1	Prediction of debris-avalanches and -flows triggered by a
2	tropical storm by using a stochastic approach: An
3	application to the events occurred in Mocoa (Colombia) on
4	1 April 2017
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14	A B S T R A C T
15	Landslides are among the most dangerous natural processes. Debris avalanches and debris flows in
16	particular have often caused casualties and severe damage to infrastructures in a wide range of
17	environments. The assessment of susceptibility to these phenomena may help policy makers in
18	mitigating the associated risk and thus it has attracted special attention in the last decades.
19	In this experiment, we assessed susceptibility to debris-avalanche and -flow landslides by using a
20	stochastic approach. Two different modeling techniques were employed: i) Multivariate Adaptive
21	Regression Splines (MARS) and ii) Logistic Regression (LR). Both MARS and LR allow for
22	calculating the probability of landslide occurrence by building statistical relationships between a set
23	of environmental variables and the target variable, i.e. presence/absence of the landslide event. The

24 target variable was extracted from an inventory of debris-avalanche and - flow landslides which were triggered by the tropical storm that hit the area of Mocoa (Colombia) on 1 April 2017. As 25 predictor variables, we employed nine terrain attributes derived from a 5-m resolution DEM (i.e. 26 elevation, slope angle, northness, eastness, upslope slope angle, convergence index, topographic 27 28 position index, valley depth and topographic wetness index), in addition to lithology, distance from 29 faults and presence/absence of soil creep processes. In our experiment, we used three different landslide datasets which contain i) the highest point of each recognized landslide crown-lines 30 31 (dataset LIP), ii) the highest 10% of cells of each landslide area (dataset SOURCE), and iii) the entire landslide areas, which include initiation and accumulation zones (dataset MASS). In order to 32 33 evaluate their predictive ability. LR and MARS models were submitted to k-fold spatial crossvalidation strategy, which consists in extracting random training and test subsets from k spatially 34 disjoint sub-areas. The results of model validation, expressed in terms of Area Under the ROC 35 36 Curve (AUC), demonstrate better predictive performance of MARS models with respect to LR 37 models, for all the three landslide datasets. The mean AUC values calculated for the datasets LIP, SOURCE and MASS of the MARS models are 0.776, 0.788 and 0.768, respectively, whereas AUC 38 39 values of the LR models are 0.748, 0.751 and 0.703, respectively. Models validation also show that the predictive skill of the models is better when landslide data are sampled from the highest 40 portions of the landslides (dataset SOURCE). Maps of susceptibility to debris-avalanche and -flow 41 42 landslides for the Mocoa area were produced by using both LR and MARS and the three landslide datasets. The analysis of the distribution of events versus the susceptibility classes of the maps 43 44 confirm that MARS and the dataset SOURCE provide the best ability to discriminate between event 45 and non-event cells.

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*Keywords*: Debris flows; Landslide susceptibility; Tropical storm; Multivariate Adaptive
Regression Splines (MARS); Logistic Regression (LR); Mocoa (Colombia).

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#### 52 **1. Introduction**

53 In the last decades, the population growth and the urbanization of hazardous areas have largely 54 increased the damage and loss of lives due to natural disasters. In many developed and developing 55 countries, landslides are among the most important causes of natural hazard (Guzzetti et al., 1999).

56 Landslide hazard is particularly important in mountainous environments where, due to topography, 57 these phenomena may achieve rapid propagation and high energy. Some of the most devastating 58 landslide disasters are related to the occurrence of debris avalanches and debris flows triggered by heavy rainstorms or earthquakes (Hungr et al., 2014). When caused by intense and prolonged 59 60 rainfalls, these landslides may occur simultaneously with hyperconcentrated flows and flash floods. A dramatic example of their destructive potential is given by the disaster of Vargas (Venezuela) 61 62 which caused around 15,000 fatalities in December 1999 on a narrow coastal zone north of Caracas 63 (Larsen and Wieczorek, 2006; Larsen, 2008). More recently, in January 2011, over 1,500 casualties 64 were caused by the disaster occurred in the mountainous region of Rio de Janeiro (Brazil), where 65 clusters of debris avalanches and debris flows were triggered by an extreme rainfall event during a 66 period of 2 days (Avelar et al., 2013, Hungr et al., 2014). Other examples of natural disasters that occurred worldwide and related to debris avalanche/flow landslides are reported in the literature 67 68 (e.g., Crosta and Dal Negro, 2003; Crozier, 2005; Aronica et al., 2012).

