



Article On the Finite Element Modeling of the Lumbar Spine: A Schematic Review

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Abstract: Finite element modelling of the lumbar spine is a challenging problem. Lower back pain is among the most common pathologies in the global populations, owing to which the patient may need to undergo surgery. The latter may differ in nature and complexity because of spinal disease and patient contraindications (i.e., aging). Today, the understanding of spinal column biomechanics may lead to better comprehension of the disease progression as well as to the development of innovative therapeutic strategies. Better insight into the spine's biomechanics would certainly guarantee an evolution of current device-based treatments. In this setting, the computational approach appears to be a remarkable tool for simulating physiological and pathological spinal conditions, as well as for various aspects of surgery. Patient-specific computational simulations are constantly evolving, and require a number of validation and verification challenges to be overcome before they can achieve true and accurate results. The aim of the present schematic review is to provide an overview of the evolution and recent advances involved in computational finite element modelling (FEM) of spinal biomechanics and of the fundamental knowledge necessary to develop the best modeling approach in terms of trustworthiness and reliability.

Keywords: finite element analysis; spinal column; biomechanics; modelling; lumbar spine; computational simulations

1. Introduction

The study of spine biomechanics has evolved over decades. Computational simulations provide a critical tool in light of the difficulty and complexity required to perform in vivo experiments on human spinal columns [1–3]. The biomechanics of the spine are extremely complex, and many different anatomical components are involved. In computational simulations, these components are modelled separately, each one being associated with specified modelling features according to their biomechanical response and constitutive model relationships [4,5]. A complete finite element (FE) analysis of the spine requires the modelling of bone components, intervertebral discs, facet joints, and seven major spinal ligaments, as well as the cartilaginous endplates [5–8].

The bone component consists of three parts: the cancellous bone (the innermost part), cortical bone (the outermost part), and posterior bony elements (which represent the vertebral arch where the bone marrow is inserted) [7]. The intervertebral disc is divided into the nucleus pulposus and the fibrous annulus, composed of the annular ground substance and reinforcing fibers. The three distinct parts of the disc should be modelled to simulate the correct biomechanics of the spinal column [7,8]. Therefore, the facet joint needs to be represented in order to account for the relative movement between the spinal processes of the two vertebrae. The seven major ligaments represented in the FE model are the anterior longitudinal ligament (ALL), posterior longitudinal ligament (PLL), interspinous ligament (IL), intertransverse ligament (TL), flavian ligament (FL), supraspinous ligament (SL), and capsular ligament (CL) [5,6]. Ligaments contribute to spinal stabilization by



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). establishing the follower force path-way, which passes through the rotation centers of the vertebrae [9–12]. In an FE model of the lumbar spine, all these different components must be considered and modelled in order to ensure that the model is as reliable as possible. Dreisharf et al. [13] compared eight different finite element studies [14–21] of the spine in a very comprehensive study. The eight element models were chosen according to the importance of the research carried out by the authors. The aim of the comparison was to observe whether it was possible to develop a prediction model of the lumbar spine's behaviour under certain loading conditions. From the different studies, a certain homogeneity and average of the results was observed. This homogeneity was achieved as a result of the correct and complex modelling of the different anatomical parts modelled by the authors in a comprehensive manner.

The target of most biomechanical spine simulations is to evaluate the spinal loading conditions under physiological and pathological conditions [13,22,23]. Intradiscal pressure (IDP) and displacement measurements are the main parameters for analyzing the intervertebral disc mechanical response during the compression phase. Other analysis factors are the radial and circumferential internal stresses and the stretching in response to loading stresses. During flexion, extension, lateral bending, and rotation movements, the range of motion (ROM) is analyzed and examined [13,22–24]. The final step of a computational simulation is to validate the so obtained finite element results using experimental testing. There are several types of in vivo experiments specific to the characterization and quantification of the mechanical response of the anatomical components [25–34]. Several experiments involve simply testing the intervertebral disc among two pairs of vertebrae, then subjecting these to different stress states [25,26,29,30,33]. Other experiments concern the muscular trunk and the generation of follower forces. In such experiments, specimens are subjected to a simple compressive force and then a follower force, through which the obtained results can then be compared. The follower force stabilizes the spine by increasing the load resistance and decreasing the IDP [9–12,28]. Other experiments investigate the spinal response subjected to different loading conditions, while keeping in mind all other different anatomical components such as ligaments and facet joints as these are fundamental for stabilization of the spine under compression [27,28,31,32,34].

The aim of this schematic review is to present the modelling methods of the spine in computational simulations, emphasizing the different anatomical components in relation to mechanical modelling, loading conditions, model verification, and validation approaches. The article proposed by Alawneh et al. [35] is used as a benchmark for the framework adapted in the present schematic review.

2. Materials and Methods

2.1. Literature Search Strategy

A careful and comprehensive search in terms of data validation and quantization was conducted using databases in the scientific and engineering domains. The search aimed to identify research works of any nature having finite element analysis used to examine the biomechanics of the lumbar spine as a central topic. The search combined two databases, SCOPUS and Web of Science. The search protocol involved searching by the following keywords related to the lumbar spine: computational, modelling, model, biomechanics, finite element, spinal, which were added neatly each time. The initial search protocol involved five keywords, then the output was filtered to present the most innovative findings.

2.2. Study Selection

Following the search protocol to four keywords, several inclusion and exclusion criteria were chosen. Hence, a further selection was made within the article collection process by searching for additional keywords to restrict the number of identified articles, reaching a total of nine keywords. Thus, the amount of articles to be investigated was reduced to topics including finite element modelling (FEM) of the lumbar spine. The exclusion criteria used

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were the following: FEM unrelated to the lumbar spine, articles lacking information on how they modelled the lumbar spine, and absence of the FE analysis and validation processes.

2.3. Data Extraction

The main information types extracted were on the modeling of the individual anatomical component of the lumbar spine, i.e., the cortical, and cancellous bone, posterior bone elements, cartilaginous endplate, annular ground substance, annular collagen fibers, nucleus pulposus, ligaments, boundary and loading conditions, and follower forces. Data were extracted from simulations, with constitutive models considered for each individual component. Both the material information and FE modeling approaches were considered.

3. Results

3.1. Research Strategy

The search protocol identified a total of 297 articles from Web of Science and 96 from Scopus through five keywords. After identifying and eliminating 53 duplicates, further screening of the articles was carried out by adding four more keywords, reaching 117 total articles. The next step involved a process of screening the articles by title and abstract while eliminating articles according to the exclusion criteria. A final total was reached of 20 articles that satisfied the inclusion and exclusion criteria. Finally, a further 11 articles were added from a bibliographic search cross-referenced with articles identified by keywords and inclusion criteria, for a total of 31 articles [14,15,21,24,36–62] used in the last step of data extraction and analysis. The articles extracted from the two databases were obtained in September 2022, and the data were processed over the following two months using the workflow already set out.

Figure 1 provides an illustration of the workflow of the study's screening process. Table 1 shows the keywords, inclusion criteria, and exclusion criteria.

