation, a sample time equal to 0.01 s (quite
 345 large, compared to the typical values adopted for VFDs' modeling) is used to reduce the data point.

346 The variable-speed chiller is controlled by assuming a 7 °C setpoint value for the supply water
 347 temperature. The tuning of the PI parameters in the Temperature Controller (see Fig. 2) is performed
 348 via MATLAB *Sisotool* command [34]. By fixing a settling time of 10 minutes, the command provides
 349 the values of the proportional and integral gains to the users.

350 Regarding the constant-speed chiller with sequential control, a 7 °C value for the $T_{ws, ref}$ is assumed.
 351 However, as previously explained (see Figure 3), appropriate temperature bands are required to avoid
 352 too many cycles of CMPs. For this case, the selected temperature bands are detailed in Table 6.

Table 6. Bands definitions for CMPs cycling in sequential control.

Changes in CMP State	Threshold values
CMP 1: ON, <u>CMP 2: ON</u>	$T_{ws, CMP2_ON} = 8.0 \text{ } ^\circ\text{C}$ ($\Delta T_{ws} = +1.0 \text{ } ^\circ\text{C}$)
<u>CMP 1: ON</u>, CMP 2: OFF	$T_{ws, CMP1_ON} = 7.5 \text{ } ^\circ\text{C}$ ($\Delta T_{ws} = +0.5 \text{ } ^\circ\text{C}$)
CMP 1: ON, <u>CMP 2: OFF</u>	$T_{ws, CMP2_OFF} = 6.5 \text{ } ^\circ\text{C}$ ($\Delta T_{ws} = -0.5 \text{ } ^\circ\text{C}$)
<u>CMP 1: OFF</u>, CMP 2: OFF	$T_{ws, CMP1_OFF} = 6.0 \text{ } ^\circ\text{C}$ ($\Delta T_{ws} = -1.0 \text{ } ^\circ\text{C}$)

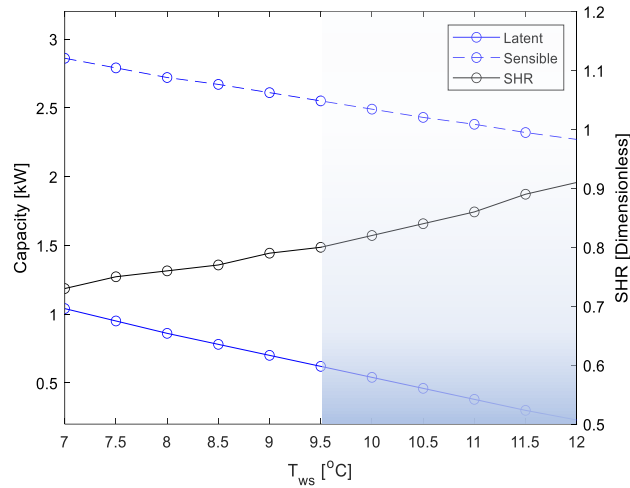
354 To evaluate the energy performance achieved by different control strategies of the chiller, the Energy
 355 Efficiency Ratio (*EER*) averaged on an hourly basis is used and defined in Eq. 10.

$$EER = \frac{\int_0^{3600} CL(t)dt}{\int_0^{3600} P_e(t)dt} \quad (10)$$

366 3.3 Variable water-supply-temperature control strategy

367 As previously mentioned, it is of utmost importance to develop chillers' modeling for simulating new
 368 control strategies aimed at (i) increasing the *EER* of the chiller or (ii) providing ancillary services to
 369 the grid under the current scenarios of growing interest for smart grids, where an active role in grid-
 360 balancing is often played by customers.

361 In this paper, the possibility to operate a chiller with a sliding $T_{ws,ref}$ is investigated. Worth noting that
 362 $T_{ws,ref}$ is usually set to 7 °C regardless of the *ODT* value. The use of sliding water supply temperatures
 363 (variable with the *ODT*) is very common in hydronic heating but rarely adopted in space cooling
 364 despite its significant energy-saving potential. Indeed, the possibility for the chiller to operate with
 365 higher evaporation pressures during moderately warm periods could lead to higher *EER* values. The
 366 reason for this scarce use of sliding water supply temperatures in hydronic cooling lies in the risk to
 367 lose control of indoor relative humidity. Depending on the type of equipment supplied (*e.g.*, fan coils,
 368 cooling coils in air handling units, etc.) the water inlet temperature is a key parameter to guarantee
 369 the required moisture removal from the treated air. Then, a preliminary assessment of the effects of
 370 chilled water supply temperature on the dehumidification capacity of coils is developed, based on the
 371 model proposed by Braun [44]. A cooling coil consisting of three rows, and eight tubes per row
 372 (typical configuration for commercial fan coils) is assumed as a reference. The analysis is aimed at
 373 assessing the changes in the Sensible Heat Ratio (*SHR*) of the coil when it is supplied by chilled water
 374 at different temperatures but with a constant flow rate. The results are shown in Fig. 6, with the
 375 cooling capacity and the *SHR* plotted vs. the chilled water temperature at the coil inlet. The resulting
 376 trends are also validated against data from catalogs of commercial fan-coil systems [45]. The T_{ws}
 377 varies in the range of 7.0-12.0 °C and significant reductions in both the sensible and latent capacity
 378 at higher water temperatures are observed. However, since the latent capacity of the coil for T_{ws} values
 379 above 10 °C is almost less than 50% compared to the value found at 7 °C, it is preferable to limit the
 380 supplied water temperature fluctuations to the 7.0-9.5 °C range (also indicated by the area in Fig. 6
 381 not covered by the light blue rectangle) so that the dehumidification capacity of the coil is only
 382 moderately affected. In quantitative terms, when T_{ws} increases from 7.0 to 9.5 °C, the sensible cooling
 383 capacity slightly decreases from 2.86 down to 2.55 kW (-10.8%) while the latent capacity decreases
 384 from 1.04 kW down to 0.81 kW (-22.12%). Consequently, the *SHR* passes from 0.73 at 7 °C up to
 385 0.8 at 9.5 °C, with a moderate 8.75% increase that sounds acceptable for most space cooling
 386 applications, whenever very strict control of indoor relative humidity is not required.



387

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Figure 6. Sensitivity of coil capacity and SHR to the inlet temperature of chilled water.