Mitigation of landslide risk may be achieved by predicting where landslides are more likely to occur in the future. This information could indeed help policy-makers in implementing land-use strategies aimed at minimizing human casualties and property damage (Guzzetti et al., 1999). The likelihood of landslide occurrence in a given area is defined as landslide susceptibility (Brabb, 1984; Carrara et al., 1995). A landslide susceptibility map depicts the spatial relative probability of landslide occurrence within a given area (Conoscenti et al., 2016).

Landslide susceptibility mapping can be achieved by using different methods. Among them, the stochastic approach has become very popular over the last decades, due to the availability of highresolution terrain data and freeware statistical and Geographical Information Systems (GIS) 78 software. This approach is based on the assumption that "the past is the key to the future" (Carrara 79 et al., 1995) and new slope failures are more likely to occur under the same conditions that caused 80 landsliding in the past. Therefore, statistical methods require the location of past landslides and 81 maps of environmental variables which directly or indirectly (as proxies) reflect the preparatory 82 factors controlling landslide occurrence in the study area. Different statistical and data mining modeling techniques have been proved to provide reliable and accurate landslide susceptibility 83 maps starting from event inventories and sets of predictor variables (Aleotti and Chowdhury, 1999; 84 85 Guzzetti et al., 1999; Brenning, 2005; Reichenbach et al., 2018).

Although widely adopted in recent years, statistical modeling of landslide susceptibility involves some critical issues which still remain unsolved. One of these is related to the selection of event and non-event data which are employed to calibrate and validate the landslide predictive models. This is recognized as a crucial step influencing the accuracy and reliability of the final landslide susceptibility models and maps.

91 In case of grid-based landslide predictions, non-event locations are typically sampled from stable portions of slopes, i.e. cells outside the landslide areas. On the other hand, no agreement exists on 92 93 the best approach to select landslide cells. These should identify landscape locations where levels of 94 the landslide controlling factors exceeded the threshold of slope stability and, thus, triggered the 95 slope failure. However, identifying the exact initiation points of a large number of landslides is very problematic (Regmi et al., 2014). In the case of debris avalanches or flows, even distinguishing 96 97 between source and accumulation zones could be quite difficult. Furthermore, once initiated, a landslide can extend upslope, downslope and/or sidewise, making the identification of the initiation 98 99 point a very challenging task.

Various landslide data selection and sampling techniques have been proposed to minimize the
uncertainty in identifying landslide initiation points. The most frequently adopted strategies are: i)
single cells randomly selected from landslide areas or from depletion zones (e.g., Vorpahl et al.,
2012; Heckmann et al., 2014; Goetz et al., 2015); ii) centroid of landslide areas or of depletion

104 zones (e.g., Atkinson and Massari, 2011; Regmi et al., 2014); iii) multiple cells (all or a fraction) 105 within landslide areas or depletion zones (e.g., Regmi et al., 2014; Conoscenti et al., 2016); iv) 106 single cell or all the cells in the upper edge of the main scarp (e.g., Clerici et al., 2006; Costanzo et al., 2012; Cama et al., 2015; 2017). Moreover, when the available DEM is more recent than the 107 108 landslide inventory, topographic triggering conditions are sampled from a buffer around the 109 landslide polygons (e.g., Süzen and Doyuran, 2004; Nefeslioglu et al. 2008; Rotigliano et al., 2011) 110 or from a reconstructed pre-failure topography within landslide areas (e.g., Van Den Eeckhaut et al. 111 2006; Gorum et al. 2008; Conoscenti et al., 2015).

Intense and prolonged rainfall events occur episodically in tropical Andes, triggering debrisavalanche and -flow landslides, hyperconcentrated flows and flash floods. These natural hazards threaten many communities living on or near alluvial fans where they may cause fatal victims and extensive property damage. The assessment of susceptibility to debris-avalanche and -flow landslides in these environments is therefore crucial to plan risk mitigation strategies and prevent large disasters.

On 1 April 2017, the area of Mocoa (Colombia) was hit by a sever tropical storm which discharged 130 mm of rain in 3 h starting from 10:00 pm of March, 31<sup>st</sup>. This heavy rainfall triggered more than one thousand debris-avalanche and -flow landslides, which evolved to hyperconcentrated flows in the main streams of the Mulato, Sangoyaco and Taruca rivers, three tributaries of the Mocoa river. The event caused 328 victims, 200 missing, more than 1000 injured and damage to more than 120 houses in 17 neighborhoods of the city.