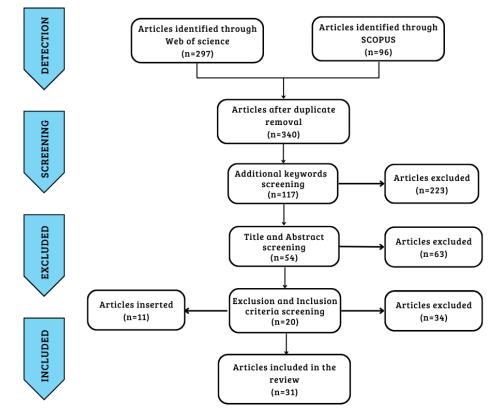


Figure 1. Prism diagram of research strategy workflow.

| Keywords, Exclusion Criteria, and Inclusion Criteria | N° Articles |
|---|-------------|
| TITLE-ABS-KEY ((lumbar AND spine) AND (computational) AND(modelling) AND (model)) | 393 |
| After duplicate removal | 340 |
| TITLE-ABS-KEY ((lumbar AND spine) AND (computational) AND (modelling) AND (model) AND (biomechanics)) AND (finite AND element)) | 117 |
| After reading and screening of abstracts and title | 54 |
| Additional papers | 11 |
| Exclusion and inclusion criteria, according to presence of all data about modelling of every single anatomical part of the lumbar spine (Young's modulus, constitutive model, density, Poisson coefficient, type element meshing) | 31 |

Table 1. Keywords, inclusion criteria, and exclusion criteria.

3.2. Analysis of Extracted Data

The characteristics of the investigated studies are summarized in Tables A1–A6 for all 31 included articles shown in Appendix A.

Figure 2 shows the network between the main items identified in the initial dataset of 393 items as visualized using VOSviewer Software (Version 1.6.18, Centre for Science and Technology Studies, Leiden University, Leiden, The Netherlands).

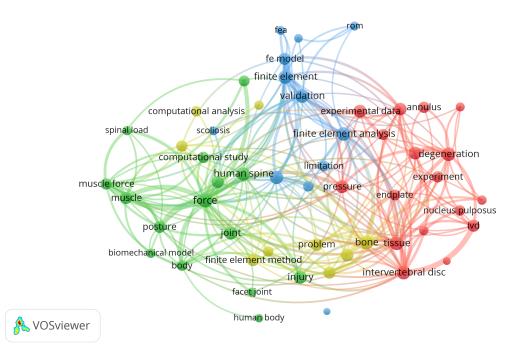


Figure 2. Network visualization for title, abstract, and keywords.

Our analysis of the network was carried out in two ways: a co-occurrence analysis, where the distance between each pair of items is calculated based on the number of documents in which the pair appears together, and a bibliographic coupling analysis, where the closeness of each pair of items is determined by the number of references they share.

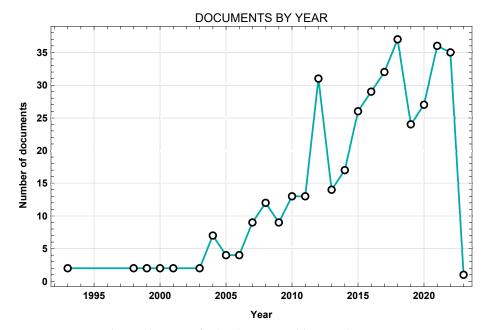


Figure 3 shows the works from the initial dataset sorted by year.

Figure 3. Network visualization of title, abstract, and keywords.

The inclusion and exclusion criteria concerned the presence of data on the modelling of the different anatomical components of the lumbar region, including the cortical bone, cancellous bone, posterior bone elements, cartilaginous endplate, annulus ground substance, annular collagen fibers, nucleus pulposus, ligaments, and follower load.

3.3. Modelling of the Different Components

Table 2 shows the most widely used modelling approaches for the anatomical components of the spine [14,15,21,24,36–62].

| Table 2. FE modelling and elements of the different anatomical components [14,15,21,24,36–62] | Table 2. FE modellir | g and elements of the different anat | tomical components | [14,15,21,24,36-62] |
|--|----------------------|--------------------------------------|--------------------|---------------------|
|--|----------------------|--------------------------------------|--------------------|---------------------|

| | Anatomical Components | Finite Element Modelling | Finite Elements | | |
|--|--------------------------------|---|----------------------------|--|--|
| Vertebral body | Cortical and Cancellous Bone | Isotropic Elastic Transversely Elastic Poroelastic behaviour | Solid | | |
| Vertebral body Intervertebral disc | Nucelus Polpous | Isotropic Elastic Incompressible Fluid Empty cavity Hyperelastic behaviour | Solid Fluid | | |
| | Annular Ground Substance | Hyperelastic behaviour | Solid | | |
| | Collagen Fibers | Isotropic Elastic Non linear behaviour Based on $\sigma - \varepsilon$ curve | Truss Beam Connector | | |
| | Ligaments | LigamentsIsotropic ElasticLigamentsIsotropic varying on strain rate Non linear behaviour Based on $\sigma - \varepsilon$ data curve | | | |
| | Cartilagineus Endplate | Isotropic Elastic | Solid | | |
| | Facet Joints | Isotropic Elastic Hyperelastic behaviour Surface to surface contact Frictionless Unidirectional gap contact | Solid Contact | | |

Cancellous and cortical bone are generally modelled through linear elastic or transversely isotropic behaviour. Poroelastic modelling represents a different modelling approaches. Concerning the posterior bony elements, they are almost always modelled through linear elastic behaviour.

3.3.2. Intervertebral Disc

The nucleus pulposus can be modelled in different ways. It can be represented as an empty cavity filled with fluid, or by modelling its elastic behaviour as an incompressible material. Even if the nucleus is modelled with hyperelastic behaviour, as a rule the Neo-Hookean, Mooney–Rivlin, or Ogden model is used. Therefore, the annulus ground substance is mostly subdivided into eight or more concentric layers of fibers, starting from the outermost layer and moving to the innermost layer by varying orientation and thickness. The annular ground substance is modelled with hyperelastic behaviour using with a Neo-Hookean, Mooney–Rivlin, or Ogden model. The annular collagen fibers are modelled in terms of their nonlinear behavior or by using elastic isotropic material properties that vary with each layer.

3.3.3. Ligaments

The seven major ligaments can be treated as connector, truss, or beam elements. The constitutive models used are usually nonlinear models or isotropic elastic response models with a varying Young's modulus according to the strain rate. Other approaches exploit non-linear $\sigma - \epsilon$ curves based on experimental data.

3.3.4. Cartilaginous Endplates and Facet Joints

The cartilaginous endplates are modelled through isotropic elastic or hyperelastic behaviour. Facet joints are often modelled through simple surface-to-surface contacts, or alternatively as uni-directional gaps or other types of contact (i.e., tie contact conditions or constraints). In addition, facet joints are modelled with a certain thickness and with isotropic or hyperelastic elastic properties.

3.4. Boundary-Loading Conditions and Validation

With respect to boundary conditions, the inferior surface of the L5 vertebra or S1 level is blocked, preventing it from moving vertically along the loading direction while being left free to rotate in other directions [14,15,21,24,36–62].

Concerning the loading conditions, a compression pre-loading conditions is often applied [13–15,21–24,36–62]. The pre-load is usually a follower pre-load, though it can be a compressive load as well, mimicking the natural compressive load condition during upright standing. Other approaches to loading involve lateral bending and the extension or flexion moments. A downward vertical displacement setting may be used to simulate the effect of compression, and thereby the effect on intradiscal pressure. Torsion is applied as well.