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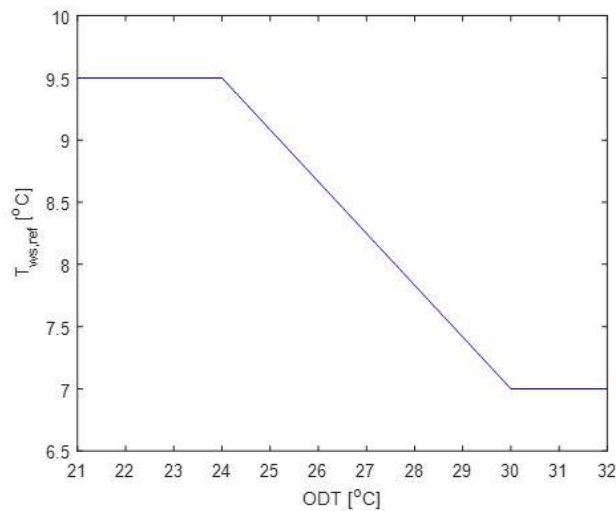
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Based on the above results, the assumption of a sliding supply temperature of chilled water over the 7.0-9.5 °C range sounds technically feasible. Then, it is worth investigating the variation in the performance of the chiller under such conditions to assess the potential benefits in terms of energy savings. As shown in Fig. 7, a linear change in $T_{ws,ref}$ is assumed. In particular, $T_{ws,ref}$ is maintained at 7 °C for ODT values higher than 30 °C. A linear increase from 7 °C up to 9.5 °C is assumed when ODT gradually decreases from 30 °C down to 24 °C. For ODT values lower than 24 °C, $T_{ws,ref}$ is set to 9.5 °C.



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Figure 7. Variable set-point for the supply temperature of chilled water vs. ODT .

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4. Results and Discussion

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400

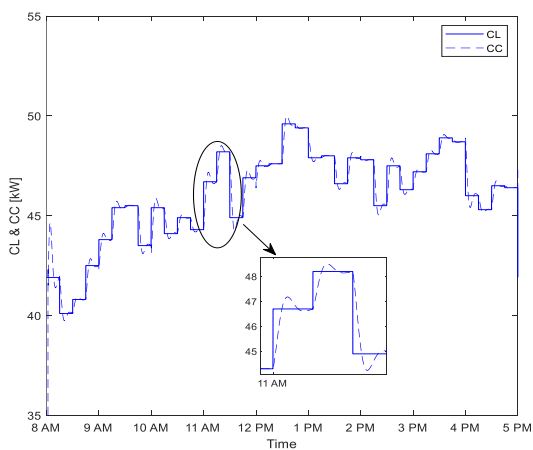
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Simulation results for the variable-speed and constant-speed chiller are first shown. Results from the sensitivity analysis are then discussed. In the last subsection, results for the flexible operation of the chiller are presented.

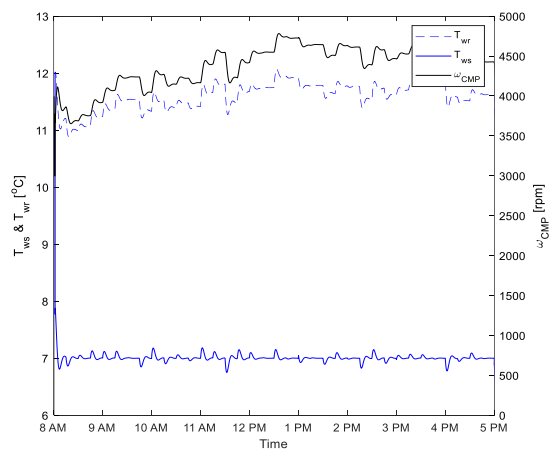
402 **4.1 Variable-speed air-cooled chiller**

403 Figures 8.a-e show results for the variable-speed chiller operation on the high cooling load day. Note
 404 that, for the sake of brevity, in this case, only results for the high cooling load day are shown.
 405 However, similar considerations could be made for the low cooling load day. In Fig. 8.a, the delivered *CC*
 406 (blue dashed line) is presented along with the *CL* profile (blue continuous line). Looking at the *CC*
 407 profile, it is worth noting that the chiller is constantly trying to match the cooling load. As it can be
 408 observed from the zooming at 11-12 am in Figure 8.a, the cooling capacity has an oscillating trend at
 409 each change in the load due to the action of the PI controller. Figure 8.b shows the temperature of the
 410 water supplied to the building. Worth noting that T_{ws} is maintained almost at 7 °C (the assumed
 411 setpoint) thanks to the controller. Some oscillations are present every 15 minutes due to the changes
 412 in *CL*. As shown in Fig. 8.b, the rotating speed of the CMPs is continuously manipulated to meet the
 413 water supply temperature setpoint. In Fig. 8.c, both the electromagnetic torque produced by the IM
 414 and the CMP torque are plotted. Since both curves are perfectly overlapped, it follows that a dynamic
 415 equilibrium is achieved between the CMP and the IM during the operation. Fig. 8.d shows the sum
 416 of the mechanical power supplied by both the IMs to the CMP. In Fig. 8.e, the absorbed RMS current
 417 by the IMs is plotted. Minimal fluctuations in the root mean square value of currents are observed.
 418 As a result, the measured value is always close to 8.2 A. The initial spike accounts for the inrush
 419 current to magnetize the IM. Fig. 8.f shows the average *EER* values calculated according to Eq. 10.
 420 The *EER* ranges between 3.43 and 3.08 during the operation due to the combined effect of part-load
 421 operation and *ODT* values.

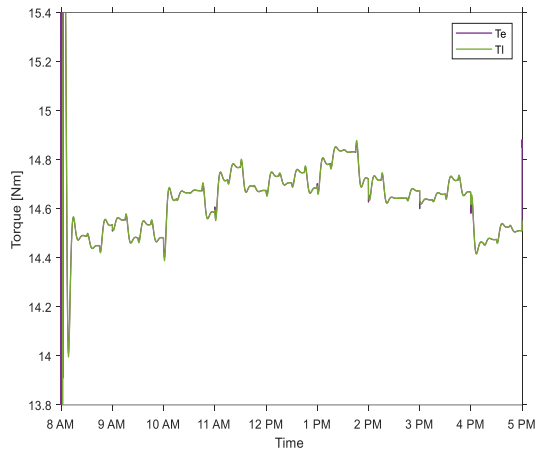
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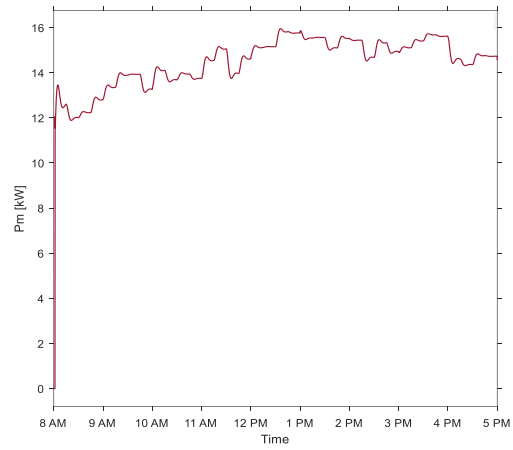
(a)