In this study we focused on the prediction of the rainfall-induced debris-avalanche and -flow landslides which occurred in the area of Mocoa. These processes initiated on the slopes and provided sediments to hyperconcentrated flows which moved rapidly down steep channels and caused debris flooding of large parts of the city located on the alluvial fans. Within the context of testing different methods of landslide data sampling for susceptibility modeling, we used and compared three criteria which differ in the way the event data were selected. The landslide datasets

130 employed in our experiment include (i) the highest point of each landslide area, (ii) the highest 10% 131 of cells of the landslide areas or (iii) the entire landslide areas. To predict the spatial distribution of the Mocoa landslides, we used two different statistical modeling techniques, namely: (i) logistic 132 133 regression (LR) and (ii) multivariate adaptive regression splines (MARS). LR has been widely 134 adopted to assess landslide susceptibility and, in particular, debris avalanche/flow landslides. Conversely, MARS has been rarely used in the field of landslide susceptibility mapping and, as far 135 136 as we know, has been employed to predict these types of slope failures only in one research study 137 (Rotigliano et al., 2018).

Therefore, the main objectives of this experiment were to: (i) test and compare three different criteria of landslide data sampling; (ii) evaluate and compare the ability of LR and MARS to predict the debris-avalanche and -flow landslides occurred in Mocoa.

# 141 2. Study area

The study area is located in the southeast portion of the Eastern Cordillera of the Colombian Andes 142 and falls in the watershed of the Mocoa River (Fig. 1). It extends for 58.3 km<sup>2</sup> and lies between 143 latitudes 01° 08' and 01° 13' N and longitudes 76° 38' and 76° 42' W. The city of Mocoa, capital 144 145 of the Departamento de Putumayo, is located in the southeast sector of the study area. Its urban area 146 is bounded to the east by the Mocoa river and is crossed by three of its tributaries: Taruca, Sangoyaco and Mulato. Precipitation in the study area occurs all year long and shows a unimodal 147 148 annual pattern with highest and lowest average monthly rainfall occurring in June and January, 149 respectively. The average annual rainfall is approximately 3715 mm.

The topography of the study area varies from flat to hilly to steep, with elevation ranging from 538 to 1893 m asl (Figs. 2 and 3). The western portion is characterized by moderately dissected mountain chains with very steep slopes (up to 77°). These are followed to the east by a hilly sector where topography is mainly controlled by structure and the slope angle is in the range 10–25°. Gentle-sloping (<10°) surfaces, which are formed by coalescing debris fans, occur on the right Mocoa riverside. A structure-controlled relief, which is located to the north of the Mocoa urban

156 area, acts as a natural barrier to protect the city from flooding events. Moreover, flat surface (i.e. 157 river terraces and alluvial plains) are located along the inter-mountainous sector of the Mocoa river. The study area is underlain by Jurassic igneous rocks and Cretaceous and Paleocene-Eocene 158 sedimentary rocks, which are covered discordantly by Quaternary unconsolidated deposits. To 159 160 explore the role of lithology as a predictor of landslide distribution, we prepared a map that includes the following lithological units: i) sedimentary rocks, mainly conglomerates; ii) sedimentary rocks, 161 mainly calcareous limestones; iii) igneous rocks mainly granites and monzonites; iv) alluvial 162 163 deposits; v) terraced alluvial deposits; vi) colluvial deposits; vii) debris-torrent deposits (Fig. 4). The igneous rocks, which are moderately to highly fractured, crop out in the western sector of the 164 165 study area. The La Tebaida fault separates these rocks to the east from the Paleocene-Eocene conglomerates of the Pepino Fm., whereas the limestones of the Villeta Fm. outcrop in the eastern 166 side of the Mocoa River. The quaternary deposits occupy the Mocoa river bed and form fluvial 167 168 terraces along its main valley. Moreover debris fans occur along the Mocoa tributaries while 169 colluvial deposits cover the foot of some slopes along the inter-mountain valleys.

# 170 **3. Materials and methods**

#### 171 *3.1. Landslide inventory*

The rainfall event considered in this study occurred between 10 pm of March, 31<sup>st</sup> and 1 am of April, 1<sup>st</sup>, 2017. The event was short but very intense with 130 mm of rain that fell in about 3 h. Such an amount of rain usually occurs in a ten days time-lapse. The rainfall event triggered a high number of debris avalanches and debris flows which propagated downslope as hyperconcentrated flows and debris floods.