The action of the muscular trunk is schematized through the follower load generated by the spine. The path for the follower load can be created as a force passing through the instantaneous centers of spinal rotation. In a different way, it can be ensured that the force path follows the curvature of the spine; the follower force may be ignored for specific applications where this does not need to be simulated.

The validation process of FE simulations generally follows the results obtained experimentally from samples of human vertebrae, though tests involving animal specimens can be a viable option as well. The experiments used for validation differ widely among different studies according to their specific testing characteristics and available in-house options. A number of experiments concern loading conditions on the spinal column based on the action of muscle forces. Other experiments involve the effects that a given loading condition has on the IDP or facet joints, while other allow for full investigate of the biomechanical response and stiffness of the seven main spinal ligaments and the collagen fibers of the intervertebral disc.

Figure 4 shows several of the principal loading conditions to which the spine is subjected.

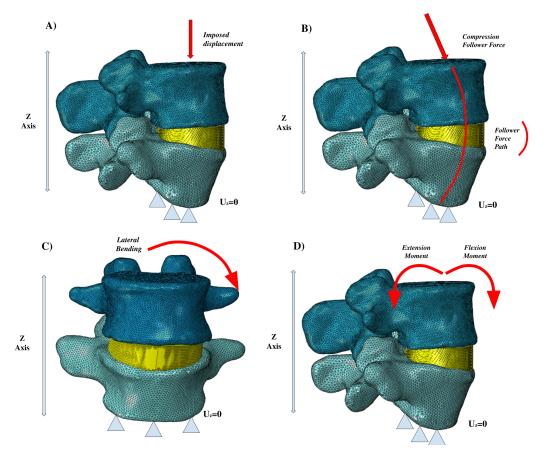


Figure 4. Different loading conditions: (**A**) imposed displacement, (**B**) compression follower force, (**C**) lateral bending, (**D**) extension and flexion moments.

4. Discussion

The present study involved a schematic literature review conducted to fully analyze the existing literature about FE modelling of the lumbar spine. This work involved number of different steps. First, a search was conducted through the Web of Science and Scopus databases in order to find the most relevant works, using specific keywords to identify the most innovative approaches. A laborious screening process followed, starting with the removal of duplicates, then further screening through additional keywords, title, and abstract. A total of 31 articles were included in the final review, each of which was exhaustively examined. The nature of the selected articles was assessed through the VosViewer software. Figure 2 demonstrates how most current investigations have focused on topics aligned with the database research concerning the following: the lumbar spine, FE analysis, computational analysis, spinal load, validation, etc. Network visualization was essential for verifying the relevance of the resulting database. It can be clearly seen that the obtained database suits the desired search parameters. Afterwards, the publication dates were analyzed. Figure 3 highlights the works in the source database, showing that they cover a wide temporal interval ranging from 1992 to 2022. This range allowed us to observe both the evolution and the consistency of computational modelling techniques of the lumbar spine over the years.

The final step was the extraction of data from articles presented in this review. All articles were carefully examined in order to extract the researchers' choices in modelling the different parts of the considered anatomical area along with the numerical

techniques used for the boundary conditions, loading conditions, and model validation process [14,15,21,24,36–62]. All of this information is included in Tables A1–A6. These tables show the modelling proposed by the different research groups, as well as their approaches to FE. The information was extracted separately in relation to the cortical bone, cancellous bone, posterior bone elements, cartilaginous endplates, annulus ground substance, annular collagen fibers, nucleus pulposus, ligaments, and follower load. Based on a careful analysis and data extraction process, the main models used by researchers were stratified and presented; see Table 2.

Cortical bone and cancellous bone are the anatomical components that exhibit the most similar numerical approaches. Isotropic elastic modelling represents a good assumption, though modelling with transverse behaviour would be the best choice to simulate the unique characteristics of cortical bone and the trabecular architecture. Posterior bone segments can be schematized simply through linear elastic behavior, and is used by most researchers. The cartilaginous endplates can be schematized by linear elastic behavior or even as a hyperelastic Neo-Hookean material. The computational results obtained from Von Mises stress analysis or from verification of the component displacement allows for a certain homogeneity in the literature to be observed from the data obtained from simulations in relation to these models.

The intervertebral disc is the most challenging to model because of its three different components, i.e., the nucleus pulposus, annular ground substance, and annular collagen fibers. Overall, the disc exhibits viscoelastic behaviour, which means that hyperelastic modelling is the most appropriate. Many different hyperelastic models are used for the annular ground substance and the nucleus pulposus; among the most common are the Mooney-Rivlin and Neo-Hookean models. Other hyperelastic models are used as well, though the Mooney–Rivlin and Neo-Hookean aprroach are both effective in capturing the biomechanical disc response. Concerning the modeling of the annulus collagen fibers, they can be modelled in a number of different ways. Because these fibers provide important mechanical strength to the annulus, the most appropriate modelling approach is the isotropic linear elastic material model. Nonlinear material behaviour has been used as well. The final results of the computational simulations show that, when using the same modelling, the results of Von Mises stresses, displacements, and intradiscal pressure analysis are quite similar to each other. Different results can be observed depending on the constitutive model chosen for modelling based on whether more or less account is taken of the elasticity or viscoelasticity of the component, whether possible damage to the disc is considered, and other situations.

All seven spinal ligaments must be modeled, as they are essential in stabilizing the spine. The most common modelling approach is a linear elastic approach using different Young's moduli as the strain rate changes. Modelling based on nonlinear behavior can be used as well, although the lack of experimental data poses challenges when using this approach. The literature presents a number of different approaches to modelling of the facet joints. Several studies suggest using hyperelastic behavior, while others use simple surface-to-surface contact or unidirectional gap contact.

For loading conditions, Figure 4 shows the main loading conditions of the vertebral segments. The follower force is among the most important, and is often schematized by researchers based on the realization that one path line passes through all the rotational centers of the vertebrae. Lastly, the loading conditions of lateral bending, flexion, extension, and axial rotation are common to almost all of the studies we investigated. The validation process generally uses results obtained experimentally on samples of human vertebrae, although tests involving animal specimens can be a viable option. It is crucial to have the opportunity to computationally simulate the biomechanical behaviour of the spine because of the practical and economic difficulties in performing in vivo experiments. One important tool is statistical shape modelling (SSM), which is used to generate a 3D atlas of the spine that can be deformed based on specific boundaries to develop new anatomic models [63]. Among the different approaches used for validation [25–34,62,64],

Wilke et al. [30] performed an experiment on human vertebrae and then simulated and verified the effect of the muscular forces on spinal loading. This was done in order to understand how the muscular loading impacted intradiscal pressure by pure flexion and extension, lateral bending, and lateral rotation tests. Yamamoto et al. [34] implemented ad hoc experimental tests to investigate the stresses incurred by the facet joints during normal bending and extension loading conditions. Meanwhile, other researchers [62] have pursued validation concerning the collagen fibers of the annular ground substance to better explain the stiffness and response of the fibers under different loading conditions. Several different experimental approaches have been used to verify the biomechanical response of the spine considering the response of the ligaments, disc, and facet joints [25,62,64].