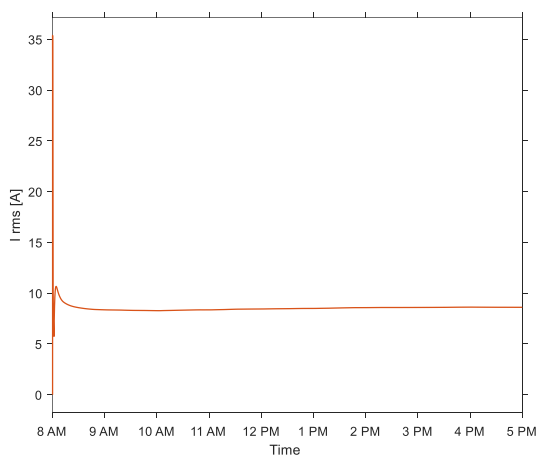
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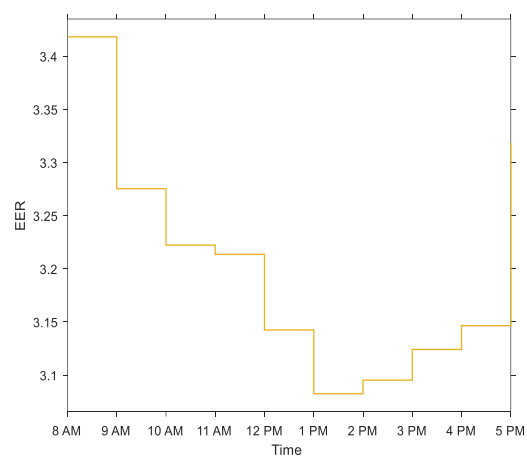
(c)



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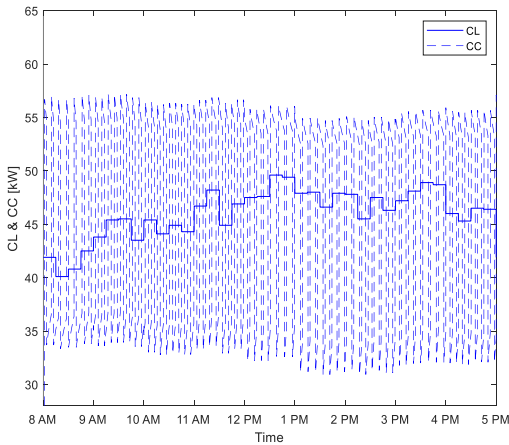
(f)

423 **Figure 8.** Variable-speed results: (a) Cooling Load and Cooling Capacity (b) Water supply temperature,
 424 Water return temperature, and CMP speed, (c) Mechanic and electromagnetic torque, (d) Mechanical Power,
 425 (e) Absorbed Current, (f) *EER*.

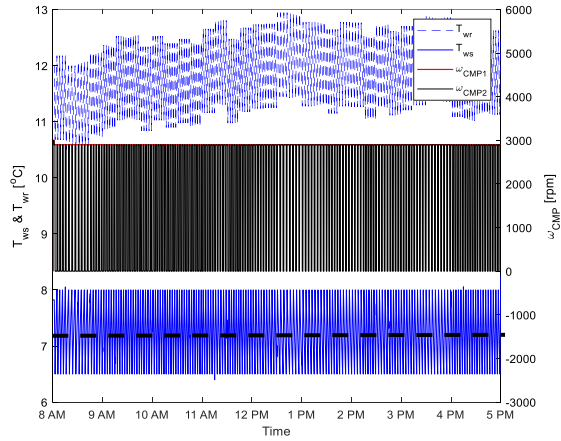
426 4.2 Constant-speed air-cooled chiller

427 Figures 9.a-d show the results for a constant-speed air-cooled chiller for the high cooling load day in
 428 Palermo. In Fig. 9.a the cooling demand profile (blue continuous line) is shown together with the
 429 capacity delivered by the chiller. The different pattern in the *CC* observed here compared to Fig 8.a
 430 is simply explained considering that CMPs are here cycled “ON-OFF”, thus leading to a
 431 discontinuous *CC* profile. Moreover, the minimum *CC* is never zero, since one CMP (i.e., CMP 1) is
 432 always operating. In this respect, as shown in Fig 9.b, the value of ω_{CMP1} is always 2900 rpm (red
 433 line), conversely ω_{CMP2} changes from 0 or 2900 rpm, according to the cycling (black line). Moreover,
 434 the temperature of the water supplied to the building is oscillating around the value of 7.25 °C value
 435 (black dashed line). In Fig. 9.c-d a zoom on two hours in the high cooling load day is shown. Fig.
 436 9.c plots the CMPs’ operation from 8 to 9 am, when the lowest cooling demand is observed. Fig. 9.d
 437 focus from 11 to 12 am. CMP 1 is always operating, since on this day the minimum cooling load
 438 value (which is observed from 8 am to 9 am) is higher than the minimum capacity provided by the

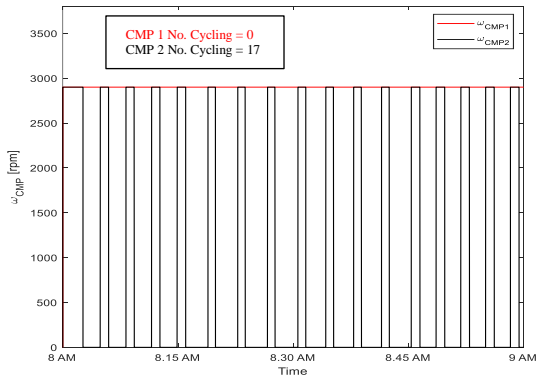
439 chiller with only one CMP operating. Conversely, CMP 2 is continuously cycling “ON-OFF” to
 440 match the load. As shown within the box in Fig. 9.c, from 8 to 9 am CMP2 is cycling “ON-OFF”
 441 almost 17 times, which is higher than the maximum threshold value equal to “12 cycles per hour”
 442 suggested by the manufacturer. From 11 to 12 am, instead, CMP 2 is cycling 19 times. In Figure 9.e,
 443 the mechanical power required by the CMPs is plotted. As expected, it is never equal to zero since
 444 CMP 1 is always ON. Fig. 9.f shows the average hourly *EER* values. The *EER* ranges between 3.29
 445 and 2.85 during the operation due to the combined effect of part-load operation and different *ODT*
 446 values.