The landslides occurred in the slopes that fed the streams of the Taruca, Sangoyaco and Mulatos rivers with a large amount of debris and blocks (with diameter up to six meters). These sediments were transported downslope and covered an area of approximately 3.2 km<sup>2</sup>, with average thickness of 4 m and a total volume of around 12 millions of cubic meters. In this work, we built a landslide inventory by 2D and 3D visual analysis of aerial photographs and of the satellite image dated April 10<sup>th</sup>, 2017, available on Google Earth. The inventory includes 1347 landslides (Fig. 5). Based on Hungr et al. (2014), two main types of movements were recognized: i) debris avalanches, which occurred on steep slopes and without confinement in an established channel and ii) debris flows, in which the movement developed along established paths, usually first or second order streams.

The mapped slope failures probably initiated as shallow slides or flows (Cruden and Varnes, 1996) and after moving a short distance transformed into debris avalanches or debris flows. However, considering that the objective of this experiment was to identify where slope failures potentially reaching the drainage axes and, eventually, the urbanized area of Mocoa, were more likely to occur, we decided not to differentiate between the two types of movements in the susceptibility mapping.

#### 192 *3.2. Predictor variables*

In this experiment, selection of landslide predictors was performed according to quality and resolution of the available data. As spatial distribution of the rainfall event was not available, only variables representing landslide preparatory causes were employed.

196 The landslide predictors were derived from a geological map of the area and a 5-m resolution raster 197 Digital Elevation Model (DEM), which provided sufficient resolution to properly map susceptibility 198 to landsliding in the Mocoa area. Conversely, the resolution of existing land cover and soil maps 199 were too coarse and thus not suitable for the analysis. All the variables were prepared as raster GIS 200 layers with 5-m cell size. The following predictors were derived from the DEM using SAGA-GIS 201 software (Conrad et al., 2015): elevation (ELEV), slope angle (SLOPE), northness (NORTH), 202 eastness (EAST), upslope slope angle (UPSLO), convergence index (CONV), topographic position 203 index (TPI), valley depth (VDEP) and topographic wetness index (TWI). These attributes were 204 selected as proxies for conditions and processes related to landslide occurrence (e.g., Wilson and 205 Gallant, 2000; Ohlmacher, 2007; Vorpahl et al., 2012). ELEV reflects the values of the available 5-206 m DEM and was selected because of its expected correlation with rainfall and vegetation spatial 207 distribution. SLOPE was calculated according to Zevenbergen and Thorne (1987). NORTH and 208 EAST were computed by applying cosine and sine transformations of slope aspect, respectively (Brenning and Trombotto, 2006; Conoscenti et al., 2016; Cama et al., 2017). NORTH, EAST, as 209 210 well as *ELEV*, may serve as proxies for seasonal wet/dry cycles of soils (Auslander et al., 2003). 211 UPSLO reflects average slope angle upstream from each position in the landscape. CONV (Koethe 212 and Lehmeier, 1996), which estimates to what extent neighboring cells point to the center cell, was calculated by setting a search radius of 50-m. To reduce detail and remove noise of the TWI (Beven 213 214 and Kirkby, 1979), a gaussian smoothing filter with search radius of 25-m was applied. CONV and TWI were included to account for runoff convergence/divergence and potential soil saturation, 215 216 respectively. TPI (Guisan et al., 1999) indicates the relative position of each cell and was calculated 217 by using a 100-m search radius. TPI and CONV values are negative on valley bottoms and positive 218 on ridges. VDEP reflects the maximum relative relief measured in cross-sections and thus is a 219 measure of local relief energy (Lóczy et al., 2012).

220 Moreover, we employed lithology (LITHO), distance form faults (FAULTD) and presence/absence of soil creep (CREEP) as predictor variables. LITHO was prepared by grouping the geological 221 222 formations that outcrop in the study area into 7 geological units, according to their expected 223 relationship with slope stability (Fig. 4). FAULTD was included to potentially reflect the degree of weakening of the bedrock due to tectonically active regional geological structures (Mathew et al., 224 225 2009; Cama et al., 2017). CREEP includes 71 areas (extending between 1 and 285 ha) affected by soil creep (Fig. 5), which in the region is favored by deforestation for agriculture and pasture. 226 227 *CREEP* was prepared by analyzing the same images employed to map the landslides.

### 228 *3.3. Statistical modeling*

Probability of debris-avalanche and -flow landslide occurrence at each 5-m grid cell in the study area was calculated by employing two statistical modeling techniques: logistic regression (LR; Hosmer and Lemeshow, 2000) and multivariate adaptive regression splines (MARS; Friedman, 1991). The statistical analyses were performed using the R software (R Core Team, 2017) with the packages "usdm" (Naimi, 2015), "sperrorest" (Brenning, 2012) and "earth" (Milborrow et al.,
2015).