Based on our literature review, general guidelines to modeling the lumbar vertebral body can be identified to improve the current scientific literature. Cortical and cancellous bone should be schematized through transversely elastic behavior in order to underline their true mechanical responses. Posterior bone segments can either follow the same modeling as cortical and cancellous bone or be schematized through linear isotropic elastic behavior. Modelling realised in this way guarantees the truthful modelling of the biomechanical behaviour of the components. The intervertebral disc is the component most likely to vary in modelling, depending on whether or not all components are present. The disc should be correctly schematized as the annulus ground substance, annular collagen fibers, and nucleus pulposus in order to properly simulate its biomechanics. Mooney-Rivlin hyperelastic modeling works quite well for the nucleus pulposus and annular ground substance, though future investigations might consider using different constitutive behaviours to considering the viscoelastic creep characteristics of the disc, as suggested by Sciortino [65], as well as its poroelastic behavior. For future studies, the intervertebral disc could be modelled through a poroelastic model, considering that its precisely biphasic nature is guaranteed by the presence of the "liquid" part of the nucleus pulposus and the "solid" part of the fibrous ring. Concerning spinal ligaments, all studies proceed with modeling in a similar way using elastic or nonlinear behaviour. However, there is variability in the results of simulations depending on the ligament modelling choices. Viscoelastic models have not yet been widely used in the literature to simulate the mechanical response of the ligaments, e.g., the use of combined springpot, spring, and dashpot models to simulate their viscoelastic nature, even though this has already been sufficiently demonstrated in the literature. Thus, future modeling might investigate better constitutive modelling approach to account for these viscoelastic characteristics. Considering the intrinsically viscoelastic nature of these biological tissues when modelling the spinal column could ensure the accurately simulation of the the kinematics, dynamics, and static behaviour of the spine. It should be noted that the present study does have a number of limitations. First, the choice of keywords, although reasoned, could represent a limitation on the selection of the articles. Changing a keyword distorts the search results in the database by including more or fewer articles. A further limitation concerns the data extracted from the articles. Data were extracted only from those articles that presented all modelled anatomical components of interest. Those articles without a clear description of anatomy modelling methods were excluded. By excluding articles with an absence of data, the screening process certainly eliminated articles with a valid invoice. Future studies might consider adding more databases and decreasing the number of keywords in order to obtain a more detailed and comprehensive database.

5. Conclusions

This study consolidates the existing knowledge and methodologies pertaining to finite element modeling of the lumbar spinal column. The literature shows that there is a wide range of different methodologies available to schematize the lumbar spine. The result achieved by this review was to provide an overview of the different methodologies, and then combine them into a general framework based on which seem most appropriate for obtaining a well-established, reliable, and truthful FEM model. The outcome achieved

by this review enables us to lay the groundwork for future research on FEM modelling of the lumbar spine, which can be realized using the notions learned and shared through this review work. Comparative insight into the different methods used is helpful in creating guidelines for future research in this field. Furthermore, it should be noted that the differences between the methodologies observed in this review is a result of different resources, research purposes, and desired levels of accuracy in the analysed studies. Future research should be based on the results extracted from the literature, including consideration of the viscoelastic characteristics of the disc and ligaments that are not fully involved in modeling. Therefore, the goal of our future work will be to precisely implement new methodologies that consider these aspects, which remain neglected today.

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Data Availability Statement: The data presented in this study are available on request from the corresponding author. The data are not publicly available for to ethical reasons.

Conflicts of Interest: The authors declare no conflicts of interest.

Appendix A

Tables A1–A6, shown below, were created from information extracted from the articles included in the review about the constitutive model and element type used for the modelling of the cortical bone, cancellous bone, posterior bony elements, cartilaginous endplates, annular ground substance, annular collagen fibers, nucleus pulposus, ligaments, facet joints, and follower force.