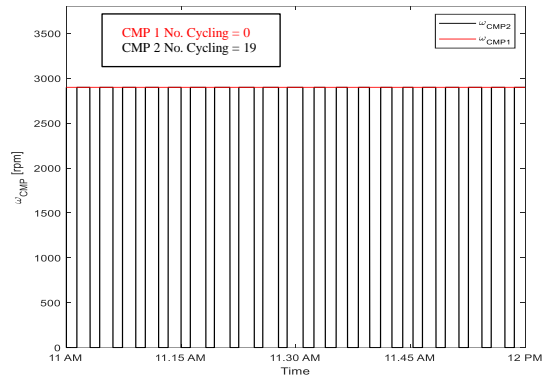
(a)



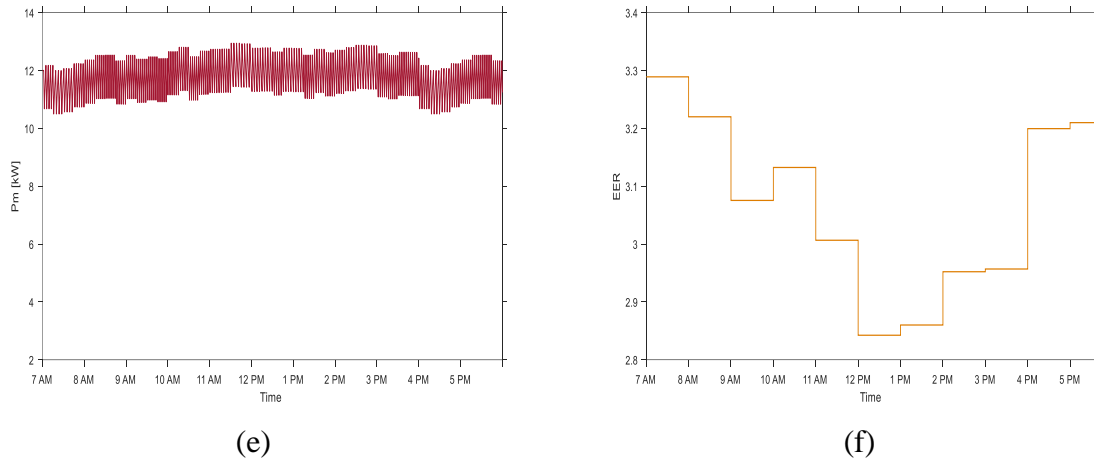
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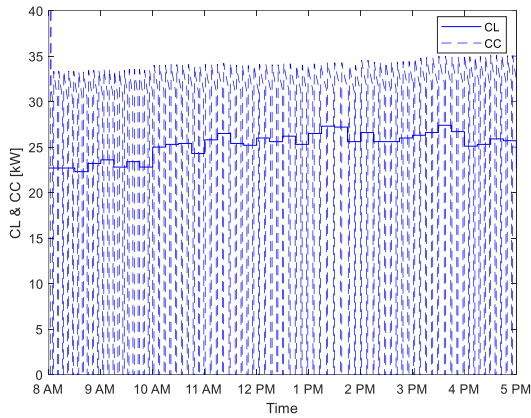
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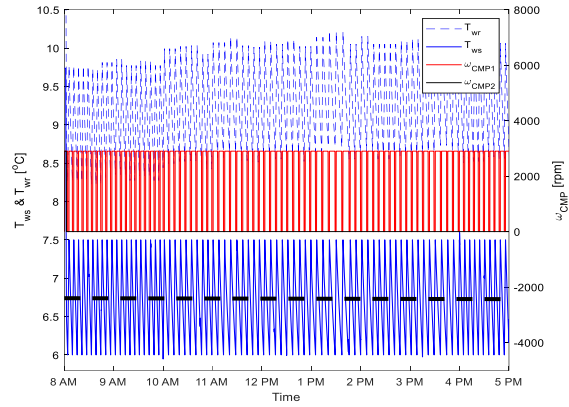
447 **Figure 9.** SC results for high-cooling load day: (a) Cooling Load and Cooling Capacity (b) Water supply,
 448 Water return temperature, and CMPs cycles, (c) CMPs' operation from 8-9 am, (d) CMPs' operation from
 449 11-12 am, (e) Mechanical Power, and (f) *EER*.

450

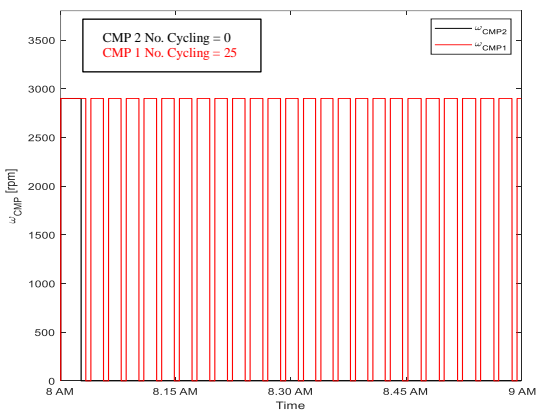
451 Figures 10.a-d show the results obtained from simulations for a constant-speed air-cooled chiller on
 452 the low-cooling day in Palermo. As shown in Fig. 10.a, compared to Fig. 9.a, the minimum delivered
 453 CC is zero, meaning that the unit is completely OFF during the day. As shown in Fig 10.b, the value
 454 of ω_{CMP2} is always zero (black line), conversely, ω_{CMP1} changes from 0 to 2900 rpm, according to the
 455 cycling (red line). Moreover, the temperature of the water supplied to the building is oscillating
 456 around the value of 6.75 °C value (black dashed line). In Fig. 10-c-d a zoom on the low load (8-9 am)
 457 and high (11-12 am) hours of this day is shown. Fig. 10.c plots the CMPs' operation from 8 to 9 am.
 458 CMP 2 is ON only for some minutes at the very beginning of the selected hours due to the start-up of
 459 the plant. Then, CMP 2 is OFF for all the remaining working hours in the day, since the maximum
 460 cooling load value (observed from 1 to 2 pm) is lower than the minimum capacity provided by the
 461 chiller with two CMPs ON. Conversely, CMP1 is continuously cycling "ON-OFF" to match the
 462 cooling load. As shown in the box in Fig. 10.c, from 8 to 9 am CMP 1 is cycling "ON-OFF" almost
 463 25 times, which is higher than the maximum threshold value equal to 12. From 11 to 12 am (Fig.
 464 10.d), CMP 1 is cycling 21 times. In Figure 10.e the mechanical power required by the CMPs is
 465 plotted. As expected, its minimum value is zero in those moments where the unit is OFF. Fig. 10.f
 466 shows the average hourly *EER* values. The *EER* ranges between 2.96 and 3.27 during the operation
 467 due to the combined effect of part-load operation and different *ODT* values. These results highlight
 468 the importance of including detailed chiller modeling in studies focused on new control strategies for
 469 increasing energy savings or flexibility in those buildings equipped with chillers: indeed, in such
 470 cases, the risk of unsafe CMPs' operation can be easily predicted.