LR is among the most frequently used statistical technique for spatial modeling of landslide 235 occurrence (Brenning, 2005) and it has been employed several times to predict specifically storm-236 237 triggered landslides (e.g., Chevalier et al., 2013; Heckmann et al., 2014; Lombardo et al., 2014, 2015; Cama et al., 2016; Trigila et al., 2015). On the other hand, MARS has been employed only 238 rarely for assessing landslide susceptibility (e.g., Vorpahl et al., 2012; Felicísimo et al., 2013; 239 240 Conoscenti et al., 2015, 2016; Pourghasemi and Rossi, 2016) and, as far as we know, this modeling technique was exploited for predicting landslides triggered by extreme rainfall events only in one 241 242 recent research paper (Rotigliano et al., 2018). LR and MARS can use both continuous and 243 categorical independent variables to estimate a response variable in the range 0 to 1, which can be interpreted as probability of an event occurrence. Both LR and MARS consist of an additive 244 245 combination of terms. Each term of the LR model is given by a linear regression of an independent 246 variable, which is fitted using the maximum likelihood method. In contrast to the assumption of LR 247 that coefficients of the predictors are constant across their ranges, MARS splits the range of the 248 independent variables into pieces, fitting to each of them a linear regression called "basis function" 249 (Vorpahl et al., 2012; Gómez-Gutiérrez et al., 2015; Conoscenti et al., 2018; Garosi et al., 2018). 250 MARS terms consist of a single basis function or a product of two or more of them. To reduce the 251 complexity of the LR models and avoid problems of overfitting, we adopted a bilateral stepwise strategy that selects only the most significant predictors. Accordingly, MARS models were 252 253 prepared by avoiding terms consisting of more than one basis function.

As both LR and MARS require the absence of multicollinearity (i.e. predictors should not be correlated with each other), we calculated the variance inflation factor (*VIF*) to measure the degree of correlation among the selected predictors. The R package "usdm" was employed to this aim. Following the "rule of 10", according to which a VIF > 10 reveals strong multicollinearity

258 (Heckmann et al., 2014; Jebur et al., 2014; Bui et al., 2015), we decided to include in the models all

the above cited variables, as their *VIF* values are well below the threshold.

#### 260 *3.4. Landslide data sampling*

In our experiment we used three different methods to select landslide data (Fig. 6). The three methods differ in the way event cells were selected. A single approach was instead employed to pick up non-event cells. These were randomly sampled from stable portions of the slopes, i.e. cells outside landslide areas (dataset STABLE). Landslide data samples were always prepared by maintaining a presence-absence ratio of 1:1. This choice was made in order to avoid prevalence in the samples (i.e. different proportion of event and non-event observations), which has been shown to affect the reliability of common accuracy statistics (Beguería, 2006).

In the first approach we selected a single cell at the highest point of each of the recognized landslide 268 crown-lines (hereafter named LIP: Lombardo et al., 2015; Cama et al., 2015, 2016), identifying a 269 270 total of 1347 event cells (dataset LIP). As model performance and robustness can be affected by the size of calibration and validation datasets (Brenning, 2005; Vorpahl et al., 2012), the same number 271 272 of event cells was selected also using the other two methods. In our second approach, event cells 273 were randomly sampled from the upper portions of the mapped landslides, which should reflect the conditions of the main source areas. These portions include the highest 10% of cells of each 274 275 landslide area (dataset SOURCE). In the third method, landslide cells were randomly picked up 276 from the entire landslide areas, which include initiation and accumulation zones (dataset MASS). In the second and third approach, we sampled as event cells a relative small fraction of pixels within 277 both upper portions (around 12% of 11,294 cells) and entire landslide areas (around 1.2% of 278 279 109,149 cells). In this way, we limited the effects of spatial autocorrelation between sampled cells, 280 which should be avoided when performing statistical prediction of landslide occurrence.

### 281 *3.5. Models training and validation strategy*

In order to evaluate their predictive ability, LR and MARS models were submitted to a k-fold spatial cross-validation strategy, which consists in extracting random training and test subsets from k spatially disjoint sub-areas. These were identified by using the k-means clustering algorithm (Ruß and Brenning, 2010; Goetz et al., 2015). As classic k-fold cross validation, the adopted approach uses k - 1 combined subsets at time for calibration and the remaining one for validation. The process is then repeated k times.