| | Chen et al. (2001) [36] | | | Schimdt et al. (2006) [37] Chen et al. (2008) [38] | | | | | Rohlmann et al. (2009) [| 39] | Zander et. al. (2009) [40] | |
|---|---|---|--|--|--------------------|---|---|-------------------|---|--------------------|--|------------------|
| Anatomical Component | Constitutive Model | | Element Type | Constitutive Model | Element Type | Constitutive M | odel | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type |
| Cortical Bone | Isotropic Elastic E = 12,000 MPa $\nu = 0.3$ | | 8-node Solid | $\begin{array}{l} \label{eq:constraints} \hline {\bf Transversely Isotropic} \\ E_{xx} = 11300 \ {\rm MPa} \\ \nu_{xy} = 0.484 \\ E_{yy} = 11,300 \ {\rm MPa} \\ \nu_{xz} = 0.203 \\ E_{zz} = 22,000 \ {\rm MPa} \\ G_{xy} = 3800 \ {\rm MPa} \\ G_{yz} = 5400 \ {\rm MPa} \\ G_{xz} = 5400 \ {\rm MPa} \end{array}$ | 8-node Solid | $\begin{array}{c} \mbox{Transversely Iso} \\ E_{xx} = 11,300 \ M \\ v_{xy} = 0.48 \\ E_{yy} = 11,300 \ M \\ v_{xz} = 200 \ M \\ G_{xy} = 22,000 \ M \\ G_{xy} = 22,000 \ M \\ G_{yy} = 5400 \ M \\ G_{yz} = 5400 \ M \\ G_{yz} = 5400 \ M \end{array}$ | IPa Pa Pa Pa | 8-node Solid | Isotropic Elastic E = 10,000 MPa $\nu = 0.3$ | 8-node Solid | Isotropic Elastic E = 10,000 MPa $\nu = 0.3$ | 8-node Solid |
| Cancellous Bone | Isotropic Elastic E = 100 MPa $\nu = 0.2$ | | 8-node Solid | $\begin{array}{l} \label{eq:constraints} \hline {\bf Transversely Isotropic} \\ E_{XX} = 140 \ {\rm MPa} \\ v_{Xy} = 0.450 \\ E_{yy} = 140 \ {\rm MPa} \\ v_{yz} = 0.315 \\ E_{zz} = 200 \ {\rm MPa} \\ v_{Xz} = 0.325 \\ G_{Xy} = 48.3 \ {\rm MPa} \\ G_{xz} = 48.3 \ {\rm MPa} \\ G_{xz} = 48.3 \ {\rm MPa} \end{array}$ | 8-node Solid | $\begin{array}{c} {\rm Transversely Iso} \\ E_{xx} = 140 {\rm Mi} \\ v_{xy} = 0.450 \\ E_{yy} = 140 {\rm Mi} \\ v = 0.315 \\ E_{zz} = 200 {\rm Mi} \\ v = 0.315 \\ G_{xy} = 48.3 {\rm Mi} \\ G_{yz} = 48.3 {\rm Mi} \\ G_{xz} = 48.3 {\rm Mi} \end{array}$ | ropic a a a 2 a 2 a | 8-node Solid | $\begin{array}{l} \mbox{Transversely Isotropic}\\ E_{xx} = 140 \ \mbox{MPa}\\ v_{xy} = 0.450\\ E_{yy} = 140 \ \mbox{MPa}\\ v_{yz} = 0.315\\ E_{zz} = 200 \ \mbox{MPa}\\ v_{xz} = 0.315 \end{array}$ | 8-node Solid | Transversely Isotropic $E_{xx} = 140 \text{ MPa}$ $E_{yy} = 140 \text{ MPa}$ $E_{zz} = 200 \text{ MPa}$ $v_{xz} = 0.315$ | 8-node Solid |
| Posterior bone elements | Isotropic Elastic E = 3500 MPa $\nu = 0.25$ | | 8-node Solid | Isotropic Elastic E = 3500 MPa $\nu = 0.25$ | 8-node Solid | Isotropic Elas E = 3500 MP $\nu = 0.25$ | tic a | 8-node Solid | Isotropic Elastic E = 3200 MPa v = 0.25 | 8-node Solid | Isotropic Elastic E = 3500 MPa $\nu = 0.25$ | 8-node Solid |
| Cartilaginous Endplate | - | | - | Isotropic Elastic E = 23.8 MPa $\nu = 0.4$ | 8-node Solid | Isotropic Elas E = 24 MPa $\nu = 0.4$ | tic | 8-node Solid | Neo-Hokean $c_1 = 0.3448, d_1 = 0.3$ | 8/6-node Solid | Neo-Hokean $c_1 = 0.3448, d_1 = 0.3$ | 8-node Solid |
| Annular ground substance | Isotropic Elastic E = 4.2 MPa v = 0.45 | | 8-node Solid | | 8-node Solid | Mooney-Rivl $c_1 = 0.42$ $c_2 = 0.105$ | in | 8-node Link | Neo-Hookean <i>c</i> = 0.3448, <i>d</i> = 0.3 | 8-node Solid | Neo-Hookean <i>c</i> = 0.3448, <i>d</i> = 0.3 | 8-node Solid |
| Annular Collagen fibers | Isotropic Elastic <i>E</i> = 175 MPa A = 0.76 mm ² | | 2-node Cable | Calibrated $\sigma - \varepsilon$ Non-Calibrated $\sigma - \varepsilon$ | Spring Elements | Isotropic Elas <i>E</i> = 550–357.5 M A = 0.76–0.35 n Change by lay | 1Pa um ² | 2-node Link | Non-linear and dependent on the distance from the disc centre | Spring Element | Non Linear | 2-node Link |
| Nucleus polposus | Isotropic Elastic E = 1 MPa v = 0.499 | | 8-node Solid | | - | Incompressible $E = 1666.7 \text{ MI}$ | Fluid Pa | 8-node Fluid | Incompressible Fluid | Fluid Element | Incompressible Fluid | Fluid Element |
| Ligaments ALL PLL LF TL CL IL SL | $\begin{array}{c} E (MPa) \\ 7.8-20 (c \leq 12\%) \\ 10-20 (c \leq 11\%) \\ 15-19.5 (c \leq 6.2\%) \\ 10-58.7 (c \leq 18\%) \\ 7.5-32.9 (c \leq 25\%) \\ 10-11.6 (c \leq 14\%) \\ 8-15 (c \leq 20\%) \end{array}$ | A (mm ²) 63.7 20.0 40.0 1.8 30.0 40.0 30.0 | Calibrated Force-Deflection curves Non-Calibrated Force-Deflection curves | Spring Elements | | E (MPa) 7.8 10 15 10 8 10 8 10 8 | A (mm ²) 24 14.4 40.0 3.6 30.0 26 23 | 2-node Link | Non Linear | Spring Eléments | Non Linear | 2-node Solid |
| Facet Joint | - | | - | Contact Frictionless | - | Sliding Conta | ct | 8-node Contact | Soft Contact | - | Soft Contact | - |
| Follower | - | | - | - | - | - | | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - |

Table A1. The main information extracted from [36–40].

| | Zander et al. (20 | 09) [21] | Ayturk et al. (2010 |) [14] | Manek et al. (20 | 12) [<u>41</u>] | Weisse et al. (2 | 2012) [42] | Kiapour et al. (2012) [| 15] |
|---|--|-----------------|---|-----------------|---|--------------------------------|--|--|---|------------------|
| Anatomical Component | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type |
| Cortical Bone | Isotropic Elastic E = 10,000 MPa $\nu = 0.3$ | 8-node Solid | Transversely Isotropic $E_{11} = 8000 \text{ MPa}, v_{12} = 0.4$ $E_{22} = 8000 \text{ MPa}, v_{13} = 0.35$ $E_{33} = 12,000 \text{ MPa}, v_{23} = 0.3$ | 8-node Solid | Isotropic Elastic E = 16,000 MPa v = 0.25 | Shell Element | Isotropic Elastic E depending on $\rho_{CT_{scan}}$ $\nu = 0.3$ | pending on $\rho_{CT_{scan}}$ | | 8-node Solid |
| Cancellous Bone | Transversely Isotropic $E_1 = 200 \text{ MPa}, v_1 = 0.45$ $E_2 = 140 \text{ MPa}, v_2 = 0.315$ | 8-node Solid | Based on CT scans | 8-node Solid | Isotropic Elastic E = 120 MPa $\nu = 0.25$ | 8-node Solid | E depending on $\rho_{CT_{scan}}$ $\nu = 0.3$ | 8-node Solid | Isotropic Elastic $E = 100 \text{ MPa } \nu = 0.2$ | 8-node Solid |
| Posterior bone elements | Isotropic Elastic E = 3500 MPa $\nu = 0.25$ | 8-node Solid | Isotropic Elastic E = 3500 MPa v = 0.3 | 8-node Solid | - | 8-node Solid | - | - | Cortical Bone $E = 12,000 \text{ MPa}, \nu = 0.3$ Cancellous Bone $E = 100 \text{ MPa}, \nu = 0.2$ | 8-node Solid |
| Cartilaginous Endplate | Neo-Hookean $c_{10} = 0.3448, d_1 = 0.43$ | - | Isotropic Elastic8-nodeIsotropic Elastic8-nodeNeo-Hokean8-node $E = 23.8$ MPa, $\nu = 0.4$ Solid $E = 500$ MPa, $\nu = 0.25$ 8-node Solid $c_1 = 0.3448, d_1 = 0.3$ Solid | | - | - | | | | |
| Annular ground substance | Neo-Hookean $c_{10} = 0.3448, d_1 = 0.3$ | 8-node Solid | Fiber reinforced Yeoh material $c_{10} = 0.0146, c_{20} = -0.0189$ $c_{30} = 0.041$ $a_3 = 0.03, b_3 = 120.00$ | 8-node Solid | Two Ring Layer Isotropic Elastic $E_1 = 30$ MPa, $\nu_1 = 0.37$ $E_2 = 18$ MPa, $\nu_2 = 0.41$ | 8-node Link | Ogden Different values | 8-node Solid | Neo-Hookean $c_{10} = 0.3448, d_1 = 0.3$ | 8-node Solid |
| Annular Collagen fibers | Non-Linear dependent on the distance from the disc centre | Rebar | - | - | - | - | Force–displacement curve | 8-node Solid | Isotropic Elastic $E = 357-550$ MPa, $\nu = 0.3$ | Rebar |
| Nucleus polposus | Incompressible | Fluid | Isotropic Elastic , $E = 1$ MPa $\nu = 0.499$ | - | Isotropic Elastic $E = 2$ MPa, $\nu = 0.499$ | 8-node Fluid | Mooney Rivlin $c_1 = 0.12, c_2 = 0.03$ | 8-node Solid | Incompressible Fluid $E = 1$ MPa, $\nu = 0.499$ | Fluid Element |
| Ligaments ALL PLL LF TL CL IL SL | Exponential Non Linear Spring force Elements displacement curves | | Spring Elements | - | - | Force displacement curve | Spring Elements | $\begin{array}{c c c c c c c c c c c c c c c c c c c $ | Truss Elements | |
| Facet Joint | Soft Contact | - | Neo-Hokean $c_{10} = 2$ | - | Isotropic Elastic $E = 2.28$ MPa, $\nu = 0.3$ | 8-node Solid | Isotropic Elastic $E = 24$ MPa, $\nu = 0.45$ | Surface to surface | Unidirectional Gap | - |
| Follower force | Acting in the centre of each vertebral body | - | - | - | - | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - |