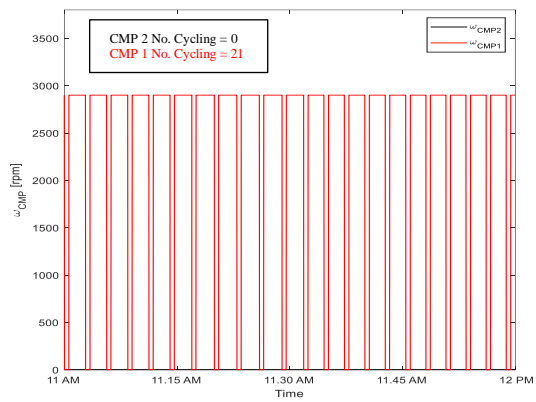
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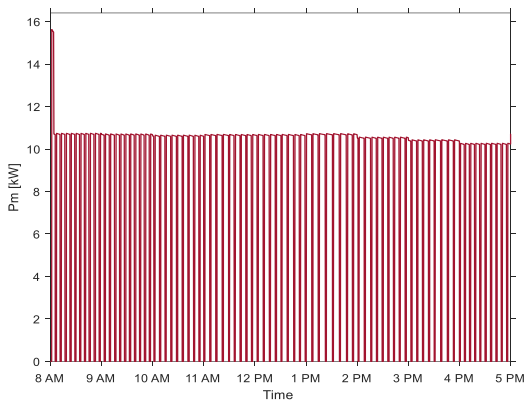
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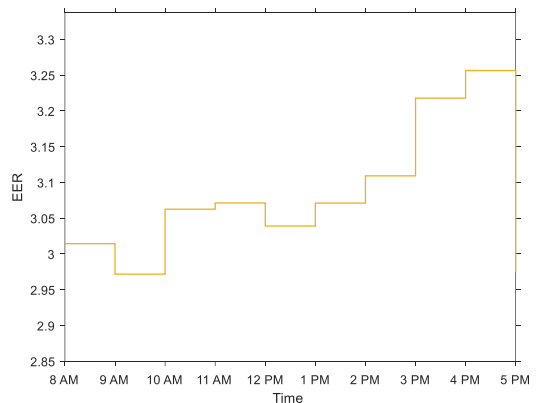
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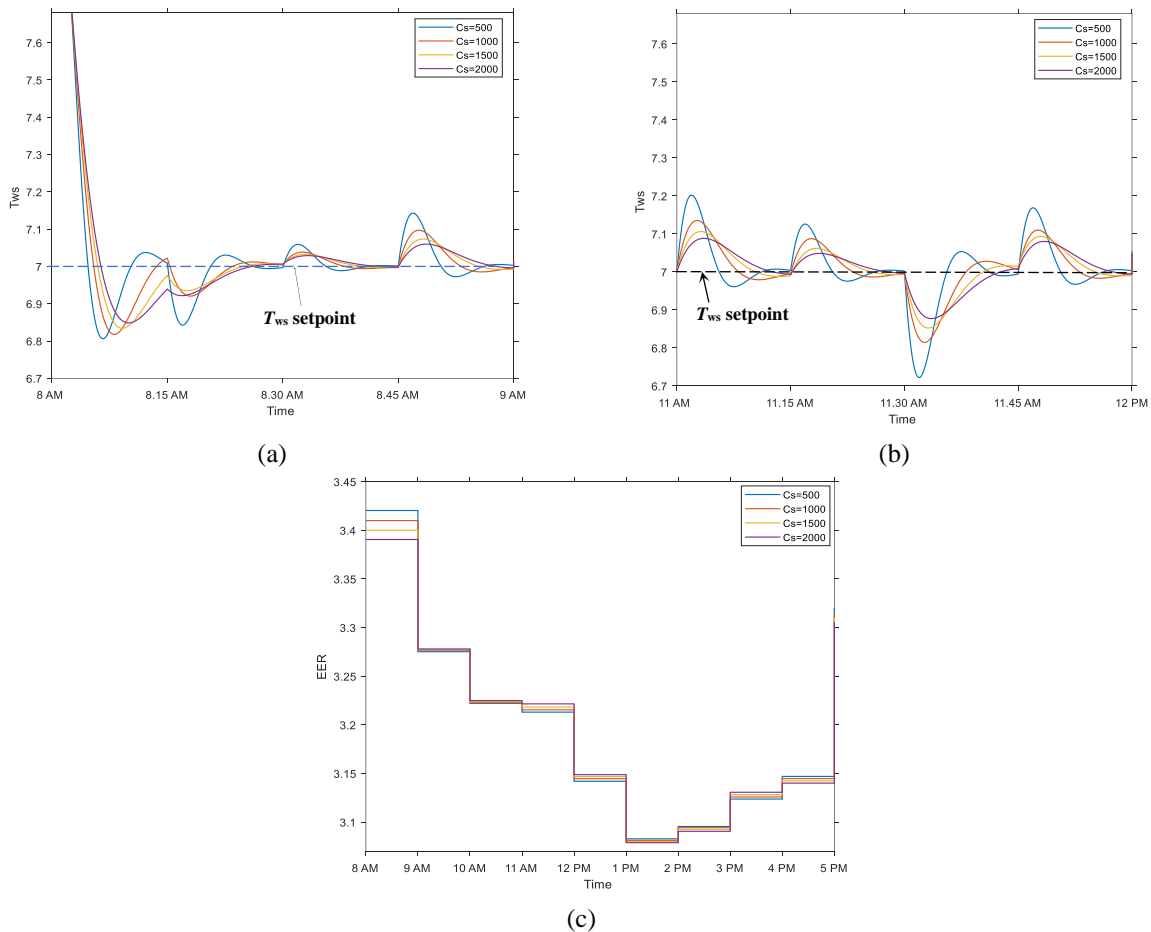
471 **Figure 10.** SC results for low-cooling load day: (a) Cooling Load and Cooling Capacity (b) Water supply,
 472 Water return temperature, and CMPs cycles, (c) CMPs' operation from 8-9 am, (d) CMPs' operation from
 473 11-12 am, (e) Mechanical Power, and (f) *EER*.
 474

