

Tamsin Meaney · Christiane Benz ·
Antonella Montone · Benedetto Di Paola ·
Michele G. Fiorentino *Editors*

Engaging with Mathematics in the Early Years

Results from the POEM6 Conference

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