Table A2. The main information extracted from [14,15,21,41,42].

| | Little et al. (2 | 013) [43] | Schmidt et al. (2 | 013) [44] | Park et al. (201 | 3) [<u>18]</u> | Kim et al. (2015) [45] | | Erbulut et al. (2015) | 46] |
|---|--|-------------------------------------|--|--------------|--|------------------|---|-----------------|--|-------------------|
| Anatomical Component | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type |
| Cortical Bone | Isotropic Elastic E = 113,000 MPa v = 0.2 | 4-node Shell | Poroelastic Model E = 10,000 MPa v = 0.3 Poroelastic coefficients | - | Isotropic Elastic $E = 12,000 \text{ MPa}, \nu = 0.3$ | Solid Element | | | Isotropic Elastic E = 12,000 MPa v = 0.3 | Solid |
| Cancellous Bone | Isotropic Elastic E = 140 MPa $\nu = 0.2$ | First-Order Break | Poroelastic Model E = 100 MPa $\nu = 0.2$ Poroelastic coefficients | - | $\begin{array}{c} \textbf{Isotropic Elastic} \\ E = 190 \text{ MPa} \\ \nu = 0.2 \end{array} \qquad \begin{array}{c} \textbf{Solid} \\ \text{Element} \end{array} \qquad \begin{array}{c} \textbf{Transversely Iso} \\ E_{xx} = 140 \text{ MPa}, \nu_{xy} \\ E_{yy} = 140 \text{ MPa}, \nu_{xy} \\ E_{zz} = 200 \text{ M} \\ G_{xy} = 48.3 \text{ M} \\ G_{yz} = 48.3 \text{ M} \end{array}$ | | Transversely Isotropic $E_{xx} = 140$ MPa, $v_{xy} = 0.450$ $E_{yy} = 140$ MPa, $v_{xz} = 0.315$ $E_{zz} = 200$ MPa $G_{xy} = 48.3$ MPa $G_{yz} = 48.3$ MPa $G_{xz} = 48.3$ MPa | - | Isotropic Elastic E = 450 MPa $\nu = 0.25$ | Solid |
| Posterior bone elements | Quasi-Rigid | Linear Beam | - | - | Isotropic Elastic $E = 35,000 \text{ MPa}, \nu = 0.25$ | Solid Element | Isotropic Elastic $E = 3500 \text{ MPa}, \nu = 0.25$ | - | Isotropic Elastic $E = 3500 \text{ MPa}, \nu = 0.25$ | Solid |
| Cartilaginous Endplate | - | - | Poroelastic Model $E = 10,000$ MPa, $\nu = 0.3$ Other coefficients | - | Isotropic Elastic $E = 23.8 \text{ MPa}, v = 0.4$ | Solid Element | Isotropic Elastic E = 24 MPa, $v = 0.4$ | - | Modelled | - |
| Annular ground substance | Mooney-Rivlin $c_{10} = 0.7, c_{01} = 0.2$ | First-Order Brick | Fiber reinforced Poroelastic Model Neo-Hookean $c_{10} = 1.23$ MPa D = 0.688 MPa ⁻¹ | - | Mooney-Rivlin $c_1 = 0.18, c_2 = 0.045$ | Solid Element | Isotropic Elastic $E = 4.2 \text{ MPa}, \nu = 0.4$ | - | Neo-Hookean $c_{10} = 0.3448,$ $D_1 = 0.3$ | Solid |
| Annular Collagen fibers | Isotropic Elastic $E = 500 \text{ MPa}, \nu = 0.3$ | Rebar | Rebar applied to Ground Substance | - | Hyperelastic Strain rate dependent | Truss | Isotropic Elastic $E = 358-550 \text{ MPa}, \nu = 0.3$ | - | Isotropic Elastic $E = 357-550$ MPa, $\nu = 0.3$ | Rebar |
| Nucleus polposus | Hydrostatic fluid Incompressible | 4-node Fluid | Poroelastic Model Neo-Hookean $c_{10} = 0.627 \text{ MPa},$ $D = 2.475 \text{ MPa}^{-1}$ | - | Different value E | Fluid Element | Isotropic Elastic $E = 1$ MPa, $\nu = 0.499$ | - | Isotropic Elastic E = 9 MPa, $v = 0.499$ | Solid |
| Ligaments ALL PLL LF TL CL IL SL | Non Linear | Connector and Spring Elements | Modelled | - | Hyperelastic Material Strain rate dependent | Truss | $\begin{array}{c c c c c c c c c c c c c c c c c c c $ |) - | $\begin{array}{c c} \mathbf{E} \left(\mathbf{MPa}\right) & \nu \\ 7.8{-}20 \left(\varepsilon \leqslant 12\% \right) & 0.3 \\ 10{-}20 \left(\varepsilon \leqslant 11\% \right) & 0.3 \\ 15{-}19.5 \left(\varepsilon \leqslant 6.2\% \right) & 0.3 \\ 10{-}58.7 \left(\varepsilon \leqslant 18\% \right) & 0.3 \\ 7.5{-}32.9 \left(\varepsilon \leqslant 25\% \right) & 0.3 \\ 10{-}11.6 \left(\varepsilon \leqslant 14\% \right) & 0.3 \\ 8{-}15 \left(\varepsilon \leqslant 20\% \right) & - \end{array}$ | Truss Elements |
| Facet Joint | - | - | Surface to Surface Frictionless | - | Surface to Surface Soft contact | - | Surface to Surface Frictionless | - | Gap contact | - |
| Follower force | - | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - |

Table A3. The main information extracted from [18,43–46].