475 4.3 Sensitivity analysis with the design of the hydraulic loop

476 In the previous section, simulations were performed assuming a C_s equal to 600 kJ/°C. It is worth
 477 investigating the effect of different C_s values on the controller actions and overall energy

478 performance. Then, simulations are performed considering the following C_s values: 500 -1000-1500
479 -2000 kJ/°C.

480 Results for the case of the variable-speed chiller are presented in Figure 11. In particular, Fig. 11.a-b
481 presents the water supply temperature for all the C_s values at 8-9 am. Note that for the sake of clarity,
482 only data for two hours, i.e., 8-9 am and 11-12 am are here presented for the high-cooling load (Fig.
483 11.a-b). In both figures, moving from the smallest value (i.e., 500 kJ/°C, blue line) to the highest one
484 (i.e., 2000 kJ/°C, purple line), a reduction in the peak value of T_{ws} is observed after changes in the
485 cooling demand. For instance, as shown in Fig. 5.a-b the temperature overshoot after a load change
486 is almost halved passing from 500 kJ/°C to 2000 kJ/°C. Moreover, when increasing the C_s value, the
487 oscillating behavior in T_{ws} is reduced, leading to a more stable chiller operation and the quick reaching
488 of steady-state operation. Fig. 11.c presents the average hourly EER values. Worth noting that the
489 variation of C_s has a negligible impact on hourly EER values. These results suggest that, in the case
490 of variable-speed units, variation in the thermal inertia of the hydronic loop mainly affects the
491 dynamic response of the chiller (overshoot of the supplied water temperature), while changes in
492 energy performance are almost negligible.



493 **Figure 11.** Variable-speed chiller results with different C_s values: (a) Water supply temperature profile from
494 8-9 am in the high cooling load day, (b) Water supply temperature profile from 11-12 am on the high cooling
495 load day, and (c) EER values in the high cooling load day

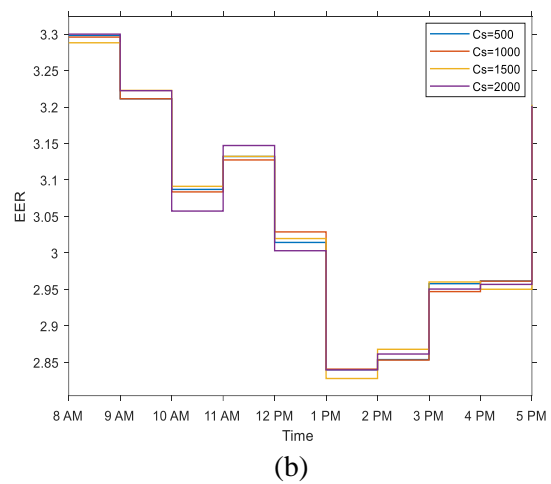
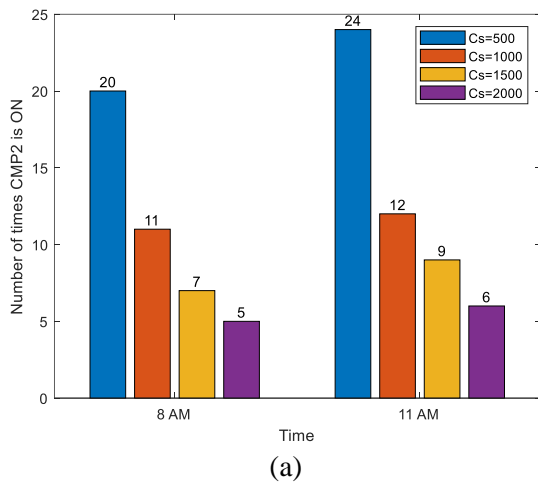
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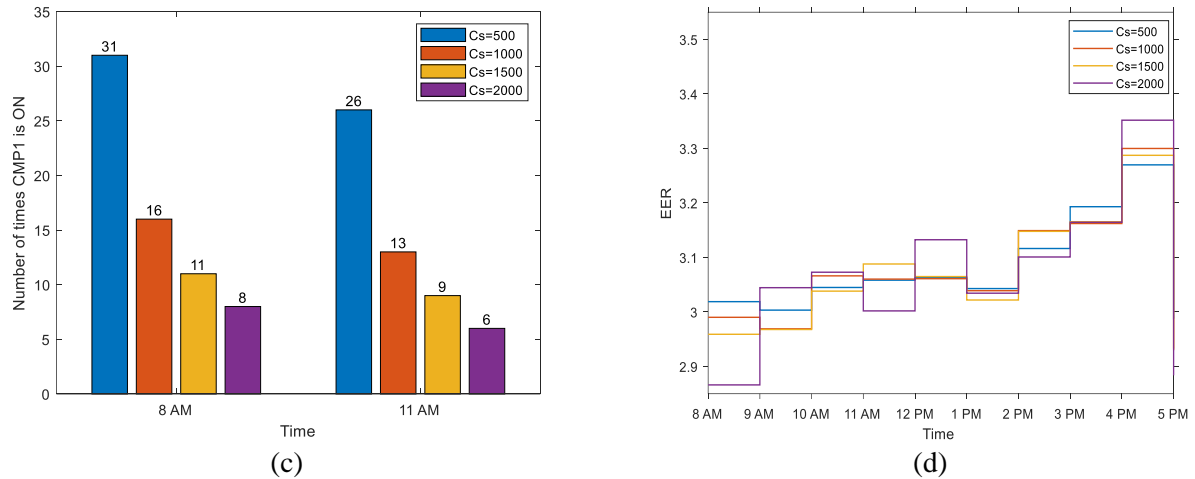
497 The results of the sensitivity analysis for the case of the constant-speed chiller are presented in Figure
498 12. In this case, results for the same two hours (i.e., 8-9 am and 11-12 am) are presented not only for
499 the high cooling day (Fig 12. a-b) but also for the case of low cooling day (Fig 12.c-d).