288 In our experiment we used k = 5 spatial cross-validation folds. To improve the robustness of the landslide predictions and mitigate the rare-events issue (Heckmann et al., 2014; Svoray et al., 2012; 289 290 Van Den Eeckhaut et al., 2012), multiple learning samples were extracted for each fold. More in 291 detail, our approach included the following steps, which were repeated for each of the five folds: i) sampling of ten balanced subsets from the four (i.e. k - 1) calibration sub-areas: ii) training a model 292 293 on each of the ten calibration subsets; iii) sampling of a balanced subset from the validation sub-294 area; iv) calculating a probability (P) of landslide occurrence in the validation subset by averaging 295 the scores obtained from the ten model runs; v) estimation of the model performance by averaging 296 the performance evaluated across each of the five folds. To assess the robustness of our approach, 297 this validation process was repeated 100 times for both LR and MARS models.

The prediction skill of the models was evaluated with the area under the receiver operating 298 characteristics (ROC) curve (AUC). The ROC curve plots for all possible cut-off values the true 299 300 positive rate TPR (sensitivity) versus the false positive rate FPR (1 – specificity). AUC values close 301 to 1 indicate perfect discrimination ability between the target variable levels (0 or 1) whereas values 302 close to 0.5 reflect no discrimination ability of the models. Intermediate AUC values were interpreted as acceptable, excellent or outstanding if higher than 0.7, 0.8 and 0.9, respectively 303 304 (Hosmer and Lemeshow, 2000). The Wilcoxon signed-rank test was applied to detect significant 305 differences in model performance. Differences at p-value < 0.01 were considered significant.

# 306 *3.6. Debris-avalanche and -flow landslide susceptibility maps*

307 A total of six debris-avalanche and -flow landslide susceptibility maps were prepared for the area of Mocoa by using LR and MARS with samples extracted from the datasets LIP, SOURCE and 308 309 MASS. The following procedure was applied for both the modeling techniques (i.e. LR and MARS) 310 and the three datasets (i.e. LIP, SOURCE and MASS): i) sampling of 100 balanced subsets made of 2694 cells; ii) calibration of a model for each of the 100 subsets of cells; iii) calculation of 311 probability (P) of landslide occurrence for each cell of the study area by averaging the scores 312 313 obtained from the 100 model runs. The range of debris avalanche/flow probability (0.00 - 1.00) was 314 classified into four equal interval levels (interval width: 0.25). As both LR and MARS models were 315 prepared using balanced datasets of event and non-event pixels, the score averaged from the 100 model runs should be interpreted as relative probability of debris avalanche/flow occurrence (Goetz 316 et al., 2015). 317

# **4. Results**

### 319 *4.1. Validation of the susceptibility models*

The predictive performance of LR and MARS evaluated for the three datasets is summarized in Fig. 7 by using six box plots. Each box plot shows the variability of 100 *AUC* values which were computed by means of the validation procedure described in Section 3.5. The average *AUC* values of LR and MARS calculated for the three datasets are all in the range 0.7 - 0.8, demonstrating an acceptable (*AUC* > 0.7) overall accuracy of the debris-avalanche and -flow landslide predictive models in the area of Mocoa. However, significant differences are revealed if we compare the performance of the models by applying the Wilcoxon signed-rank test.

The 100 MARS model runs validated on the dataset SOURCE (mean AUC = 0.788) demonstrated a significant (*p*-value <  $2.2e^{-16}$ ) higher accuracy than those tested on the dataset LIP (mean AUC =0.776), which in turns performed better (*p*-value =  $7.23e^{-07}$ ) than the MARS-MASS model runs (mean AUC = 0.768). On the other hand, no significant (*p*-value = 0.1355) difference of performance was measured between LR predictions of LIP (mean AUC = 0.748) and SOURCE (mean AUC = 0.750) datasets whereas LR-MASS model runs clearly exhibited the poorest predictive performance (mean AUC = 0.703). In all three datasets, MARS runs outperformed LR model repetitions (*p*-value <  $2.2e^{-16}$ ).

As regards performance variation, which was evaluated by means of the standard deviation (SD), MARS- and LR-LIP models exhibited very similar robustness (SD: 0.0075 vs 0.0076), whereas MARS predictive skill was slightly more stable when validated on the SOURCE (SD: 0.0098 vs 0.0117) and MASS datasets (SD: 0.0102 vs 0.0131). For any of the two modeling techniques, *AUC* values dispersion increases from LIP, through SOURCE to MASS datasets.

# 340 4.2. MARS and LR susceptibility maps

The six debris-avalanche and -flow landslide susceptibility maps prepared with MARS and LR using the three landslide datasets are plotted in Fig. 8. To help compare and evaluate the maps, Fig. 9 shows the relative frequency distributions of the datasets ALL (all pixels in the study area), STABLE, LIP, SOURCE and MASS over the four relative probability classes, for each of the six maps.