| | Barthelemy e (2015) [47 | | Xu et al. (2016) [48] | | Zander e (2016) [4 | | Kang et al. (2017) [50] | | Fan et al. (2017) [47] | |
|---|--|--------------|--|---|---|------------------|---|--|---|-------------------|
| Anatomical Component | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type |
| Cortical Bone | Isotropic Elastic E = 12,000 MPa $\nu = 0.4$ | - | Isotropic Elastic $E = 12,000 \text{ MPa}, \nu = 0.3$ | 8-node Solid | Isotropic Elastic <i>E</i> = 10,000 MPa | Shell Element | $\begin{array}{l} \textbf{Transversely Elastic} \\ E_{xx} = 11,300 \text{ MPa}, \nu_{xy} = 0.484 \\ E_{yy} = 11,300 \text{ MPa}, \nu_{xz} = 0.203 \\ E_{zz} = 22,000 \text{ MPa} \\ G_x = 3800 \text{ MPa} \\ G_y = 5400 \text{ MPa} \\ G_z = 5400 \text{ MPa} \end{array}$ | Solid | Isotropic Elastic E = 12,000 MPa v = 0.3 | 3-node Solid |
| Cancellous Bone | Isotropic ElasticIsotropic Elastic $E = 140$ MPa, $\nu = 0.45$ $E = 100$ MPa, $\nu = 0.20$ | | 8-node Solid | Transversely Elastic <i>E</i> = 100–300 MPa | Transversely Elastic $E_{xx} = 140$ MPa, $v_{xy} = 0.45$ $E_{yy} = 140$ MPa, $v_{xz} = 0.315$ $E_{zz} = 200$ MPa $G_x = 48.3$ MPa $G_y = 48.3$ MPa $G_r = 48.3$ MPa | | 4-node Solid | Isotropic Elastic $E = 100 \text{ MPa}, \nu = 0.2$ | 4-node Solid | |
| Posterior bone elements | Isotropic Elastic $F = 35000 \text{ MPa}_{-17} = 0.30$ | | Isotropic Elastic $E = 35,000 \text{ MPa}, \nu = 0.25$ | 8-node Solid | Isotropic Elastic <i>E</i> = 35,000 MPa | - | Isotropic Elastic4-node $E = 3500$ MPa, $\nu = 0.25$ Solid | | Isotropic Elastic $E = 3500 \text{ MPa}, \nu = 0.25$ | 4-node Solid |
| Cartilaginous Endplate | Isotropic Elastic $E = 1000 \text{ MPa}, \nu = 0.30$ | | | 8-node Solid | E | | Isotropic Elastic $E = 23.89$ MPa, $\nu = 0.40$ | | | 3-node Solid |
| Annular ground substance | und Osmo-poro-viscoelastic - | | Mooney-Rivlin $c_1 = 0.56, c_2 = 0.14, \nu = 0.45$ | 8-node Solid | Neo-Hookean $c_{10} = 0.3448, D_1 = 0.3$ | - | $\begin{array}{l} \textbf{Mooney-Rivlin} \\ c_1 = 0.2, c_2 = 0.05 \end{array} \qquad \qquad \text{Solid}$ | | Mooney-Rivlin $c_{10} = 0.18, c_{01} = 0.045$ | 8-node Solid |
| Annular Collagen fibers | - | - | Nonlinear $\sigma - \epsilon$ curve | 4-node Shell Rebar | Nonlinear $\sigma - \epsilon$ curve | - | Different value E | Truss | - | - |
| Nucleus polposus | Osmo-poro-viscoelastic | - | Mooney-Rivlin $c_{10} = 0.12, c_{01} = 0.09, \nu = 0.4999$ | 8-node Solid | Hydrostatic | - | Isotropic Elastic $E = 1$ MPa, $\nu = 0.499$ | 8-node Solid | Mooney-Rivlin $c_{10} = 0.12, c_{01} = 0.09, \nu = 0.4999$ | Solid |
| Ligaments ALL PLL LF TL CL IL SL | Hypoelastic | Truss | Non-Linear $\sigma - \epsilon$ curve | 4-node Shell | Non-Linear $\sigma - \varepsilon$ curve | - | $\begin{array}{c c c c c c c c c c c c c c c c c c c $ | Truss Elements | $\begin{array}{cccc} {\bf E} ({\bf MPa}) & \nu \\ 7.8-20 (\varepsilon \leqslant 12\%) & 0.3 \\ 10-20 (\varepsilon \leqslant 11\%) & 0.3 \\ 15-19.5 (\varepsilon \leqslant 6.2\%) & 0.3 \\ 10-58.7 (\varepsilon \leqslant 18\%) & 0.3 \\ 7.5-32.9 (\varepsilon \leqslant 25\%) & 0.3 \\ 10-11.6 (\varepsilon \leqslant 14\%) & 0.3 \\ 8-15 (\varepsilon \leqslant 20\%) & - \end{array}$ | Truss Elements |
| Facet Joint | Surface to Surface Frictionless | - | Soft frictionless contact | - | Surface to Surface contact | - | Surface to Surface frictionless | - | Surface to Surface frictionless | - |
| Follower force | - | - | Acting in the centre of each vertebral body | - | - | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - |

Table A4. The main information extracted from [47–51].

| | Finley et al. (20 | 18) [52] | Zhou et al. (2019 |) [53] | Fan et al. (2019) [54] | Fan et al. (2019) [54] | | 5] | Haj-Ali et al. (2019) [56] | |
|---|---|--------------------|--|--------------|---|------------------------|---|-----------------|---|------------------|
| Anatomical Component | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type |
| Cortical Bone | $\begin{array}{c} \textbf{Transversely Elastic} \\ E_1 = 8000 \text{ MPa} \\ \nu_{12} = 0.4 \\ E_2 = 8000 \text{ MPa} \\ \nu_{23} = 0.3 \\ E_3 = 12,000 \text{ MPa} \\ \nu_{31} = 0.35 \end{array}$ | Solid Element | Isotropic Elastic E = 12,000 MPa, $v = 0.3$ | - | Isotropic Elastic $E = 12,000 \text{ MPa}, \nu = 0.3$ | Solid Element | $\begin{array}{c} \textbf{Transversely Elastic} \\ E_{xx} = 11,300 \text{ MPa}, \nu_{xy} = 0.484 \\ E_{xz} = 11,300 \text{ MPa}, \nu_{xz} = 0.203 \\ E_{zz} = 22,000 \text{ MPa} \\ G_x = 3800 \text{ MPa} \\ G_y = 5400 \text{ MPa} \\ G_z = 5400 \text{ MPa} \end{array}$ | - | Isotropic Elastic E = 12,000 MPa v = 0.3 | Solid Element |
| Cancellous Bone | Neo-Hookean E = 100 MPa v = 0.2 | Solid Element | $\begin{array}{l} {\bf Transversely Elastic} \\ E_{xx} = 140 \ {\rm MPa}, \nu_{xy} = 0.45 \\ E_{yy} = 140 \ {\rm MPa}, \nu_{xz} = 0.315 \\ E_{zz} = 200 \ {\rm MPa} \\ G_x = 48.3 \ {\rm MPa} \\ G_y = 48.3 \ {\rm MPa} \\ G_z = 48.3 \ {\rm MPa} \end{array}$ | - | Isotropic Elastic E = 100 MPa $\nu = 0.2$ | Solid | $\begin{array}{l} \textbf{Transversely Elastic} \\ E_{xx} = 140 \text{ MPa}, \nu_{xy} = 0.45 \\ E_{yy} = 140 \text{ MPa}, \nu_{xz} = 0.315 \\ E_{zz} = 200 \text{ MPa} \\ G_x = 48.3 \text{ MPa} \\ G_y = 48.3 \text{ MPa} \\ G_z = 48.3 \text{ MPa} \end{array}$ | - | Isotropic Elastic $E = 100 \text{ MPa}, \nu = 0.2$ | Solid Element |
| Posterior bone elements | Neo-Hookean E = 35,000 MPa $\nu = 0.30$ | - | Isotropic Elastic E = 35,000 MPa v = 0.25 | - | Isotropic Elastic E = 35,000 MPa $\nu = 0.25$ | - | Isotropic Elastic $E = 3500 \text{ MPa}, \nu = 0.25$ G = 1400 MPa | - | - | - |
| Annular Collagen fibers | Exponential power $\alpha = 65 \text{ MPa}, \beta = 2 \text{ MPa}$ $\zeta = 0.296 \text{ MPa}$ | - | Annular Lamellae Non-linear | - | Isotropic Elastic <i>E</i> = 360–550 MPa | - | Two layers $k_1 = 3$ MPa, $k_2 = 45$ MPa | - | - | - |
| Cartilaginous Endplate | Neo-Hookean $E = 23.8 \text{ MPa}, \nu = 0.42$ | - | Isotropic Elastic $E = 24$ MPa, $\nu = 0.40$ | - | Isotropic Elastic $E = 23.8 \text{ MPa}, \nu = 0.4$ | Solid | - | - | - | - |
| Annular ground substance | Holmes-Mow $E = 1$ MPa, $\nu = 0.4$ $\beta = 3.4$ | - | Mooney-Rivlin $c_1 = 0.18, c_2 = 0.045$ | - | Mooney-Rivlin $c_1 = 0.18, c_2 = 0.045$ | Solid Element | Neo-Hookean $c_{10} = 0.250$ | Solid | Isotropic Elastic $E = 8.4$ MPa, $\nu = 0.45$ | Solid |
| Nucleus polposus | Neo-Hookean $E = 1$ MPa, $\nu = 0.49$ | - | Mooney-Rivlin $c_{10} = 0.12, c_{01} = 0.03$ | - | Mooney-Rivlin $c_{10} = 0.12, c_{01} = 0.03$ | Solid | Mooney-Rivlin $c_{10} = 0.12, c_{01} = 0.03$ | 8-node Solid | Isotropic Elastic $E = 1 \text{ MPa } \nu = 0.4999$ | Solid |
| Ligaments ALL PLL LF TL CL IL SL | Non-linear | Spring Elements | Non-Linear force-deflection relation | - | $\begin{array}{c c c c c c c c c c c c c c c c c c c $ | Truss | Tension-only | - | Different modelling Non-linear E varying on ɛ-rate | - |
| Facet Joint | Neo-Hookean $E = MPa, \nu = 0.4$ | - | Isotropic Elastic $E = 35$ MPa, $\nu = 0.4$ | - | - | - | Non-Linear Isotropic elastic Surface to surface | - | Contact Frictionless | - |
| Follower force | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - | Acting in the centre of each vertebral body | - | | - | - | - |