500 As shown in Fig. 12.a, for the high cooling load day, only effects of CMP 2 are shown, since as
501 previously observed, CMP 1 is always ON. Worth noting that, as C_s increases (i.e., when the thermal
502 inertia of the hydronic circuit increases) the number of cycling strongly reduces. Indeed, when passing
503 from $C_s= 500$ kJ/°C to 1000 kJ/°C, the number of cycling “ON-OFF” for CMP 2 decreases, but it is
504 almost near the threshold values in both hours (i.e., 12 cycles per hour). However, if C_s is increased
505 up to 1500 kJ/°C the number of cycling falls below the threshold value.

506 Regarding the low-load cooling day (Fig 12.c-d), only results for CMP 1 are shown, since as
507 previously observed, CMP 2 is always OFF. Note that C_s should be increased up to 1500 kJ/°C to
508 maintain the number of cycling below the threshold (i.e., 12 cycles per hour). By looking at the *EER*
509 values in Figs 12.b and 12.d, it can be noted that the variation of C_s has minimal impact on it. As in
510 the case of variable-speed systems, these results suggest that for the case of the constant-speed chiller,
511 variation in thermal inertia of the hydronic loop does not heavily affect its energy performance, but
512 it can lead to unsafe operation of CMPs.

513





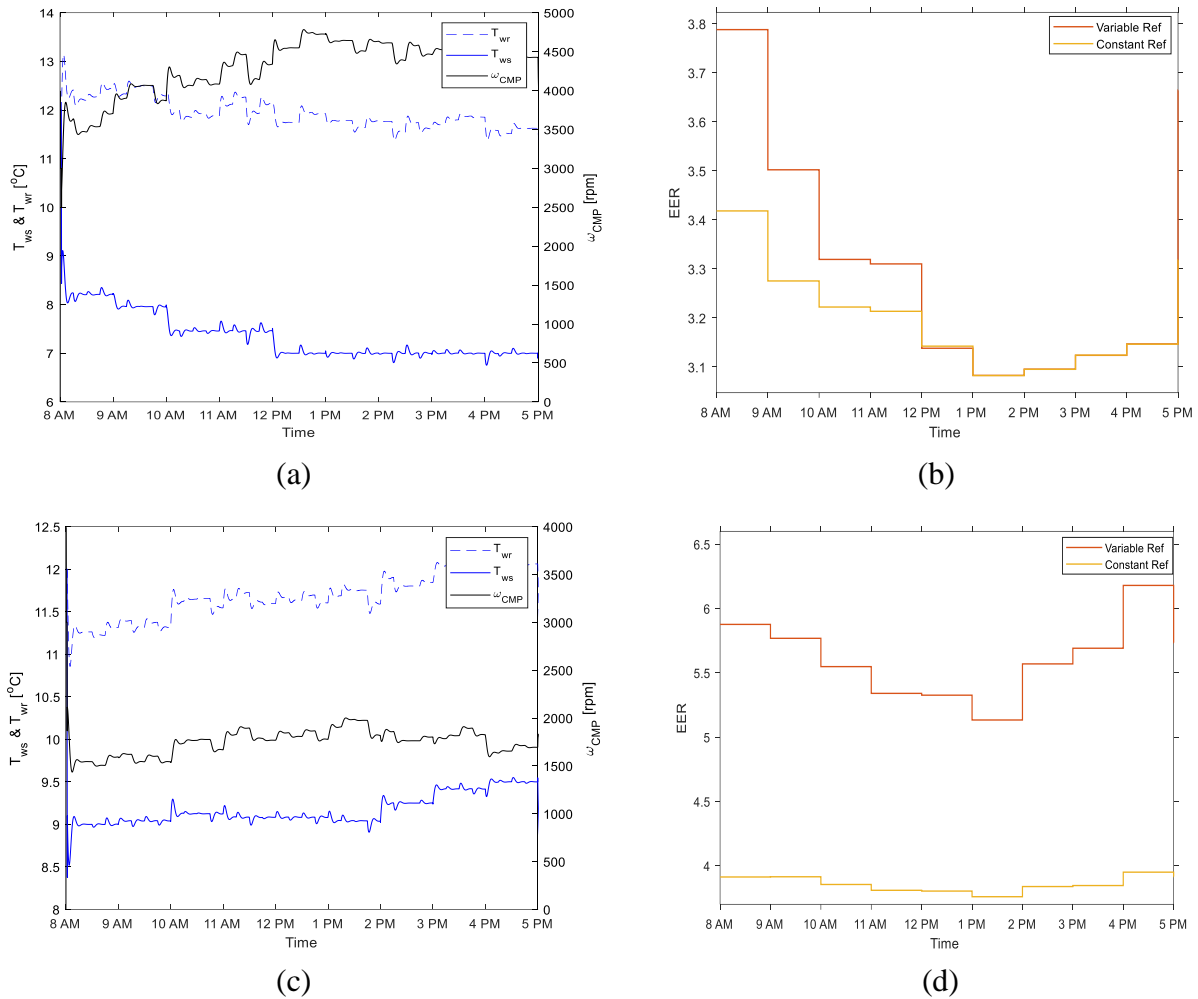
514 **Figure 12.** Constant-speed chiller results with different C_s values: (a) Number of CMP 2 cycling in the high
 515 cooling load day, (b) EER values in the high cooling load day, (c) Number of CMP 1 cycling in the low
 516 cooling load day, and (d) EER values in the low cooling load day.
 517

518 4.4 Flexible operation of the air-cooled chiller

519 In the proposed scenario, the chiller is operated by setting a variable setpoint for the temperature of
 520 the water supplied to the building, as shown in Figure 7. Results for the high cooling load day are
 521 shown in Figure 13.a-b. As shown in Fig. 13.a, the T_{ws} is not more kept at 7 °C like before (see Fig.
 522 8-b). The values of T_{ws} vary from 8 °C in the early morning to around 7.4 °C from 10 to 12 am, since
 523 the ODT values are less than 30 °C till 12 am (see Fig. 5.a). As shown in Fig. 13.b, an increase in the
 524 average value in some hours is achieved by this new strategy (orange line) compared to the previous
 525 one (yellow line). In particular, from 8 to 9 am, the percentage increase of EER is 10.8% (from 3.42
 526 to 3.79) thanks to the higher setpoint. The percentage variation of EER gradually reduces during the
 527 day, reaching almost zero during high-load hours (i.e., after 12 pm)

528 Results for the low-cooling load day are shown in Figure 13.c-d. In this case, since ODT is always
 529 less than 30 °C (as shown in Fig. 5.a.). Therefore, the water is supplied to a T_{ws} value higher than 7
 530 °C (here T_{ws} ranges between 9 and 9.5 °C), with a substantial increase in the average EER value
 531 throughout the day (Fig. 13.d). In particular, the highest percentage variation in EER is observed from
 532 4 to 5 pm (almost 60.3%), when the EER increases from about 3.9 to 6.25. Conversely, the minimum
 533 variation was found from 1 to 2 pm (almost 37.8%) when the EER increases from about 3.7 to 5.1.