All the maps show smooth prediction patterns without abrupt changes where boundaries ofcategorical variables (i.e., lithology and soil creep presence/absence) occur.

MARS provides for all landslide datasets a smoother distribution of the susceptibility classes over the entire maps (dataset ALL), with a gradually decreasing frequency from the lowest to the highest class of landslide probability (*P*). Conversely, except for the SOURCE map, LR produces roughly similar frequency of *P* classes between 0.00 and 0.75 whereas the highest class occurs more rarely. Non-event pixels (dataset STABLE) are better discriminated by the MARS-SOURCE map, where

353 75% of the stable points has a low susceptibility level (i.e. P < 0.5) whereas only 67% has a P value 354 below 0.5 in the LR-LIP map.

Fig. 9 shows that, if we consider P = 0.5 as threshold to discriminate between pixels predicted as stable (P < 0.5) and unstable (P > 0.5), event cells of the datasets LIP, SOURCE and MASS are 357 predicted with excellent sensitivity (or true positive rate, TPR) by both MARS (TPR range: 0.77 - 0.78) and LR (TPR range: 0.76 - 0.78) maps. However, if we focus on the distribution of event 359 pixels with P > 0.5, Fig. 9 reveals that, except for LIP maps, they are roughly equally distributed 360 between the two highest levels of susceptibility in the MARS maps, whereas event pixels are less 361 frequent in the highest *P* class of LR maps.

# 362 **5. Discussion**

The spatial cross-validation revealed that the statistical predictive models provided an acceptable fit to the spatial distribution of the landslides occurred in the study area during the night between March 31 and April 1, 2017. Although MARS and LR models provided apparently comparable ability to discriminate between event and non-event pixels on the three landslide datasets (i.e. LIP, SOURCE, MASS), the Wilcoxon signed-rank test revealed significant differences of performance. MARS models, indeed, showed a better prediction skill in all landslide datasets, with a mean *AUC* difference of 0.044.

The existence of non-linear relationships between selected predictors and slope failures in the study area can explain the better fit of MARS models to the landslide datasets. LR models are indeed based on linear relationships holding over the entire range of the explanatory variables whereas MARS is able to split the range of predictors into pieces and fit to each of them a different linear regression. In this way, MARS produces a smooth response curve which may better reproduce the relationships between predictors and landslide occurrence.

The better performance of MARS in our study area is consistent with the findings of few other previous works that compared the ability of LR and MARS in predicting landslide occurrence. A similar difference of mean *AUC* values between LR and MARS (0.848 against 0.889) was found by Conoscenti et al. (2015) in a catchment of Sicily (Italy) affected by earth-flow landslides. Roughly the same difference of prediction skill was revealed by internal cross validation that was applied to an inventory of shallow translational landslides in the Andes of Southern Ecuador (Vorpahl et al., 2012). A slightly better performance of MARS (*AUC* = 0.782) with respect to LR (*AUC* = 0.775)

was found by Pourghasemi and Rossi (2016), who compared the ability of four statistical techniques to predict landslides occurred in the Mazandarn Province (Iran). On the other hand, LR and MARS achieved the same accuracy (AUC = 0.76) in predicting the landslide spatial distribution in Guipúzcoa province (Spain; Felicísimo et al., 2013). Also, Vorpahl et al. (2012) found no significant difference of predictive performance when they applied an external cross validation to their data.

The results of our experiment and those of the above cited papers suggest that the role of a physical factor in controlling a geomorphological process can be better represented by a series of local functions rather than a single linear regression. In other words, simple predictive models, which are typically employed to explain relationships between factors and geomorphological processes, are less accurate than complex models, such as those provided by MARS.

As regards the different landslide datasets employed in this experiment, we found a significant lower accuracy when predictive models were calibrated and validated using event pixels sampled from the entire landslide areas (i.e. dataset MASS). The best fit to landslide data was found when we used MARS with event cells sampled from the highest 10% of cells of each landslide area (dataset SOURCE) whereas no significant difference of performance was detected when we trained and tested LR models with datasets LIP and SOURCE.