Table A5. The main information extracted from [52–56].

| | Affolter ((2020) [| | Godinho et al. (2021) [58] | | Sengul et al. (2021) [59] | | Turbucz et al. (2022) [60] | | Sanjay et al. (2022) [61] | | Tan et al. (2022) [24] | |
|---|---|------------------|---|------------------|--|------------------|---|------------------|---|------------------|---|-------------------|
| Anatomical Component | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type | Constitutive Model | Element Type |
| Cortical Bone | Transversely Elastic | Solid Element | Isotropic Elastic $E = 1200 \text{ MPa}, \nu = 0.3$ | Solid | Isotropic Elastic $E = 12,000 \text{ MP}, \nu = 0.3$ | Shell Element | Isotropic Elastic $E = 10,000 \text{ MPa}, \nu = 0.3$ | Solid | Isotropic Elastic $E = 12,000 \text{ MPa}, \nu = 0.3$ | Solid Element | Isotropic Elastic $E = 12,000 \text{ MPa}, \nu = 0.3$ | Solid Element |
| Cancellous Bone | Transversely Elastic | Solid Element | Transversely Elastic $E = 200 \text{ MPa}, \nu = 0.315$ | Solid Element | Isotropic Elastic $E = 100 \text{ MPa}, \nu = 0.2$ | Solid | Isotropic Elastic $E = 100$ MPa, $\nu = 0.2$ | Solid Element | Isotropic Elastic $E = 100 \text{ MPa}, \nu = 0.3$ | Solid Element | Isotropic Elastic $E = 100$ MPa, $\nu = 0.3$ | Solid Element |
| Posterior bone elements | Transversely Elastic | Solid Element | - | - | - | - | Isotropic Elastic $E = 3500 \text{ MPa}, \nu = 0.25$ | Solid Element | - | - | Isotropic Elastic $E = 3500 \text{ MPa}, \nu = 0.25$ | Solid Element |
| Cartilaginous Endplate | Modelled | - | Modelled | - | Isotropic Elastic $E = 23.8 \text{ MPa}, \nu = 0.4$ | Solid Element | Isotropic Elastic $E = 23.8 \text{ MPa}, \nu = 0.42$ | Solid Element | Isotropic Elastic $E = 23.8 \text{ MPa}, \nu = 0.4$ | Solid | Isotropic Elastic E = 24 MPa | Solid |
| Annular ground substance | Hyperelastic Model | Solid Element | Holzapfel $D_1 = 0.254 \text{ MPa}^{-1}$ $k_1 = 12 \text{ MPa}$ $k_2 = 300, k = 0.1$ | Solid | Mooney-Rivlin $c_{10} = 0.13$ $c_{01} = 0.03$ D = 0.6 | Solid Element | Mooney-Rivlin $c_{10} = 0.18$ $c_{01} = 0.045$ | Solid | Isotropic Elastic $E = 9$ MPa, $\nu = 0.4$ | Solid | Mooney-Rivlin | Solid |
| Annular Collagen fibers | Non-Linear | Rebar | - | - | Isotropic Elastic E = 360-550 MPa $\nu = 0.45$ | Rebar | Non-Linear $\sigma - \varepsilon$ -curve | Truss Element | - | - | Non-Linear $\sigma - \varepsilon$ - calibrated curve | Spring Element |
| Ligaments ALL PLL LF TL CL IL SL | Ogdenr 3rd Order | - | E (MPa) A (mm ²) 20 75.9 10 1.6 13 39 12 1.8 7.5 19 9.8 1.8 8.8 6 | - | Non-Linear | Connector | Non-Linear | Spring | E (MPa) 45.20 26.49 43.71 2.77 - 35.50 12.72 | - | Tension-only | Spring |
| Nucleus polposus | Fluid Cavity | Fluid | $\begin{array}{c} \textbf{Mooney-Rivlin} \\ c_{10} = 0.315 \\ c_{01} = 0.03 \\ D_1 = 0.667 \end{array}$ | - | Isotropic Elastic E = 1 MPa v = 0.499 | Solid | Mooney-Rivlin $c_{10} = 0.12, c_{01} = 0.03$ | 8-node Solid | Isotropic Elastic E = 0.1 MPa v = 0.49 | Solid | Mooney-Rivlin | - |
| Facet Joint | - | - | Gap contact Surface to surface | - | Gap contact | - | Neo-Hookean $c_{10} = 5.36, D_1 = 0.04$ | Solid | Gap contact | - | Neo-Hookean | Solid |
| Follower force | Acting in the centre of each vertebral body | - | - | - | - | - | Acting in the centre of each vertebral body | - | - | - | Acting in the centre of each vertebral body | - |

Table A6. The main information extracted from [24,57–61].

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