534 These results suggested that the proposed strategy could be a promising solution to achieve a
 535 reduction in the electricity demanded by the chiller to the grid, which could be very helpful in
 536 evaluating the feasibility and effectiveness of demand response programs.



537 **Figure 13.** Results with sliding water supply temperature: (a) Water supply, Water return temperature, and
 538 CMP speed in the high cooling load day; (b) *EER* values in the high cooling load day; (c) Water supply,
 539 Water return temperature, and CMP speed in the low cooling load day; (d) *EER* values in the low cooling
 540 load day.

541 **5. Conclusions**

542 In this paper, an integrated thermodynamic and control modeling for an air-cooled chiller is developed
 543 to simulate the control strategies typically adopted in the field to meet the variable cooling demand
 544 and to test innovative ones aimed at increasing energy efficiency. To show the capabilities of the
 545 model, a variable-speed air-cooled chiller serving an office in the Mediterranean area is assumed as
 546 the case study. Results show that in the case of a variable-speed chiller, the model allows for
 547 continuous monitoring of the effect of controller action on the unit (e.g., the instantaneous values of
 548 CMP speed, IM torque, and the temperature of the cold water supplied to the building). Moreover,
 549 the required supply water setpoint is always met. In the case of a constant-speed chiller with
 550 sequential control for CMPs, a clear picture of the number of CMP cycling is provided, allowing for
 551 safety assessment during the chiller's operation. The model enables the possibility to perform
 552 sensitivity analyses of results with the design of the hydronic loop. In the case of a constant-speed

553 chiller, the sensitivity analysis reveals that thermal inertia heavily affects the number of CMP cycling.
554 In addition, the minimum thermal inertia value which allows keeping the CMP cycling below the
555 threshold value is determined. Conversely, in the case of a variable-speed system, effects in terms of
556 supply water temperature oscillation and overshoot are estimated. Thanks to the proposed model, an
557 innovative operating strategy is simulated. In this respect, it is found that room for energy savings
558 existed when a sliding water supply temperature setpoint is adopted. In particular, the highest
559 percentage variation in *EER* is observed on a day of low cooling demand (almost 60.3%). However,
560 rooms of energy savings exist also on days of high cooling demand, where a 10.8% increase in the
561 *EER* value could be achieved. As major implications in the field, the proposed study confirms the
562 importance of a detailed thermodynamic and control modeling of chillers for the assessment of energy
563 savings achievable through the adoption of innovative operating strategies. In this regard, modeling
564 the dynamic response of chillers is crucial to quantify the time required and the energy consumed in
565 reaching a steady-state operation after any change in boundary or loading conditions. Such dynamic
566 modeling reveals extremely precious for a reliable assessment of the performance of chillers in
567 handling demand-response programs and providing ancillary services in areas characterized by high
568 penetration of intermittent renewables. In the current scenario where a large spread of hydronic
569 reversible heat pumps is expected soon (representing key technologies for the ongoing replacement
570 of gas boilers), assessing the effects of the thermal inertia of these units, when operated in cooling
571 mode as chillers, and their hydronic loops, as well as the influence of the control strategy, on the time
572 profile of power absorption, will be relevant for rational decision-making concerning power-
573 dispatching by grid operators. Finally, integrated modeling of the chiller and the controller's action
574 will be essential to guarantee strict respect for safety constraints regarding the frequency of CMP
575 cycling, thus preventing the risk that innovative energy-saving-oriented control strategies could result
576 in highly unstable operation and more frequent troubleshooting or reduced technical life expectancy
577 of chillers. In future studies, the proposed integrated model will be further implemented focusing the
578 attention on improved building flexibility.

579

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584

585

Acronyms

CMP	Compressor
CND	Condenser
CTRL	Control
EVP	Evaporator
EV	Expansion Valve
IM	Induction Motor
PI	Proportional and Integrator
RES	Renewable Energy Source
RMS	Root Mean Square
SHR	Sensible Heat Ratio
SC	Sequential control
SVM	Space vector modulation
VFD	Variable frequency drive
VSI	Voltage Source Inverter

Variables

CL	Building Cooling Load (W)
CC	Cooling Capacity (W)
V_{des}	Desired volume of water in the hydronic loop (m ³)
T_{el}	Electromagnetic torque (Nm)
EER	Energy Efficiency Ratio (dimensionless)
u_s	Input stator voltage (V)
$D_{a,b,c}$	Inverter duty cycles (sec)
\dot{m}_w	Mass flowrate of water circulating in the hydronic loop (kg/s)
P_m	Mechanical Power (W)
T_L	Mechanical torque (Nm)
L_m	Mutual inductance (H)
CC_{nom}	Nominal cooling capacity delivered (W)
NRMSE	Normalized Root Mean Square Error Index
p	Number of pair poles (dimensionless)
ODT	Outdoor air temperature (°C)
$T_{ws,ref}$	Reference Temperature of the water supplied to the hydronic loop (°C)
L_r	Rotor inductance (H)
T_r	Rotor time constant (sec)
c_w	Specific heat capacity of water (kJ/(kg °C))
i_s	Stator currents (A)
L_s	Stator inductance (H)
R_s	Stator resistance (Ω)
T_{wr}	Temperature of the water returning from the hydronic loop (°C)
T_{ws}	Temperature of the water supplied to the hydronic loop (°C)
$V_{a,b,c}$	Three-phase voltages (V)

Greek Letters

ϕ'_r	Rotor fluxes (Wb)
ω_{CMP}	Compressor rotating speed (rpm)
σ	Blondel coefficient (dimensionless)
ρ_w	Density of water (kg/m ³)

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