400 The overall better discrimination ability of the LIP/SOURCE pixels can be explained considering 401 that their terrain conditions are more specific than those of the MASS cells. The latter indeed may 402 occur on the initiation, transport and deposition zones of debris-avalanches and -flows which can be 403 characterized by heterogeneous conditions (e.g., altitude, slope, convergence index, TPI, TWI or 404 valley depth) within each individual landslide area, whereas LIP/SOURCE pixels should likely 405 have more homogeneous conditions. These results are consistent with those of Regmi et al. (2014), 406 who found that accuracy of landslide predictive models was slightly better when developed on 407 samples obtained from scarps of different types of landslides (i.e., debris flows, debris slides, rock 408 slides and soil slides) occurred in western Colorado, USA. They explain their findings assuming 409 that landslides in their study area were mainly due to unfavorable condition at the slope heads and, 410 thus, data sampling from scarps instead of landslide masses reduced uncertainties. On the other 411 hand, Vorpahl et al. (2012) found better performance in predicting landslide deposition zones than initiation zones. As possible reason of this result, they assumed that deposition zones mainly occur 412 413 close to bottom of small valleys which can be described by the selected terrain attributes better than 414 the open slope where initiation zones tend to be located. In other words, also Vorpahl et al. (2012) 415 assume that more specific terrain conditions of landslide data provide more accurate predictive skill 416 of the models.

417 Although apparently similar, the six debris-avalanche and -flow landslide susceptibility maps 418 obtained from MARS and LR models have important differences, which are revealed by the 419 histograms of Fig. 9. Based on the latter, we can infer that, also across the entire study area, MARS performed better than LR and both modeling techniques achieved better prediction skill when 420 421 employed to discriminate between stable and unstable pixels of the dataset SOURCE. We consider 422 MARS maps better than LR maps because of the following reasons. First, frequency of susceptibility levels of MARS maps gradually decreases from lowest to highest ones, which is a 423 424 desirable quality for landslide susceptibility maps. Indeed, as landsliding is normally a rare-event 425 and thus ratio of event to non-event cells can be very low, maps with high frequency of susceptible pixels can suffer from high false positive rates. Second, using P < 0.5 as threshold to identify non-426 susceptible pixels, MARS maps are characterized by significantly higher specificity (or true 427 428 negative rate) on all analyzed landslide datasets. Third, MARS maps have higher percentage of event pixels with P > 0.75. Similarly, it is reasonable to infer that dataset SOURCE yielded better 429 430 MARS and LR maps because, although roughly the same true positive rate (P threshold = 0.5) was observed for all landslide datasets, the percentage of event pixels with P > 0.75 was definitely 431 432 higher. Furthermore, a higher percentage of stable pixels with P < 0.5 occur in MARS- and LR-433 SOURCE maps.

The results of this experiment demonstrated that a stochastic approach can be used by geomorphologists to achieve reliable prediction of landslides triggered by an extreme rainfall event in a mountainous environment. The approach described in this paper could be useful particularly in developing countries which have great difficulty in affording the high costs of structural measures to reduce landslide risk. This method allows for identifying areas prone to landsliding and thus could provide a valuable aid to a rational land use planning aimed at minimizing victims and economic damage.

441

# 442 6. Concluding remarks

443 In this experiment, we employed a stochastic approach to predict the spatial distribution of the 444 debris-avalanches and -flows triggered by heavy rainfalls occurred in the area of Mocoa on April 1<sup>st</sup>, 2017. Multivariate Adaptive Regression Splines (MARS) and Logistic Regression (LR) were 445 exploited as modeling techniques. A set of nine terrain attributes, in addition to lithology, distance 446 447 from faults and presence/absence of soil creep processes were used as predictor variables. 448 Validation of the models was performed by using k-fold spatial cross-validation and by calculating 449 AUC values of 100 MARS and LR model repetitions applied to balanced samples of event and non-450 event pixels. The calibration and validation samples were extracted from three different landslide datasets which contain the highest point of each landslide crown-line (dataset LIP), the highest 10% 451 452 of cells of each landslide area (dataset SOURCE) or the entire landslide area (dataset MASS).

453

The following conclusions can be drawn for the Mocoa study area on the basis of the validation of the models and the analysis of six susceptibility maps which were obtained by using MARS and LR with the three landslide datasets.

457 1. The overall accuracy of our models can be considered acceptable (AUC > 0.7);

458 2. MARS models and maps exhibited a better ability to discriminate between event and non-event459 pixels;

3. Both MARS and LR demonstrated better accuracy when employed to predict landslide sourceareas;

462 4. The relationships between predictors and debris-avalanche and -flow landslides are more
463 accurately reproduced by piecewise linear regressions rather than individual linear functions
464 holding over the entire predictor range.

The approach employed in this experiment is relatively simple, rapid and can be reproduced by using free software and data usually available. It can be used to prepare debris-avalanche and -flow landslide susceptibility maps which can help policy makers and land managers of Colombia to establish preventive measures and mitigate risks.

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